

Romain Contant
Advisor : Markus Q. Huber

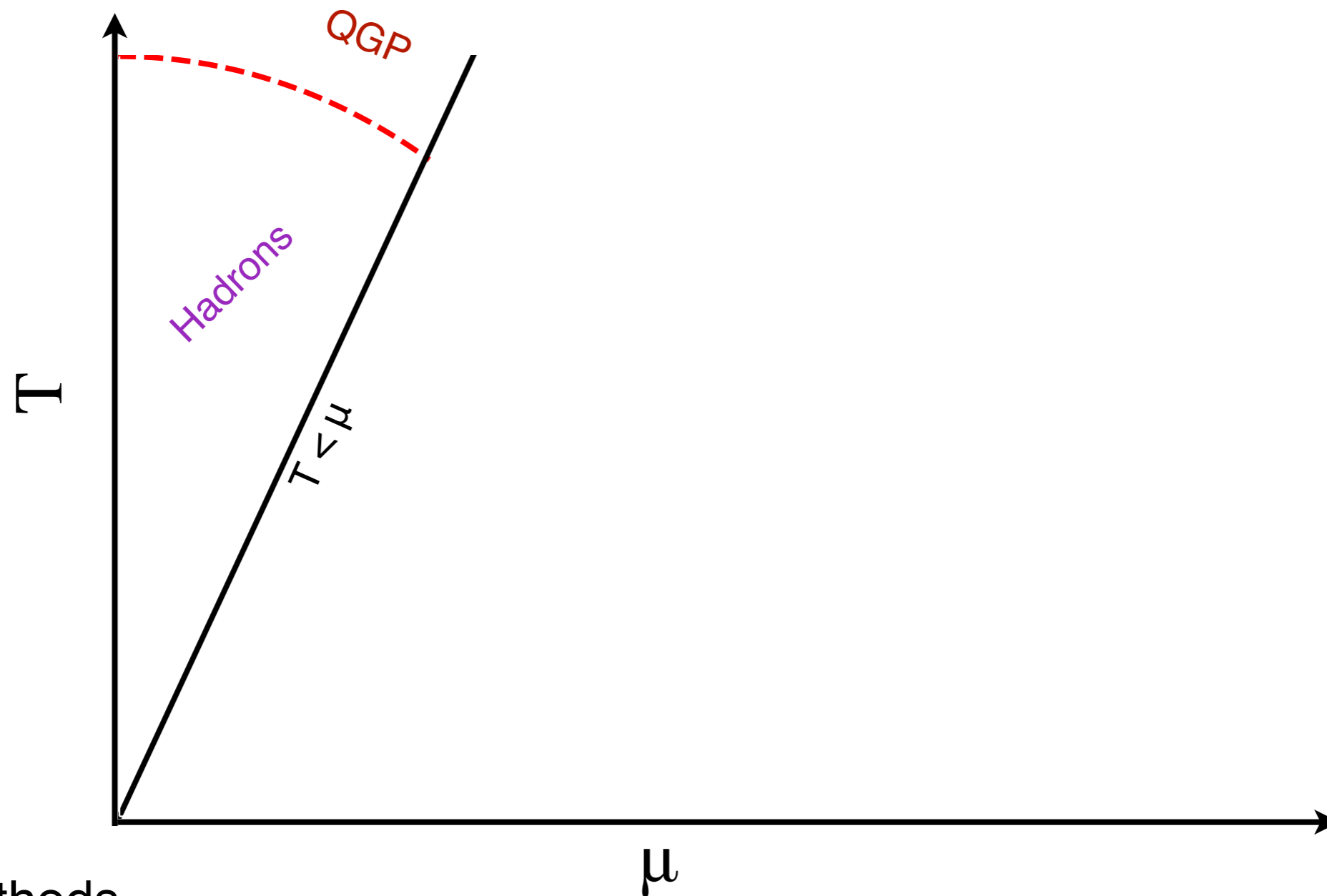
Phase transitions of QCD and QCD-like theories from Dyson-Schwinger equations

arXiv:1706.00943

arXiv:1709.03326



- The phase diagram of QCD

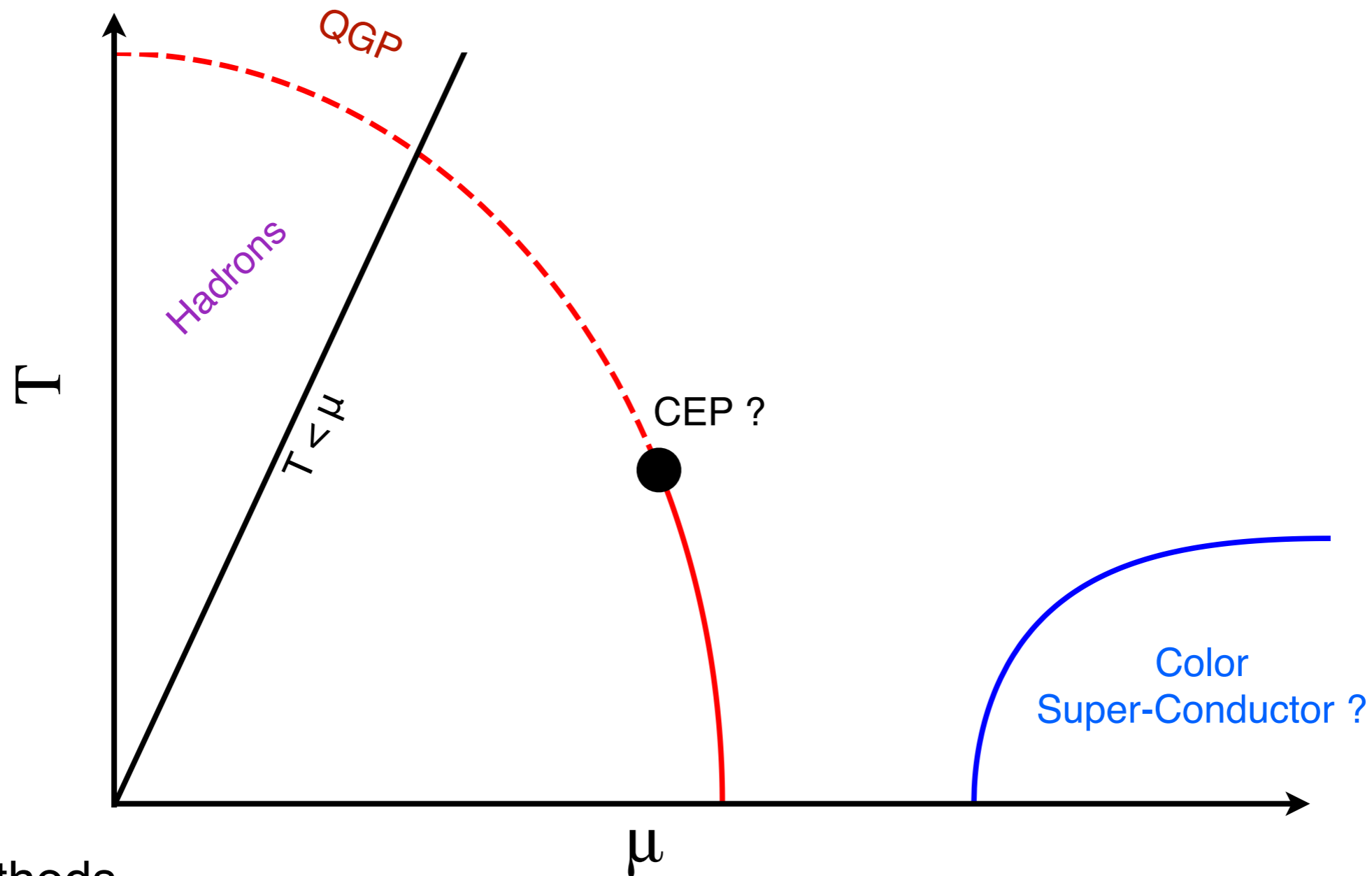


- Methods

- Lattice QCD

- Sign problem

- The phase diagram of QCD



- Methods

- Lattice QCD

- Sign problem

- Effective Models

- Fixing parameters

- Functional methods

- Truncation and modeling

QCD

Lattice QCD



sign problem

Functional Methods






Truncation

1

Introduction

QCD-like theories

QCD-like

-  A theory with dynamical mass generation
-  Confinement and asymptotic freedom
-  A positive fermion determinant

Minimal
modification of QCD

Lattice QCD



~~sign problem~~

Functional Methods



Truncation

1

Introduction

Motivation for QCD-like theories

QCD-like

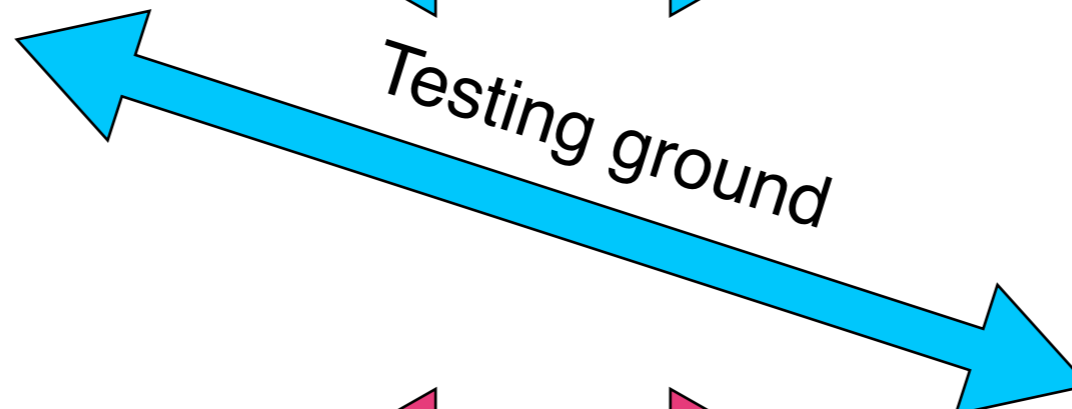
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Minimal modification of QCD

Lattice QCD



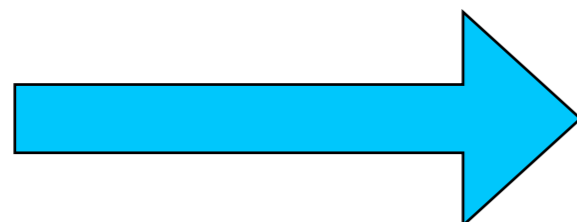
~~sign problem~~



Functional Methods



Truncation



Apply the truncation to physical QCD

1

Introduction

Motivation for QCD-like theories

- SU(2)

→ SU(2) for even number of degenerated quark flavors possesses a positive quark determinant

- G₂

- Subgroup of SO(7) which satisfies an additional cubic constraint

→ All representations are real, allow lattice simulation at $\mu > 0$

1 Introduction

Motivation for QCD-like theories

- $SU(3)$ $SU(2)$ and G_2 have many properties in common

→ Asymptotically free, chiral symmetry breaking, confinement

→ Chiral and deconfinement transition coincide in the quenched case

- Similar functional equations

→ Different Casimir operators of the gauge groups

1 Introduction

Motivation for QCD-like theories

- SU(3) SU(2) and G_2 have many properties in common

➔ Asymptotically free, chiral symmetry breaking, confinement

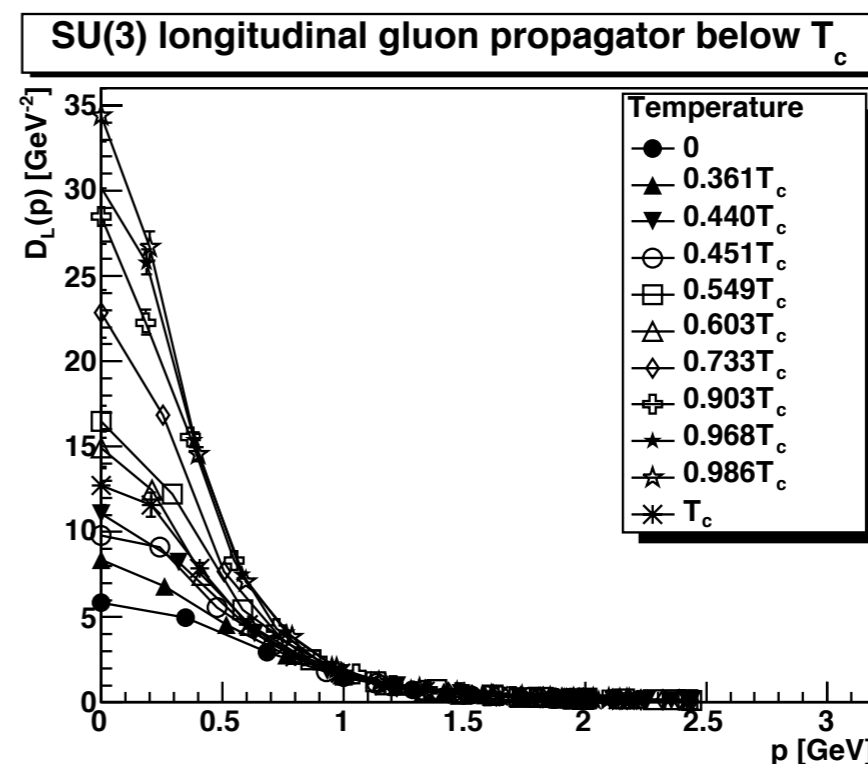
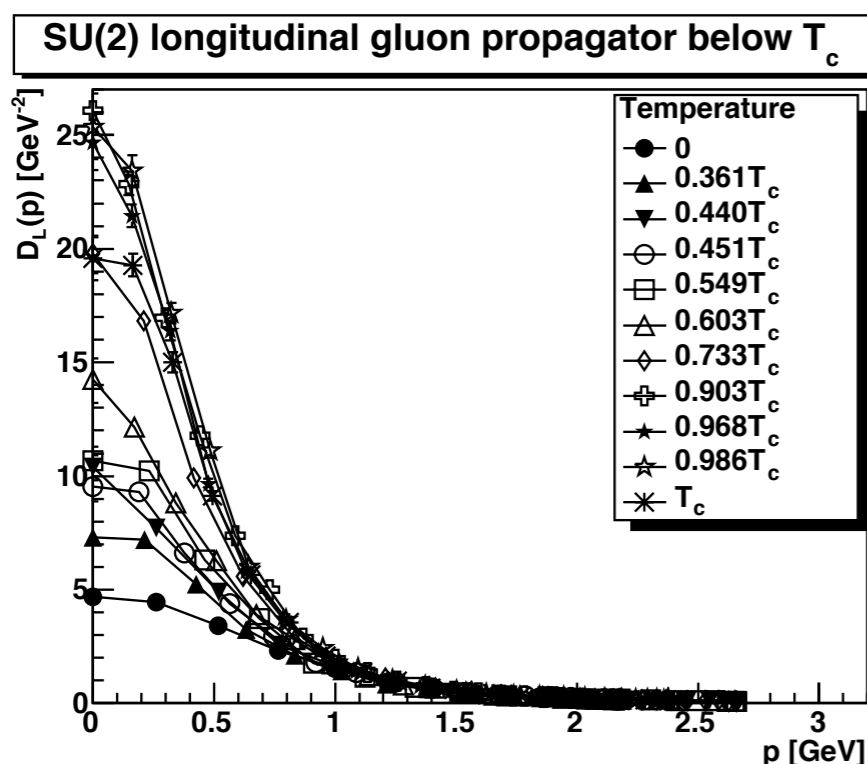
➔ Chiral and deconfinement transition coincide in the quenched case

- Similar functional equations

➔ Different Casimir operators of the gauge groups

- Similarities of the correlation function : SU(2) vs SU(3)

See talk of
O. Hajizadeh



[C.S. Fischer, A. Maas, J.A. Muller (2010)]

1 Introduction

Motivation for QCD-like theories

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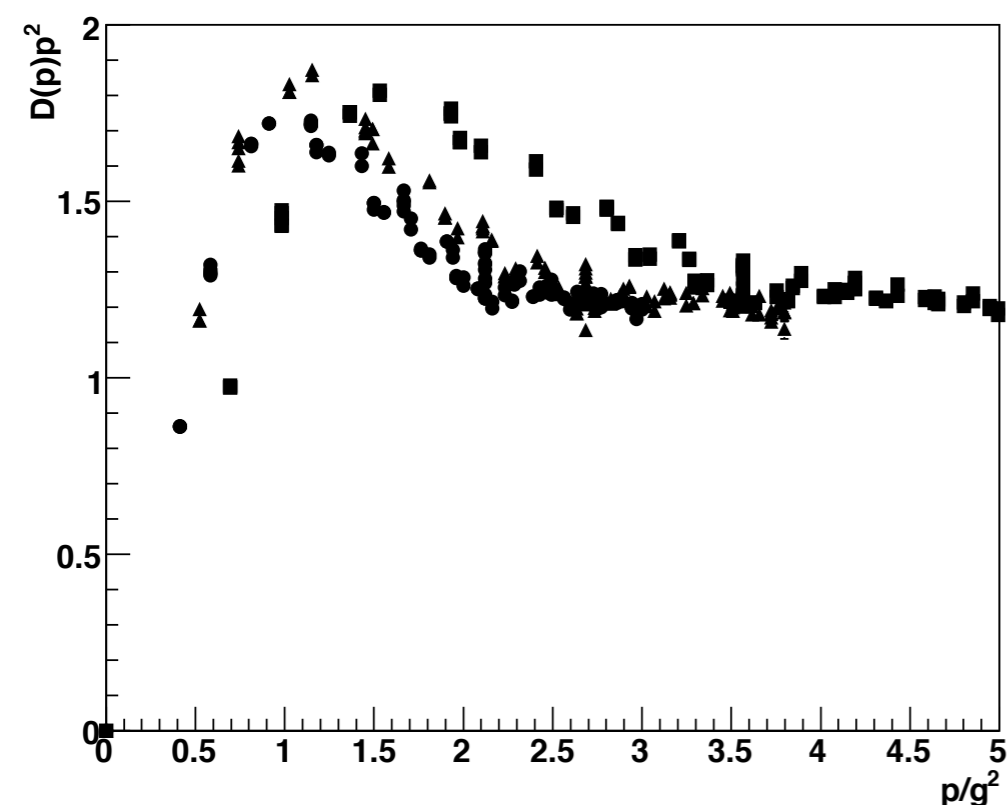
➔ Chiral and deconfinement transition coincide in the quenched case

- Similar functional equations

➔ Different Casimir operators of the gauge groups

- Similarities of the correlation functions : G_2 vs SU(3) vs SU(2) (3 dimensional)

Gluon dressing function



■ SU(3)

▲ G_2

● SU(2)

[A. Maas, S. Olejník (2008)]

1

Introduction

Difference with QCD

● SU(2)

→ Expected to be second order transition for the chiral condensate
(For the quenched system)

→ Bosonic baryons

● G₂

→ Centerless

→ Lattice simulations show a first order transition for confinement

[G. Cossu, M. D'Elia, A. Di Giacomo, B. Lucini, and C. Pica (2007)]

→ Fermionic baryons

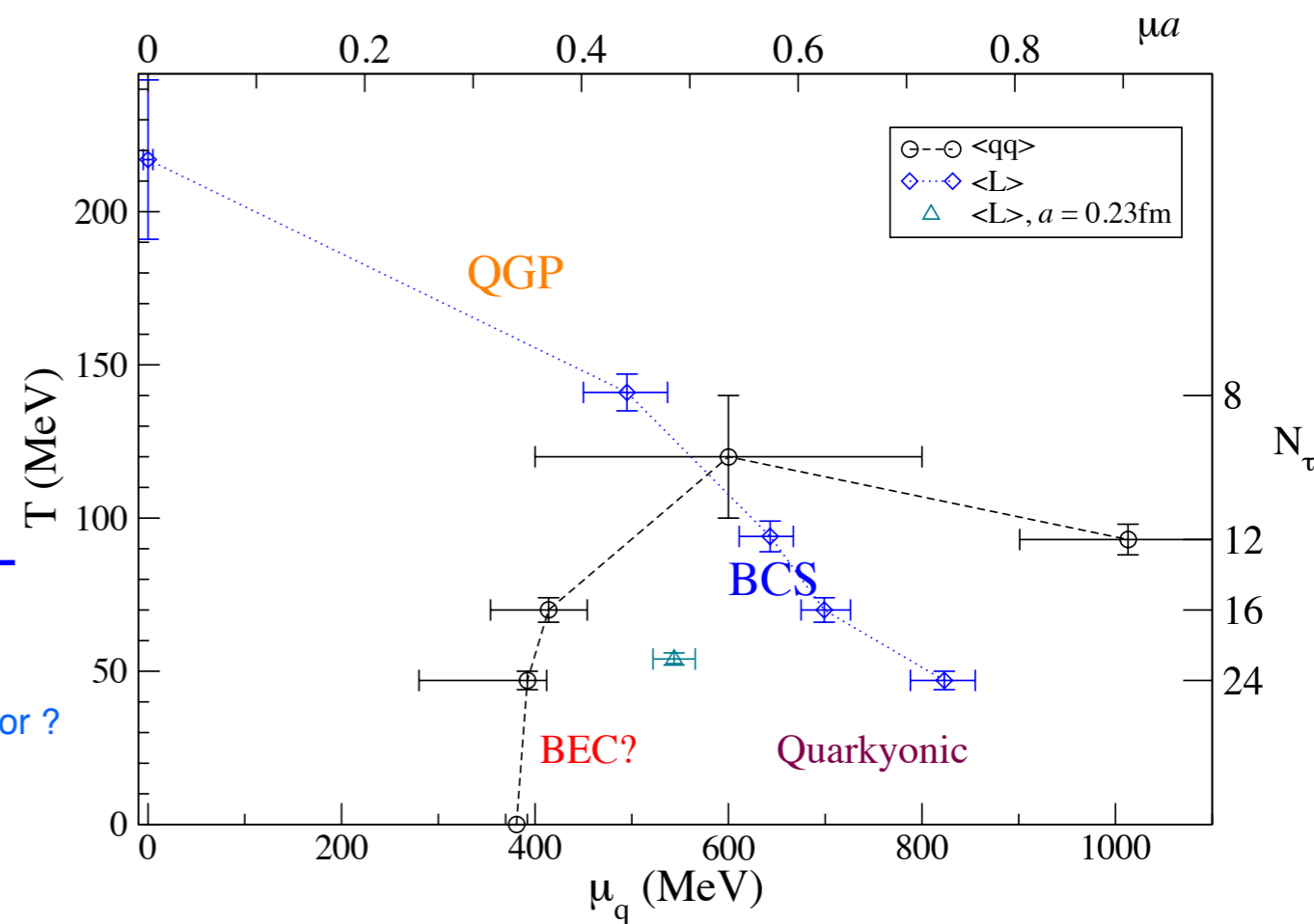
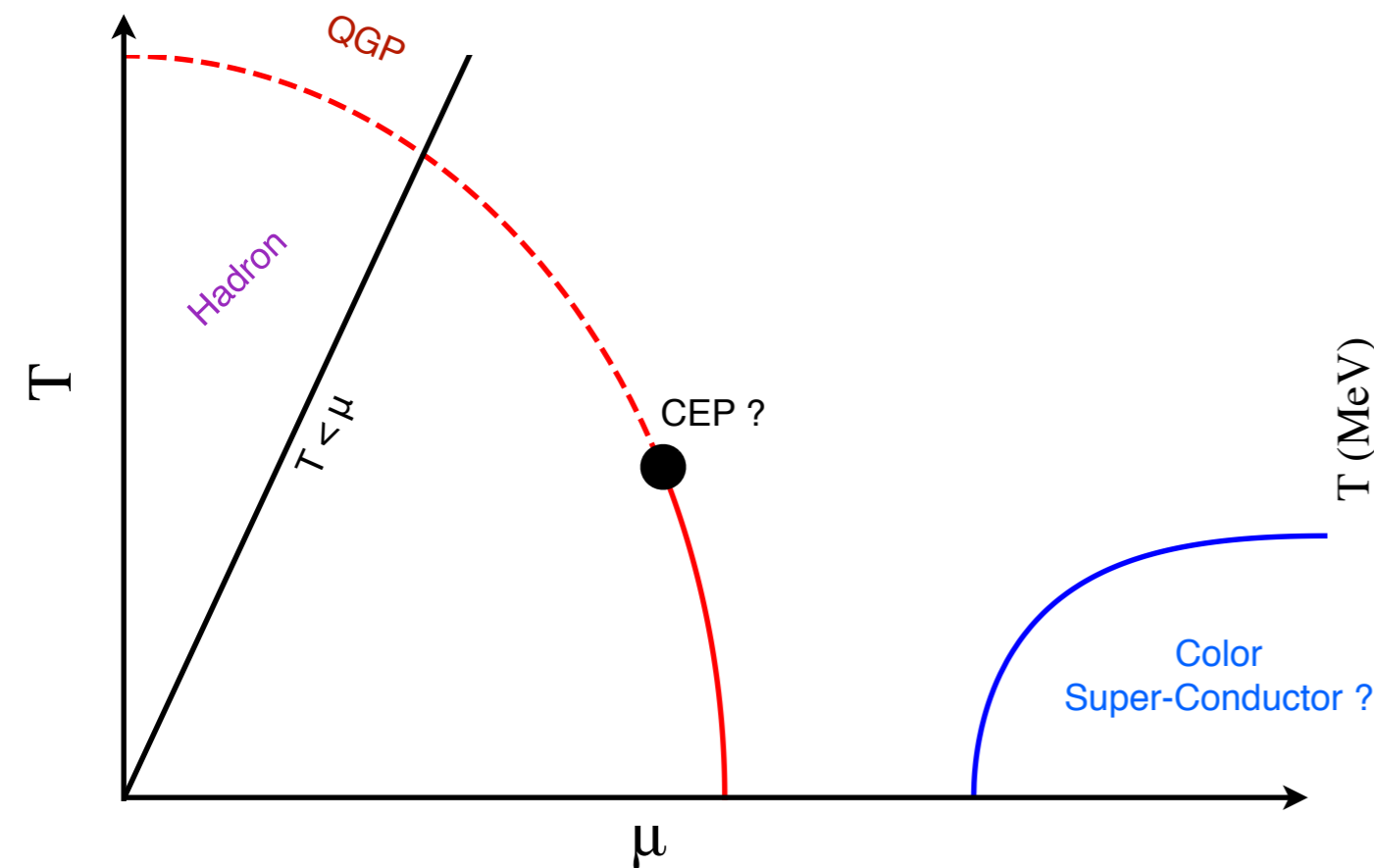
1 Introduction

QCD-like phase diagram

● Phase diagrams of QCD-like theories

● QCD sketch

● SU(2)



Is the same truncation sufficient to describe different gauge groups ?

Diquark condensate : [S. Cotter et al. Phys.rev., vol. D87, pp. 034507, (2013)]

Polyakov loop : [S. Hands et al. Eur.phys.j., vol. C48, pp. 193, (2006)]

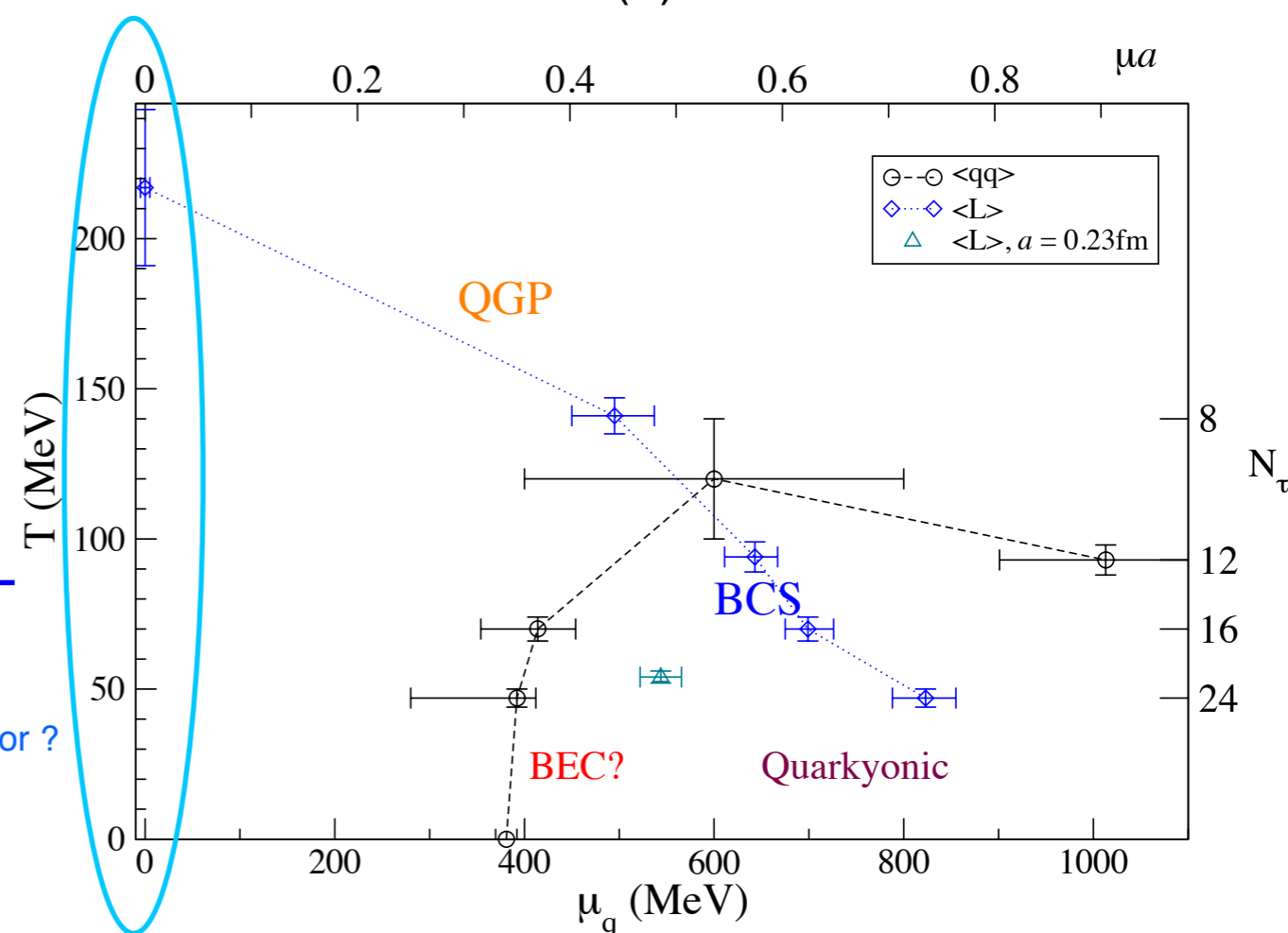
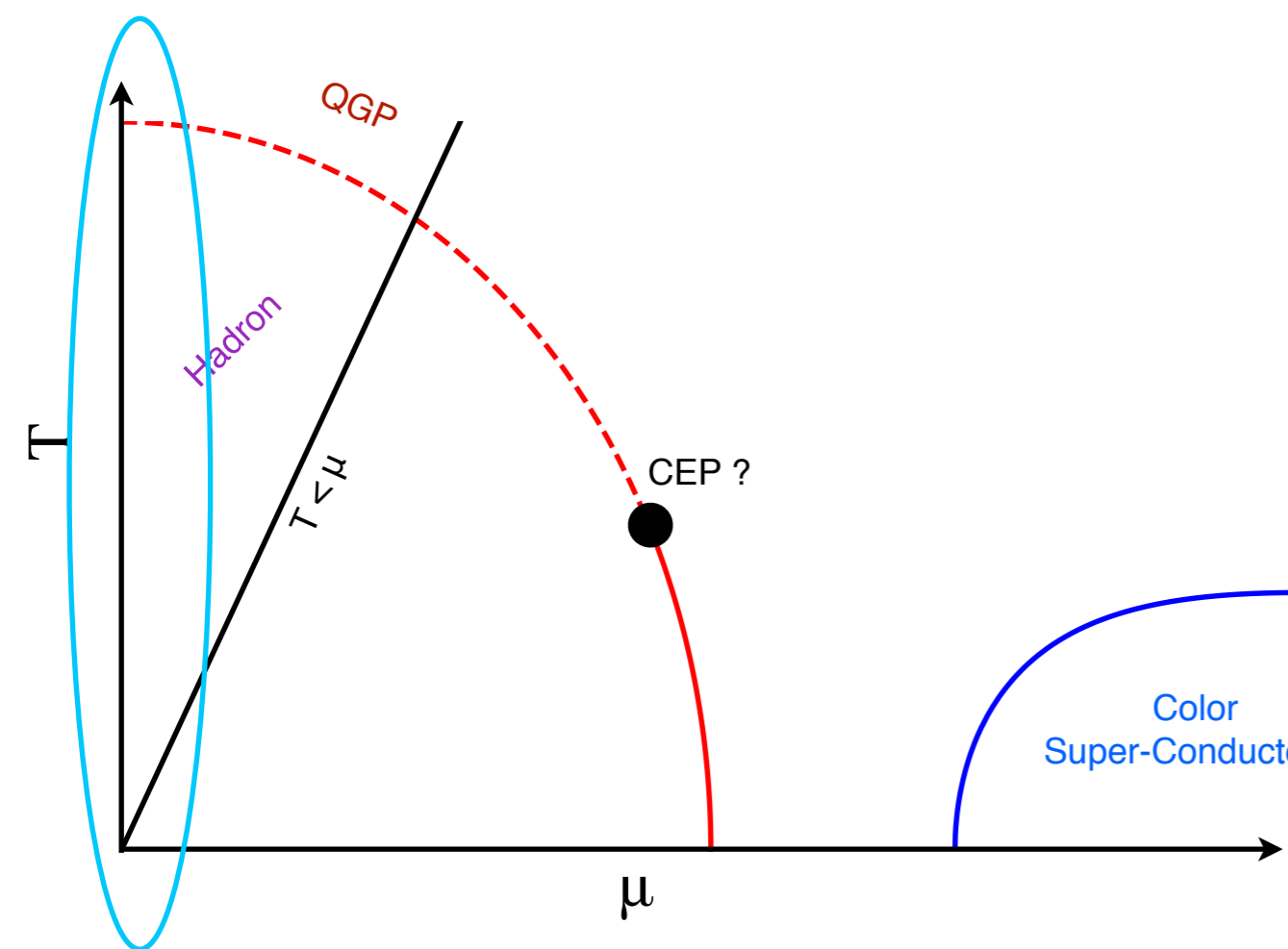
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➔ Study the quark propagator at finite T for QCD and QCD-like theories

Synopsis

1

Introduction

2

Setup

3

Quenched QCD and QCD-like study

4

Unquenching

5

Finite μ

6

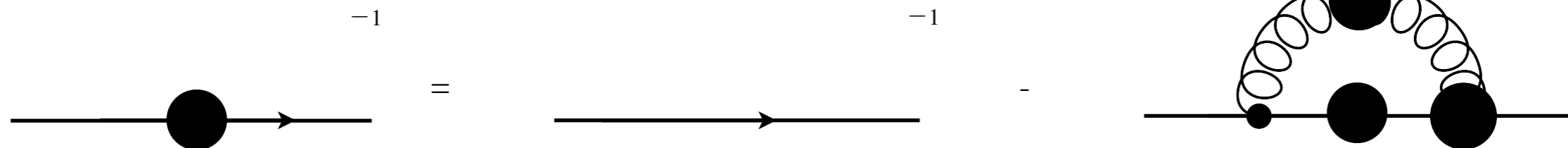
Conclusion

2 Setup Dyson-Schwinger Equation

$$Z = \int d[\Phi] \text{Exp}[-\int S[\Phi] + \Phi J] \longrightarrow W[\Phi] = \text{Log}[Z] \longrightarrow \Gamma[J]$$

Z : Partition function \rightarrow W : Connected Diagrams \rightarrow Γ : irreducible Diagrams

● Example : The gap equation



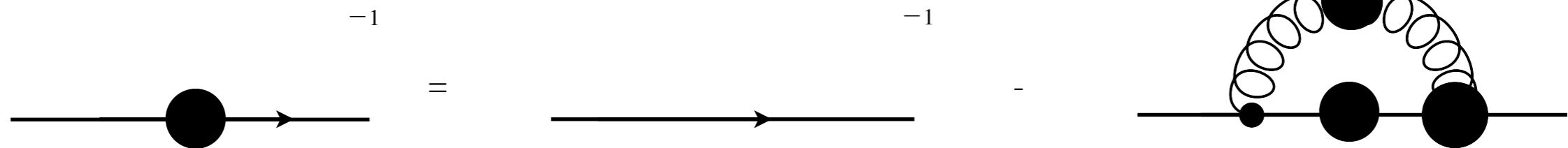
Describe all possible ways of propagation of a quark

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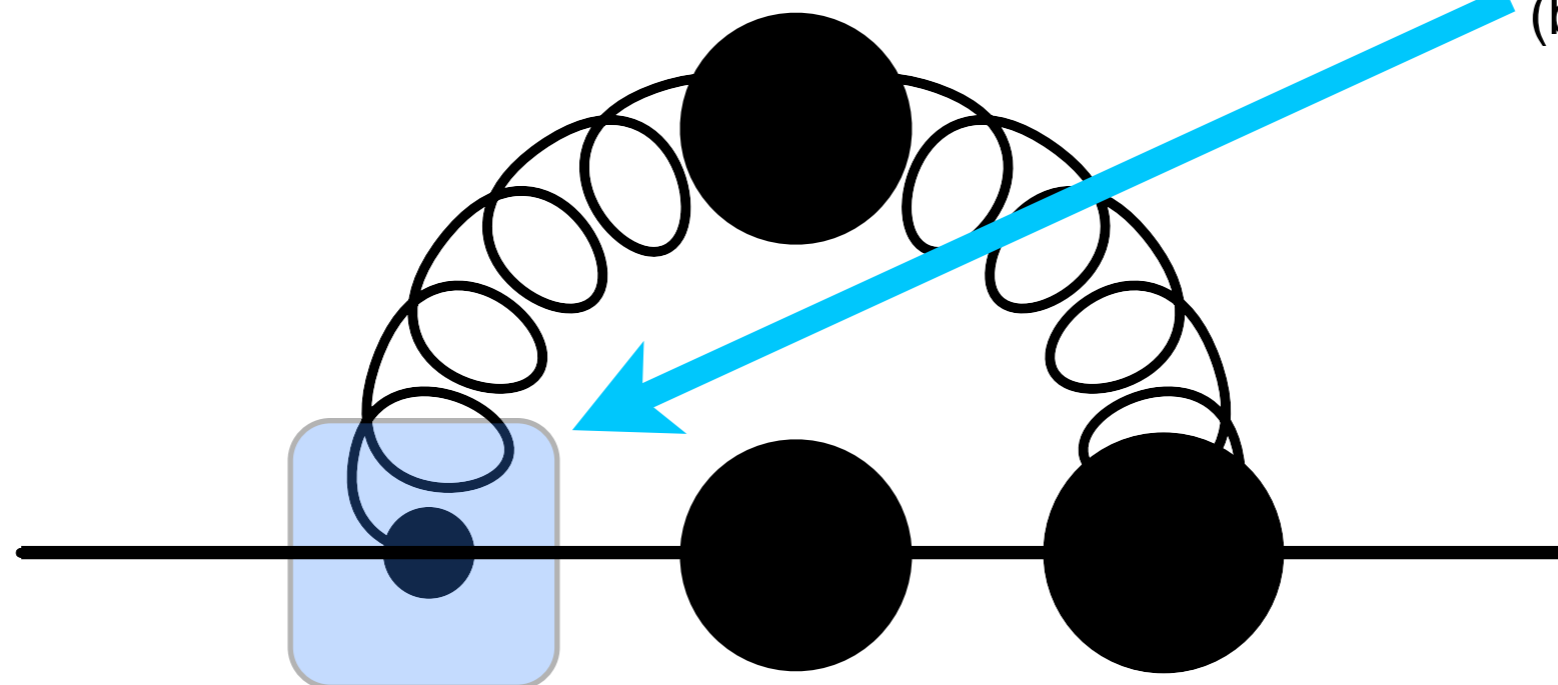
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● Example : The gap equation



Describe all possible ways of propagation of a quark

Can only split into a quark and a gluon (bare vertex)



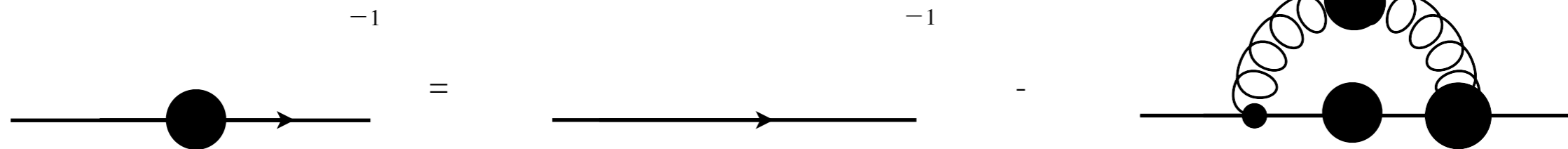
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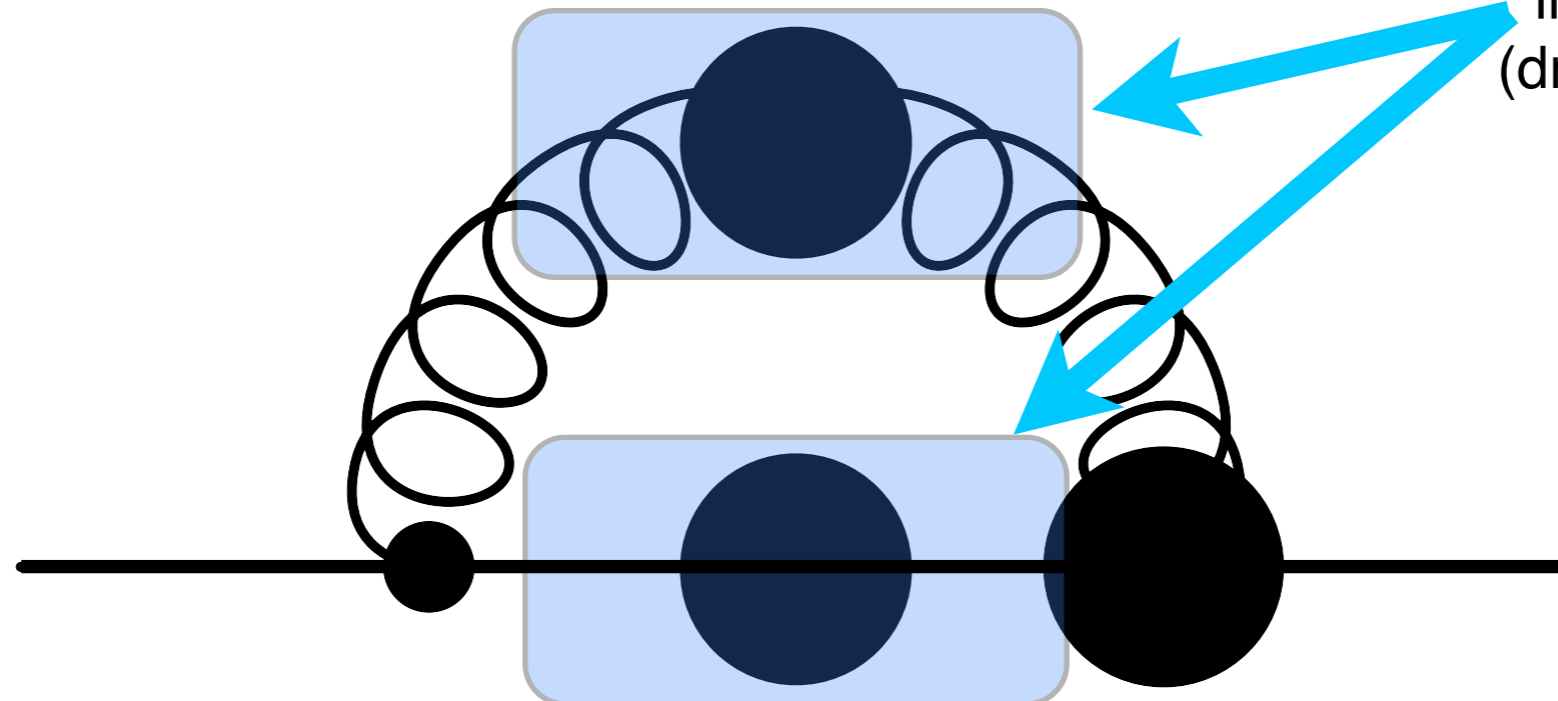
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● Example : The gap equation



Describe all possible ways of propagation of a quark

The quark and gluon propagate in all possible ways (dressed propagators)

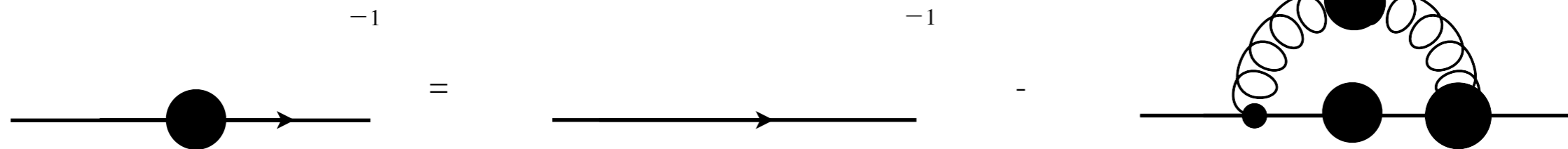


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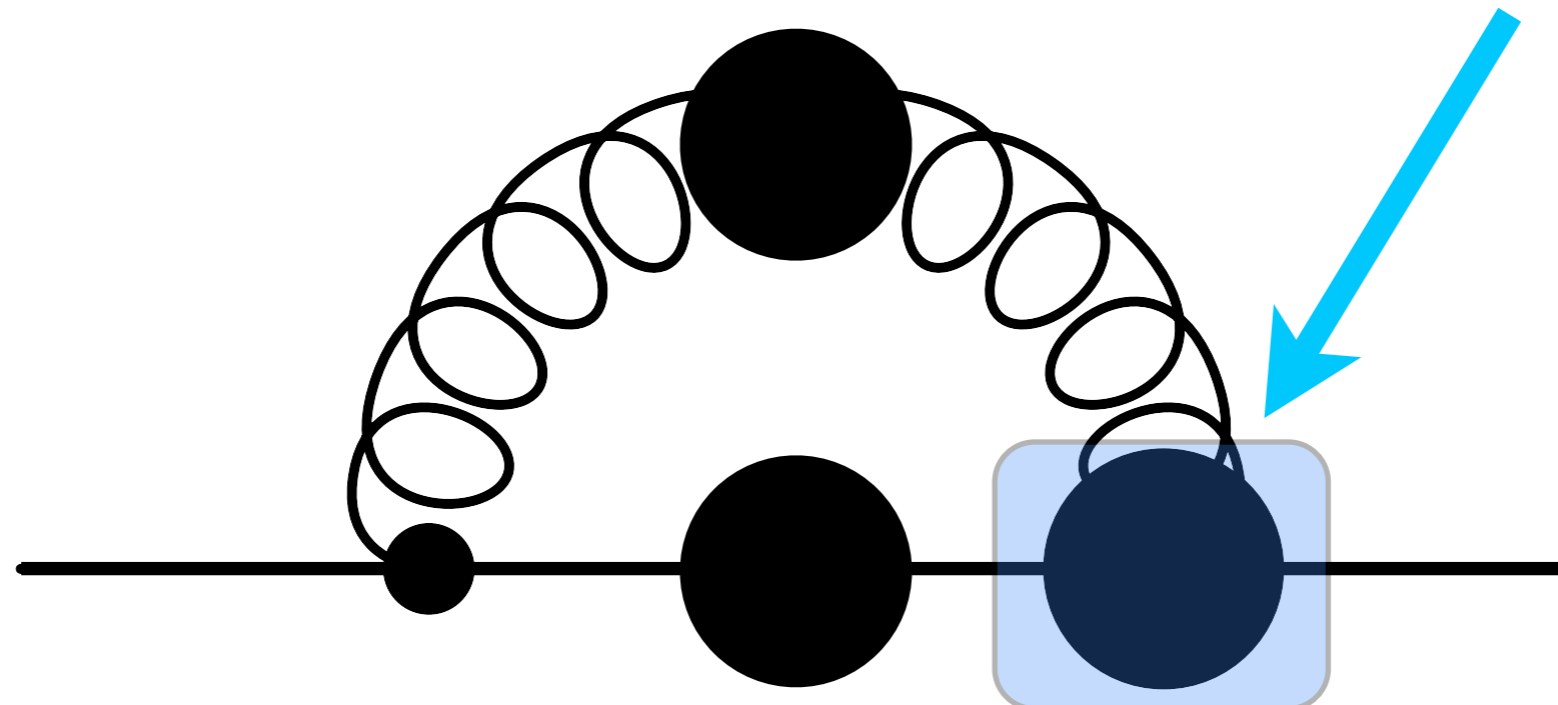
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● Example : The gap equation



Describe all possible ways of propagation of a quark

And finally recombine in all possible ways (dressed vertex)

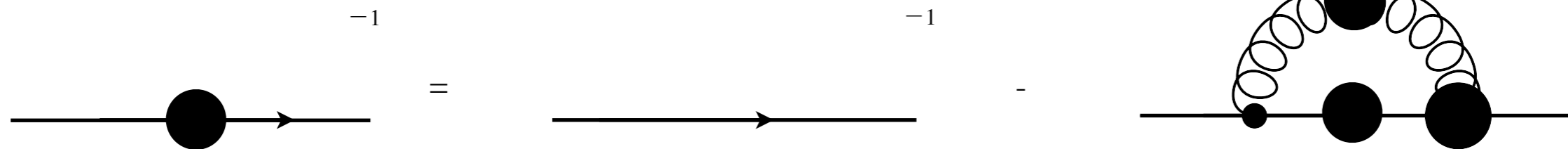


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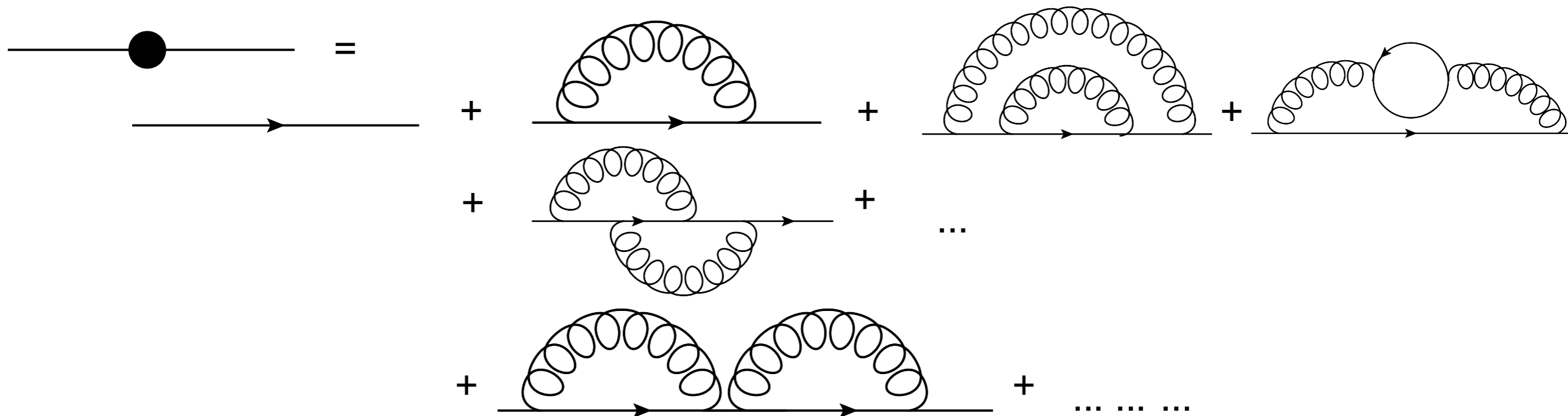
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● Example : The gap equation



➔ Describe all possible ways of propagation of a quark

● Contains perturbation theory :



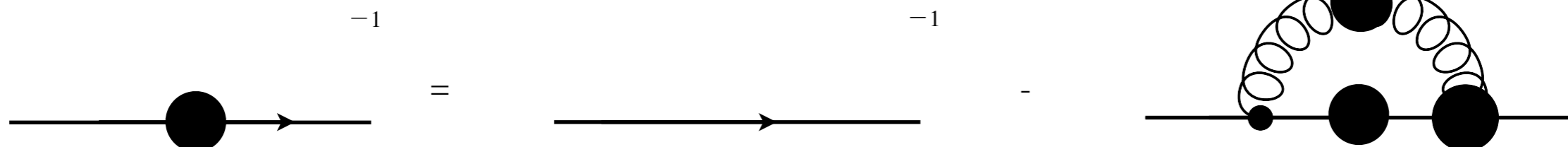
2 Setup

Dyson-Schwinger Equation

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● Example : The gap equation



Describe all possible ways of propagation of a quark



Contains perturbation theory :



Contains non-perturbative information

— Confinement and dynamical chiral symmetry breaking

— Bound states studies

— ...



Multi-scale problems feasible



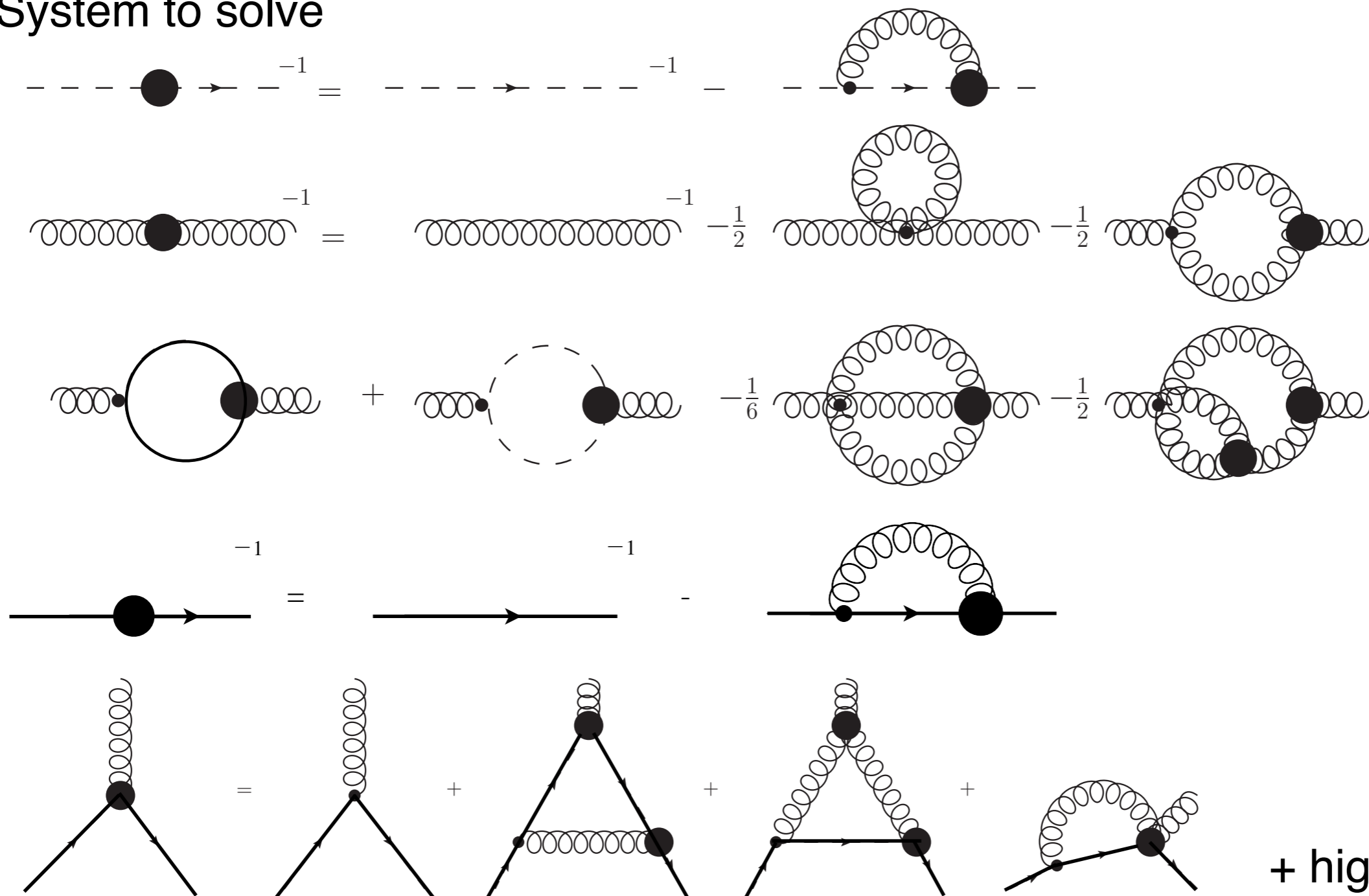
No sign problem

2 Setup Dyson-Schwinger Equation

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System to solve



2 Setup

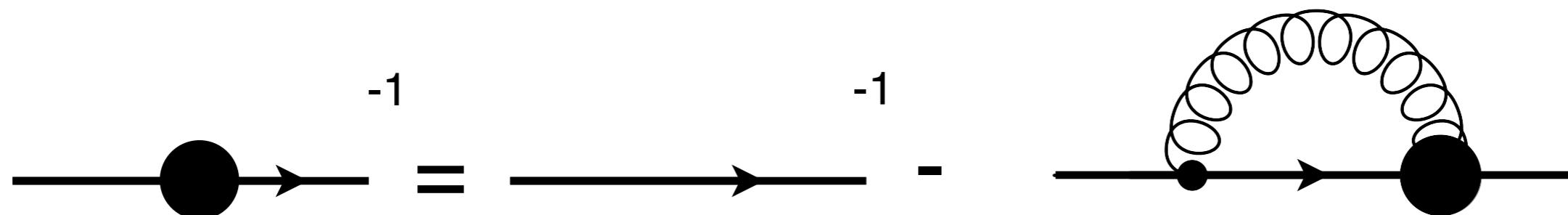
The truncation and modeling

- System to solve

- Truncations are mandatory

→ We want a realistic temperature dependence of the gluon

$$S^{-1}(\vec{p}, \omega_n) = A(\vec{p}, \omega_n) \vec{\gamma} \vec{p} + C(\vec{p}, \omega_n) \omega_n \gamma_4 + B(\vec{p}, \omega_n) + \omega_n \gamma_4 \vec{p} \vec{\gamma} D(\vec{p}, \omega_n)$$



2 Setup

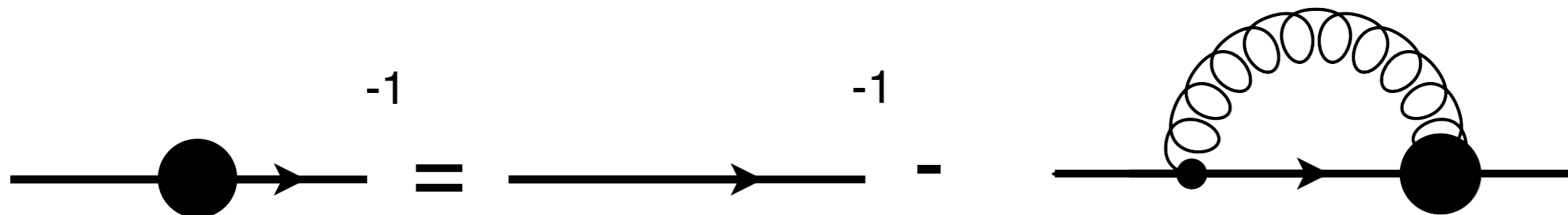
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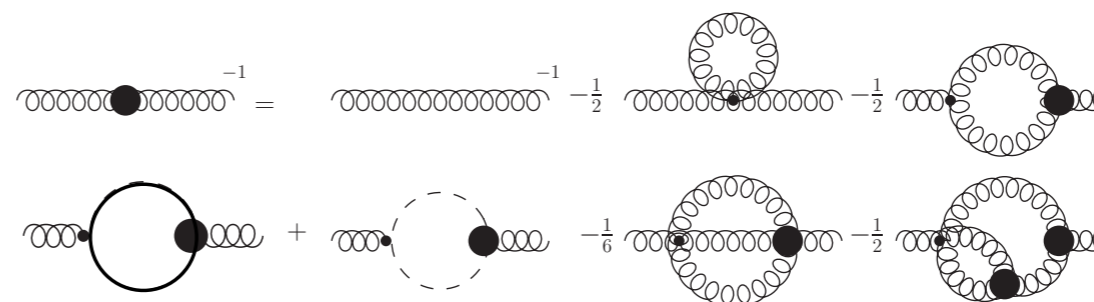
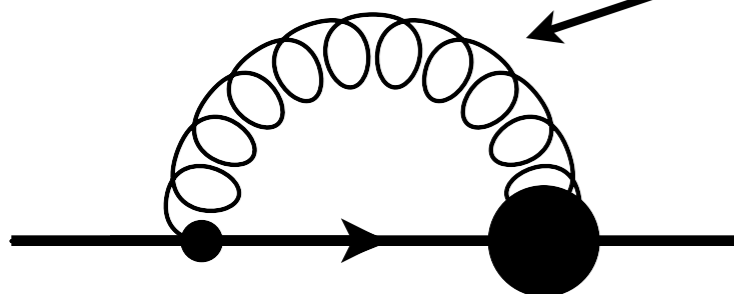
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$$D_{\mu\nu}(p) = \frac{1}{p^2} (Z_T(p) P_{\mu\nu}^T + Z_L(p) P_{\mu\nu}^L)$$



➡ Spuriously divergent terms

➡ Accessible on lattice

2 Setup

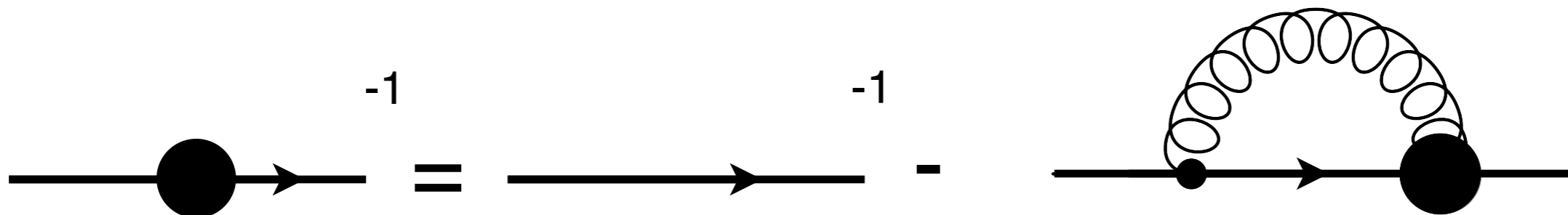
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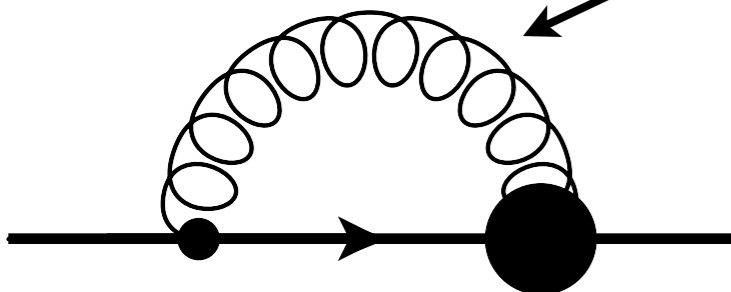


$$Z_{T,L}(x) = \frac{x}{(x+1)^2} \left(\left(\frac{c}{x + a_{T,L}(T)} \right)^{b_{T,L}(T)} + x \left(\frac{\beta_0 \alpha(\mu)}{4\pi} \ln(x+1) \right)^\gamma \right)$$

Coefficients are fitted to reproduce lattice data

[A. Maas, J.M Pawłowski, L. von Smekal, D. Spielmann (2012)]

[C.S. Fischer, A. Maas, J.A. Müller (2010)]



2 Setup

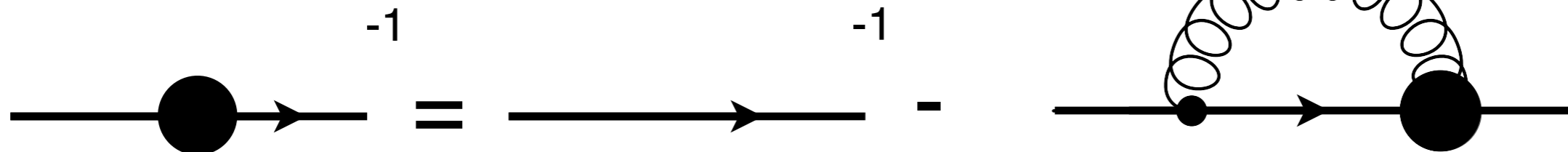
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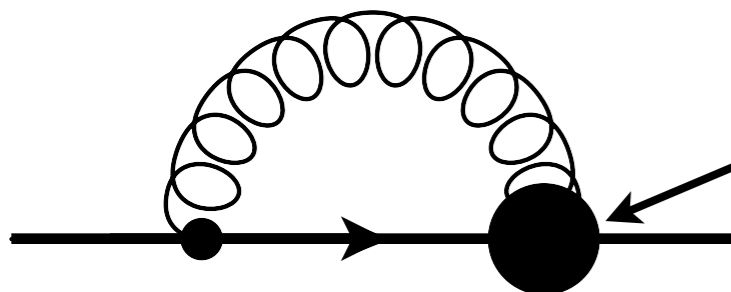


$$\Gamma_{q-gl}(p, q, l)$$

24 tensors parts

Difficult to obtain from lattice

Lack of information of the temperature dependence of this quantity from continuum studies



2 Setup

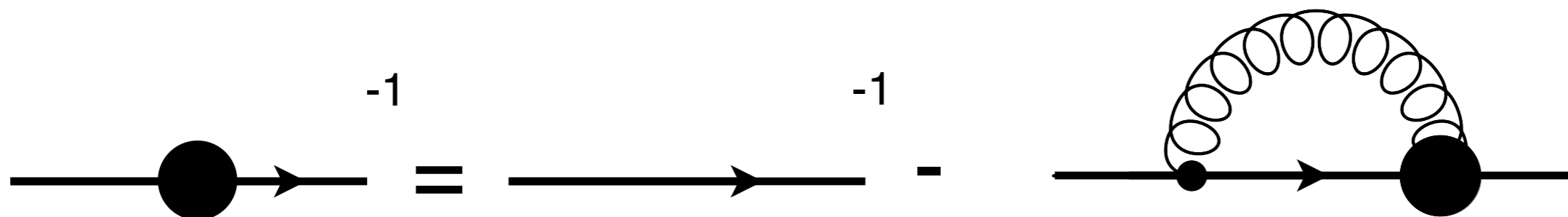
The truncation and modeling

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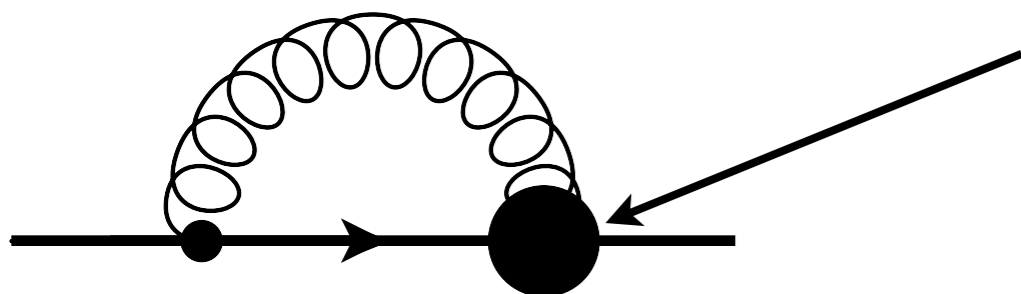
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$$\Gamma_{q-gl}(p, q, l) = \left(\frac{A(p)+A(q)}{2} \vec{\gamma}, \frac{C(p)+C(q)}{2} \gamma_4 \right) W(p, q, l)$$

$$W(p, q, l) = \frac{d_1}{d_2+l^2} + \frac{l^2}{1+l^2} \left(\frac{\beta_0 \alpha(\mu)}{4\pi} \ln(l^2+1) \right)^{2\delta}$$

[C.S. Fischer (2009)]



2 Setup

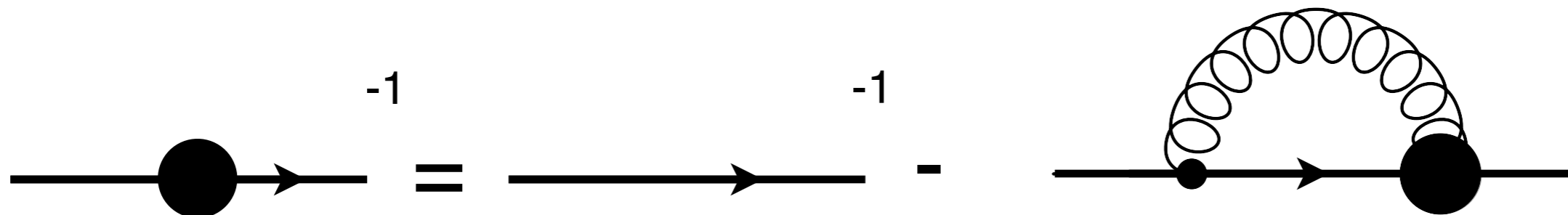
The truncation and modeling

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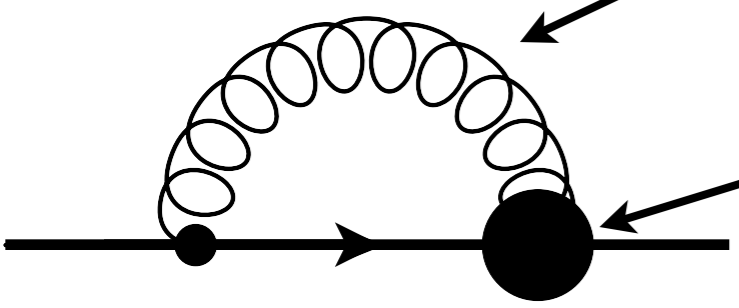
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➔ The system can be solved

2 Setup

Chiral condensate

● Chiral Symmetry Breaking

$$S^{-1}(\vec{p}, \omega_n) = A(\vec{p}, \omega_n) \vec{\gamma} \vec{p} + C(\vec{p}, \omega_n) \omega_n \gamma_4 + B(\vec{p}, \omega_n) + \omega_n \gamma_4 \vec{p} \vec{\gamma} D(\vec{p}, \omega_n)$$

$$\Delta_\pi(T) = Z_2(Z_m)N_c T \sum_{\omega_n} \int_{\vec{p}} \frac{d^3\vec{p}}{(2\pi)^3} \text{Tr}[S(\vec{p}, \omega_n)]$$

● chiral limit $m_{bare} = 0$

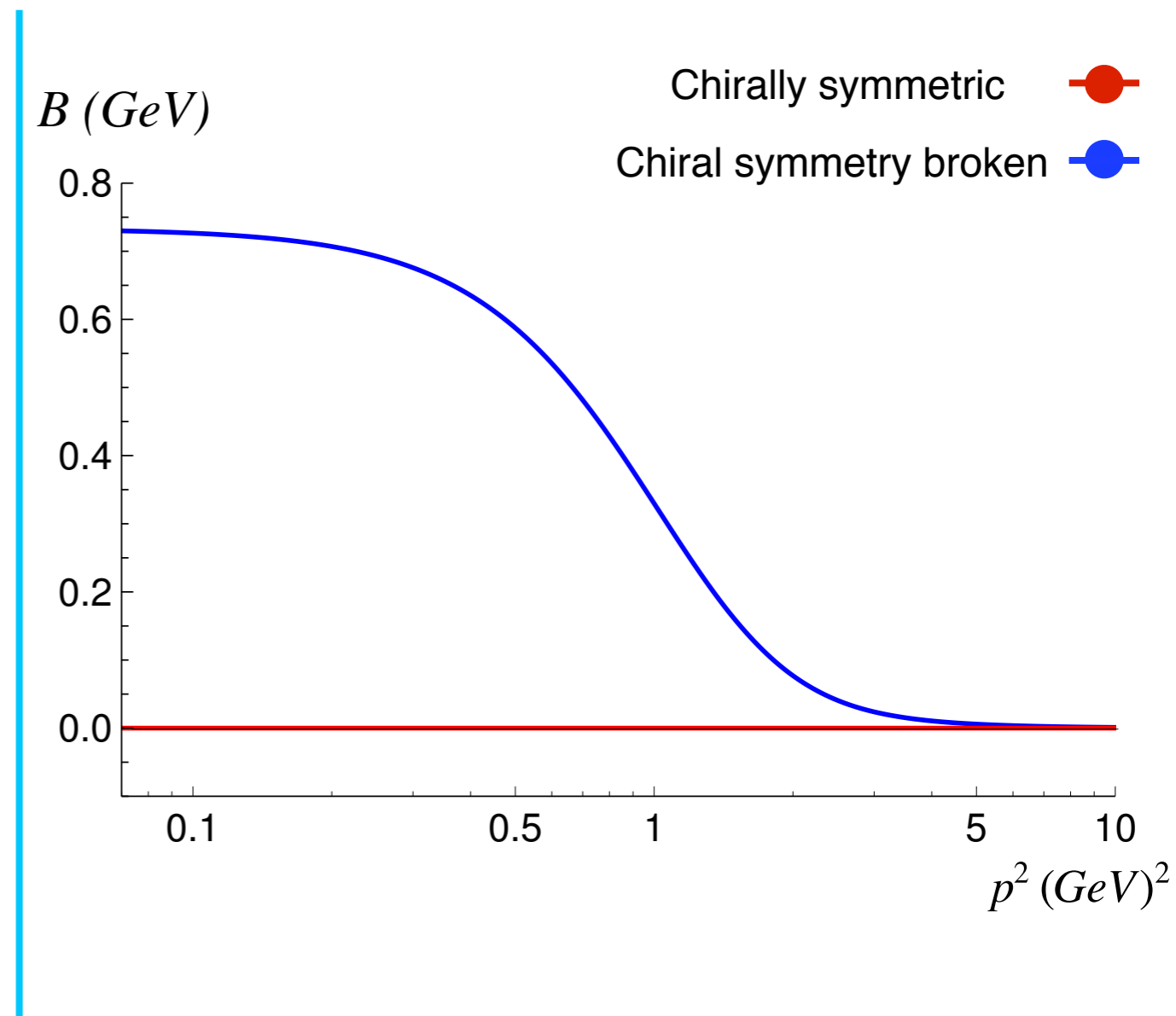
→ $B \neq 0$, formation of a chiral condensate

Chiral symmetry broken

→ $B = 0$, no chiral condensate

Chirally symmetric

order parameter



2 Setup

(Pseudo)-order parameter

- Chiral Symmetry Breaking

$$S^{-1}(\vec{p}, \omega_n) = A(\vec{p}, \omega_n) \vec{\gamma} \vec{p} + C(\vec{p}, \omega_n) \omega_n \gamma_4 + B(\vec{p}, \omega_n) + \omega_n \gamma_4 \vec{p} \vec{\gamma} D(\vec{p}, \omega_n)$$

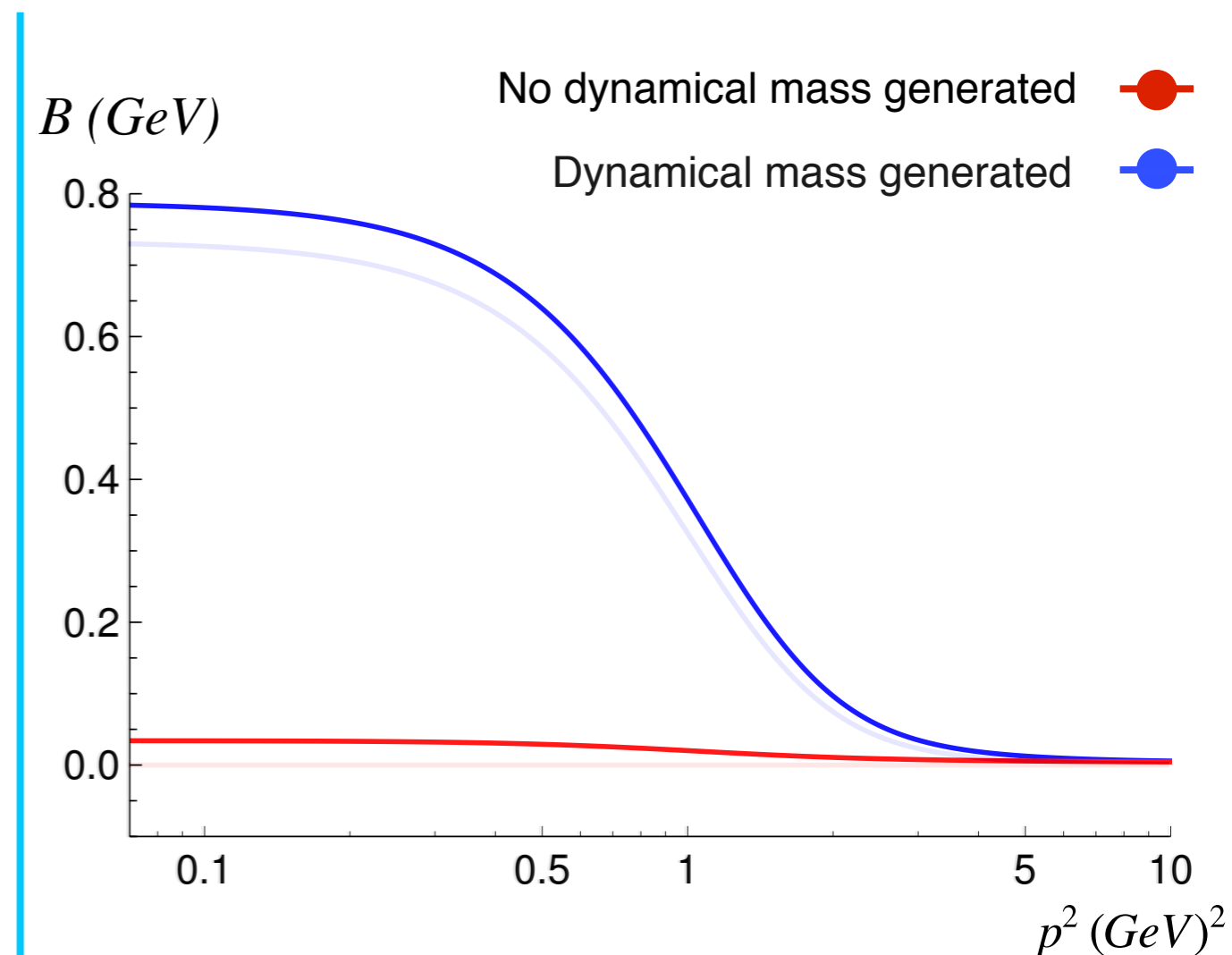
$$\Delta_\pi(T) = Z_2(Z_m)N_c T \sum_{\omega_n} \int_{\vec{p}} \frac{d^3\vec{p}}{(2\pi)^3} \text{Tr}[S(\vec{p}, \omega_n)]$$

- $m_{bare} > 0$

→ $B \neq 0$, formation of a chiral condensate

Chiral symmetry broken

Pseudo-order parameter



2 Setup


D function


14/40

● Chiral Symmetry Breaking

$$S^{-1}(\vec{p}, \omega_n) = A(\vec{p}, \omega_n) \vec{\gamma} \vec{p} + C(\vec{p}, \omega_n) \omega_n \gamma_4 + B(\vec{p}, \omega_n) + \omega_n \gamma_4 \vec{p} \vec{\gamma} D(\vec{p}, \omega_n)$$

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 $[\vec{p} \vec{\gamma} \omega_n \gamma_4, \gamma_5] = 0 \quad D \neq 0$
Chiral symmetry broken


 $D = 0 \text{ at } T = 0$


 D power-law suppressed in UV


 $D = 0$ in Rainbow ladder


 D small after the chiral restoration

We expect a small contribution of D

- Quark confinement

$$S^{-1}(\vec{p}, \omega_n) = A(\vec{p}, \omega_n) \vec{\gamma} \vec{p} + C(\vec{p}, \omega_n) \omega_n \gamma_4 + B(\vec{p}, \omega_n) + \omega_n \gamma_4 \vec{p} \vec{\gamma} D(\vec{p}, \omega_n)$$

$$\Delta_\phi(T) = Z_2(Z_m) N_c T \sum_{\omega_n(\phi)} \int \frac{d^3\vec{p}}{(2\pi)^3} \text{Tr}[S(\vec{p}, \omega_n(\phi))]$$

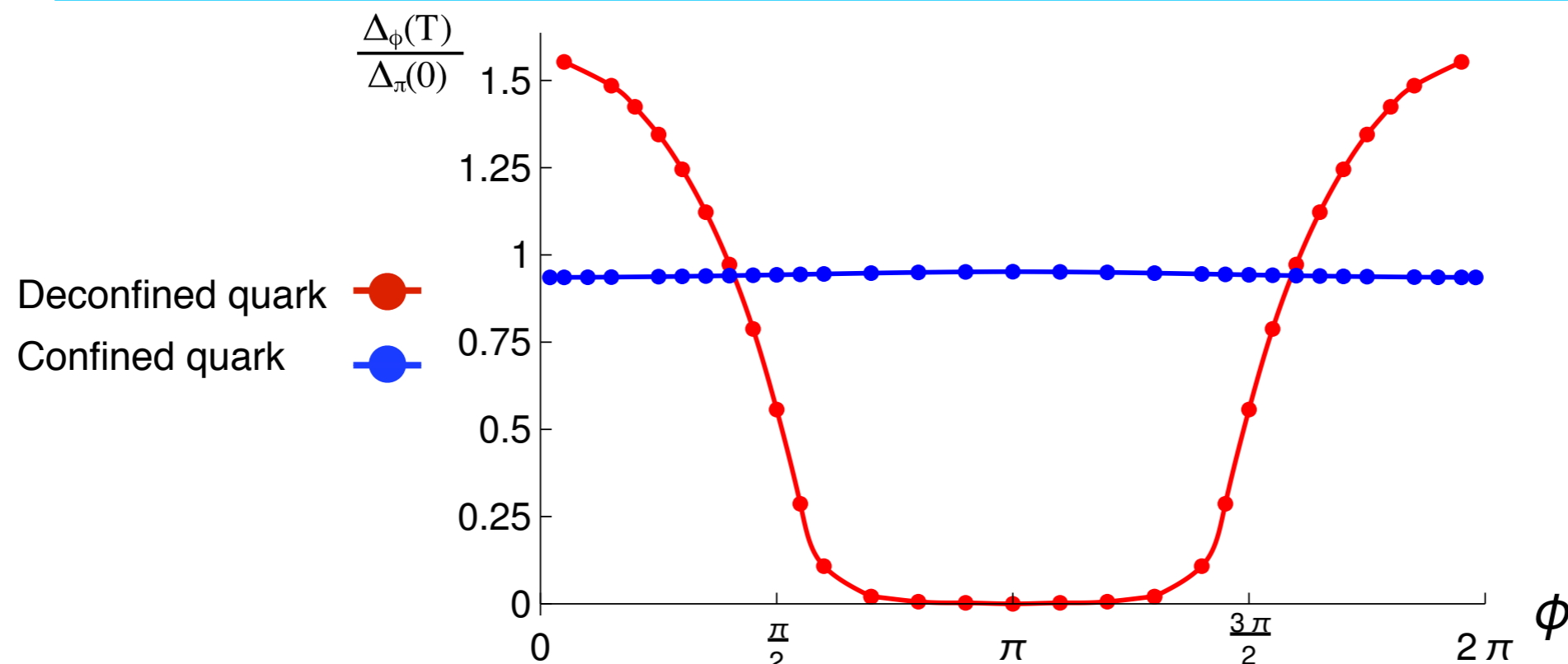
We introduce a phase dependence : $\omega_n = \pi T \left(2n + \frac{\phi}{\pi} \right)$

$$\Sigma_1 = \int_0^{2\pi} e^{i\phi} d\phi \Delta_\phi(T)$$

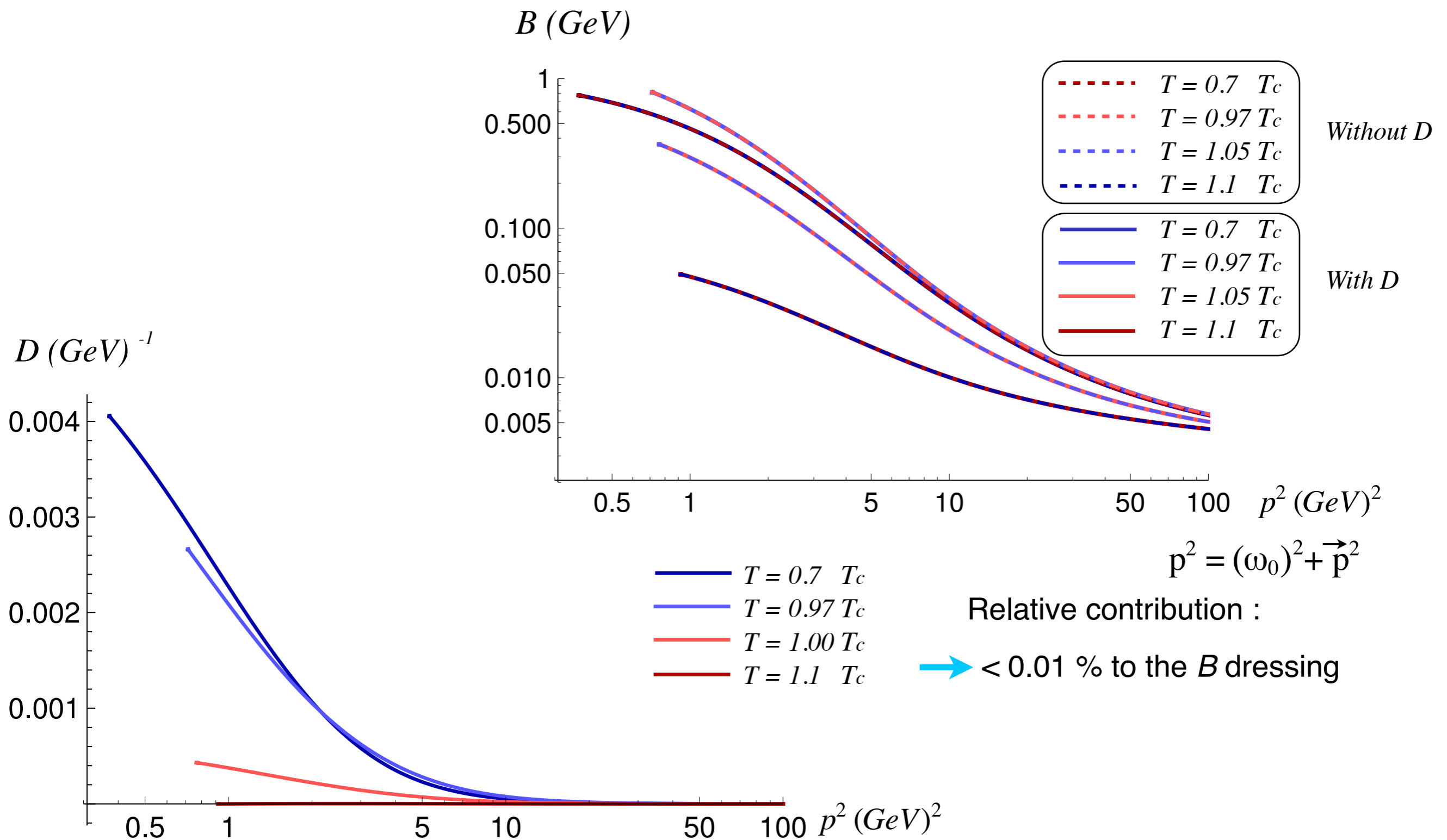
The dual quark condensate is proportional to the Polyakov Loop

[E. Bilgici, F. Bruckmann, C. Gattringer, and C. Hagen (2008)]

[C.S. Fischer (2009)]



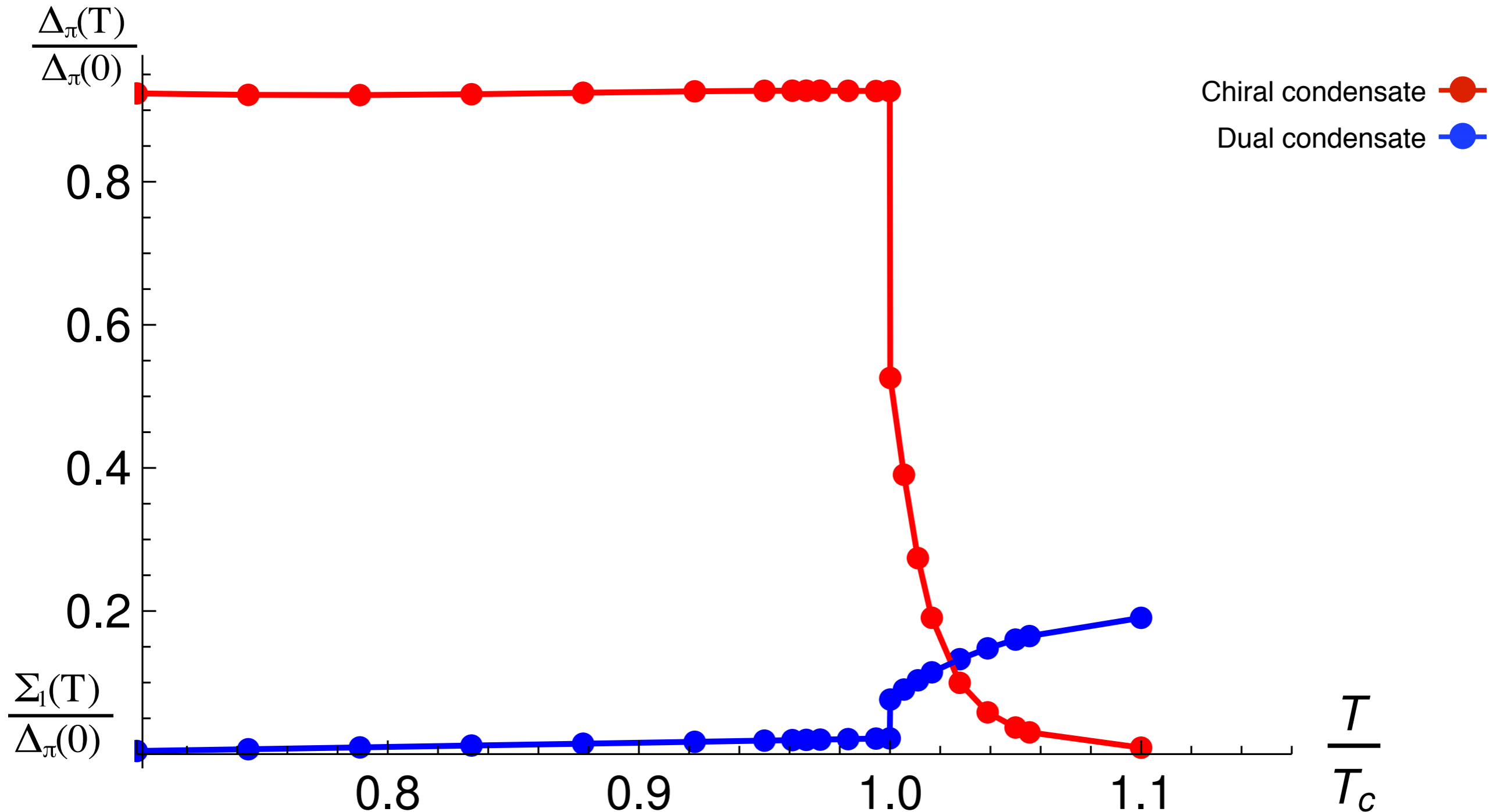
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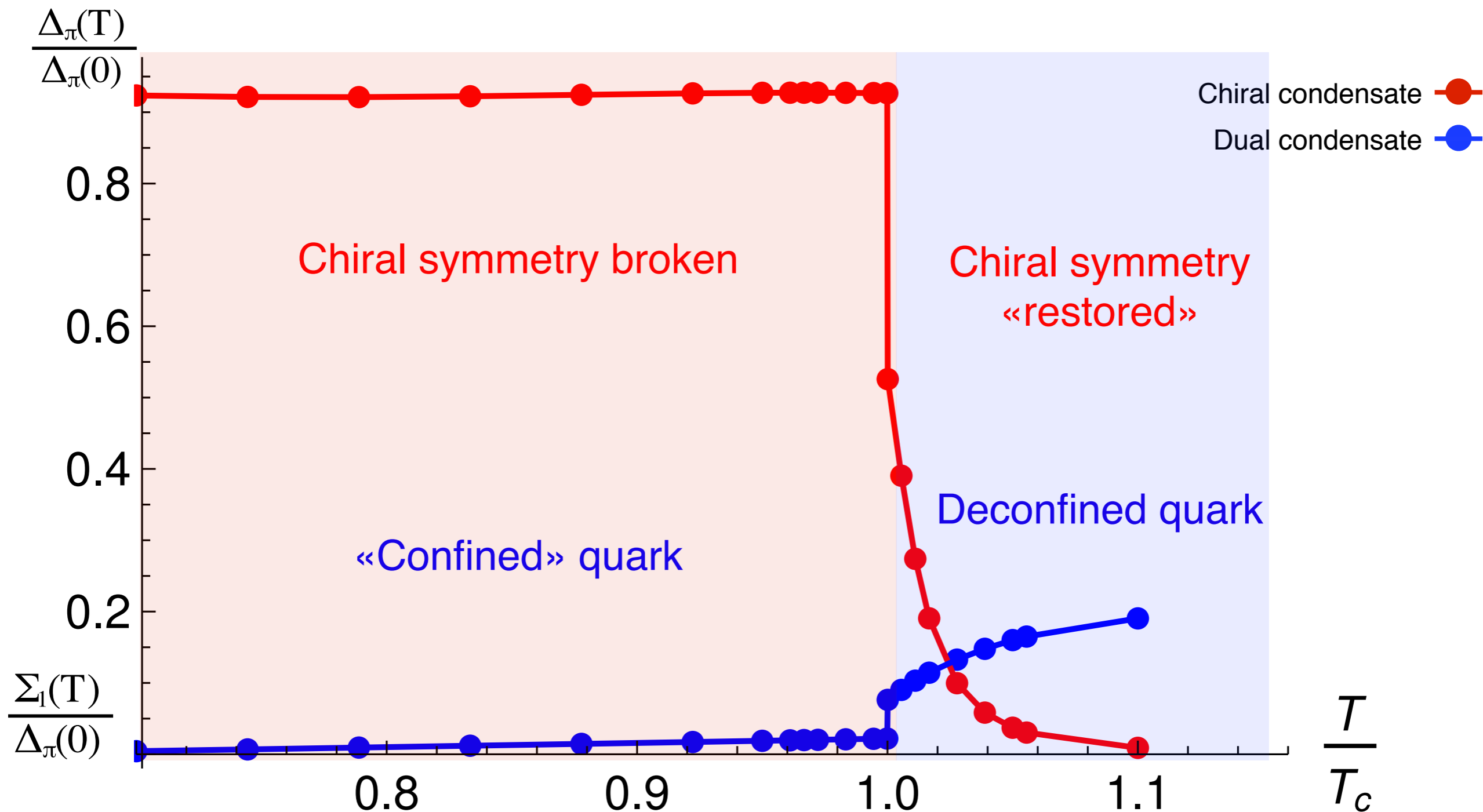
3 Quenched QCD

Order parameters

Chiral Condensate and dual condensate



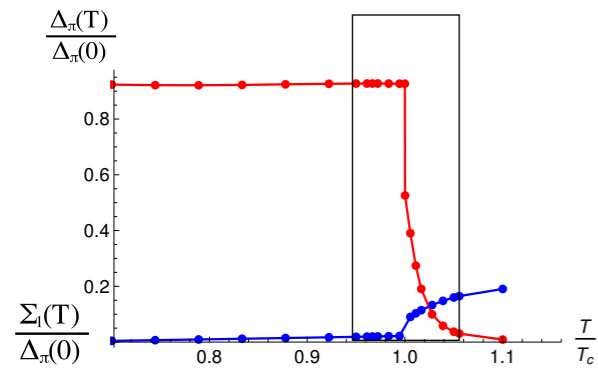
Chiral Condensate and dual condensate



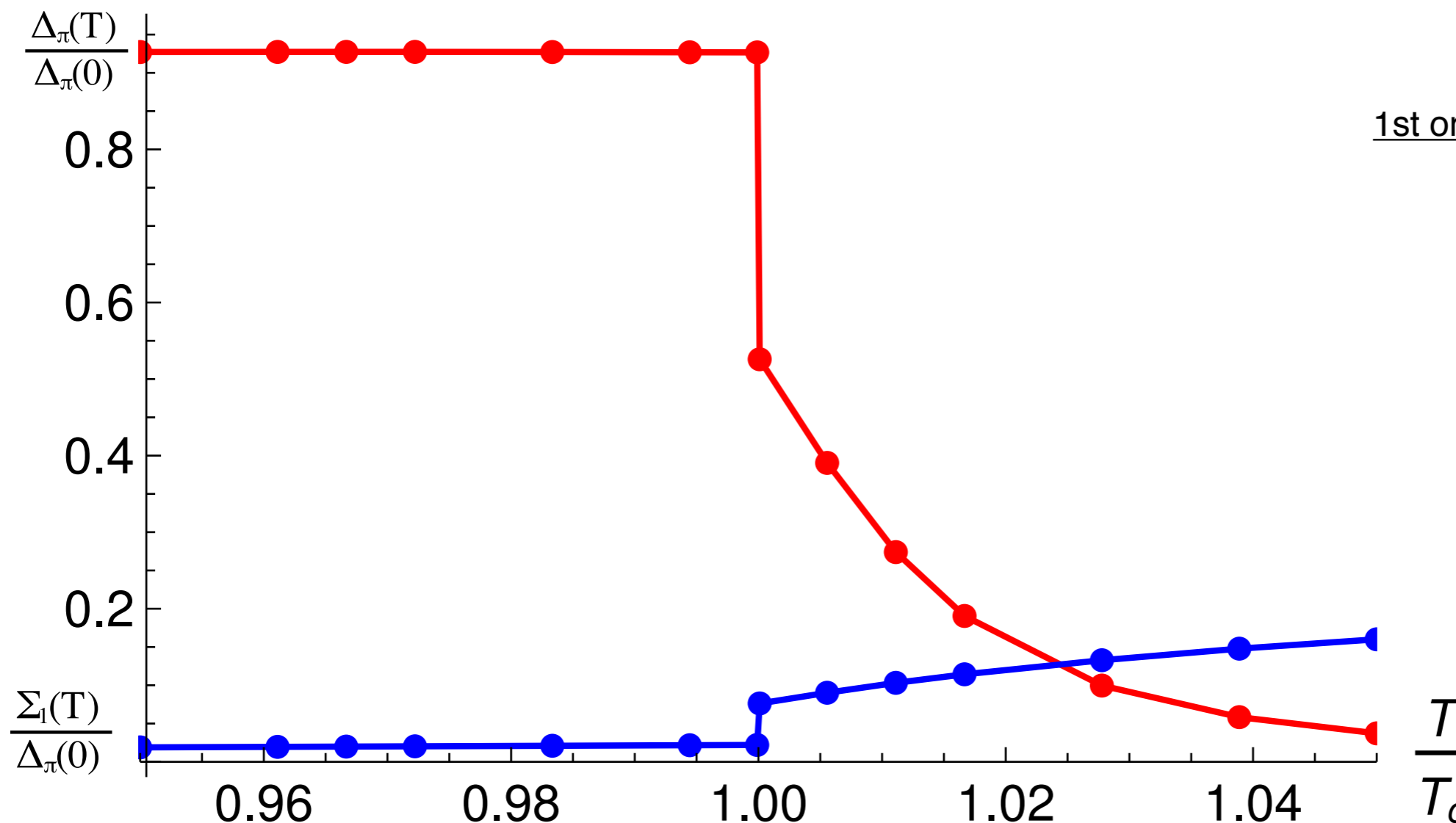
3 Quenched QCD

Order parameters

Chiral Condensate and Dual condensate
Type of transition

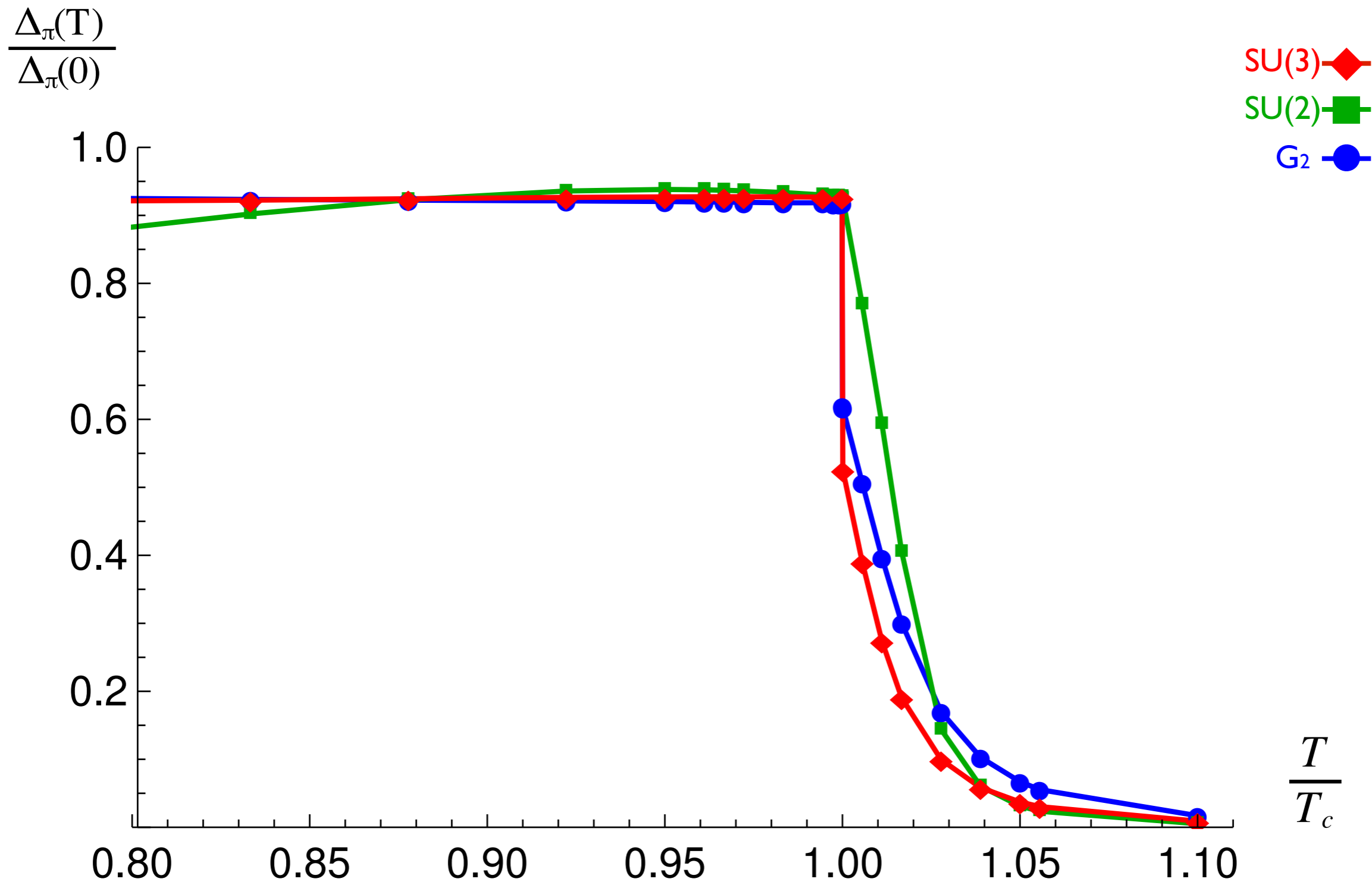


Chiral condensate ●
Dual condensate ●

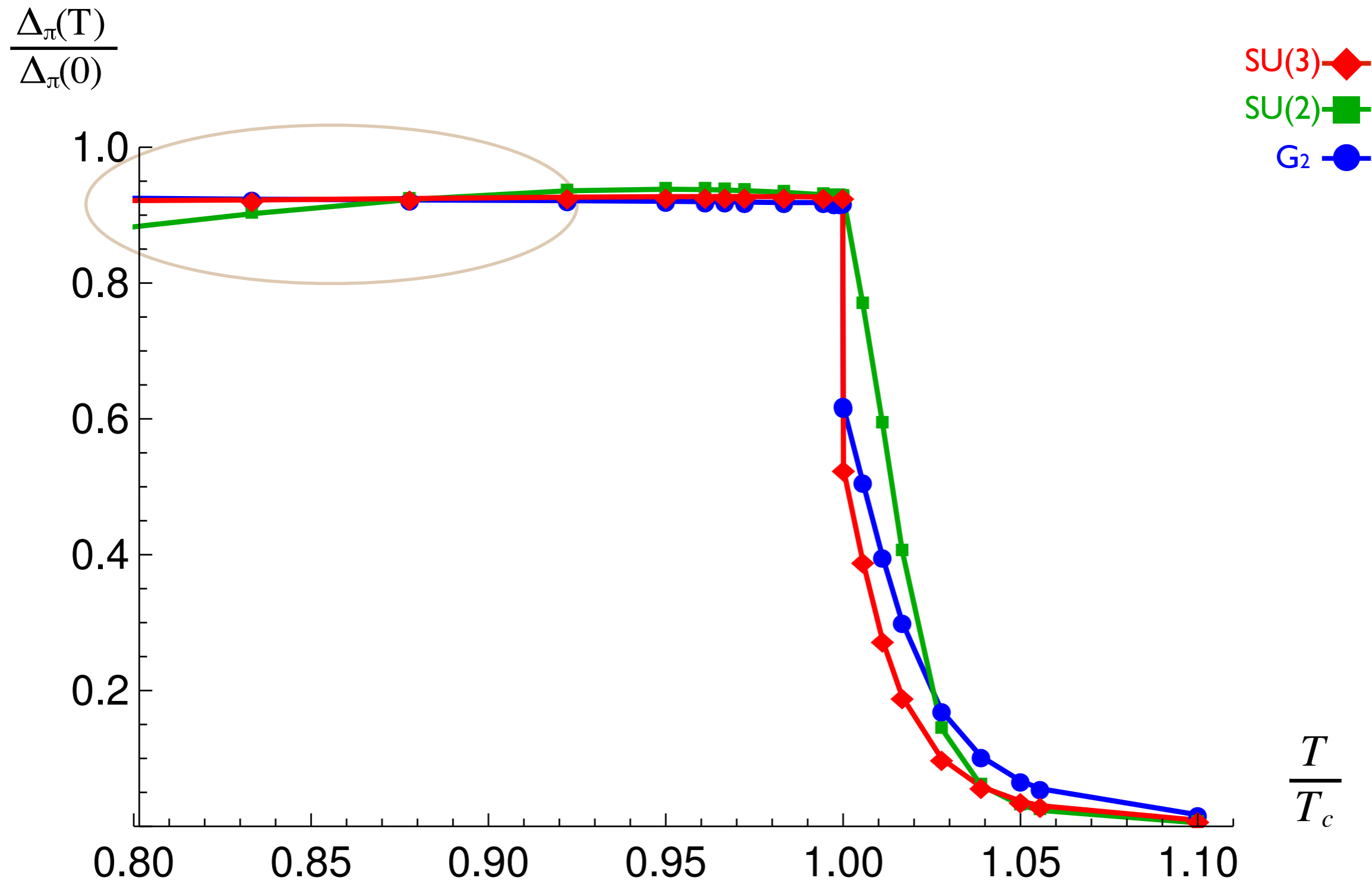


1st order transition

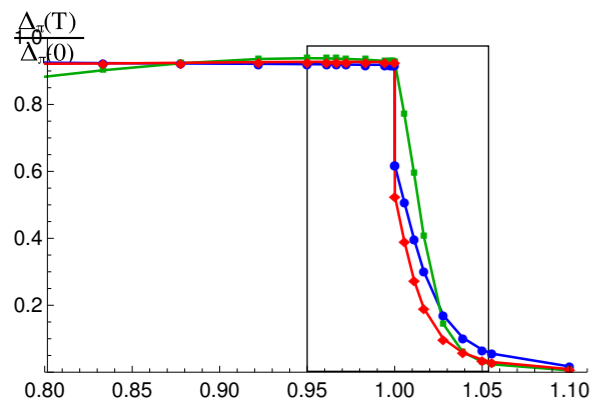
Chiral condensate



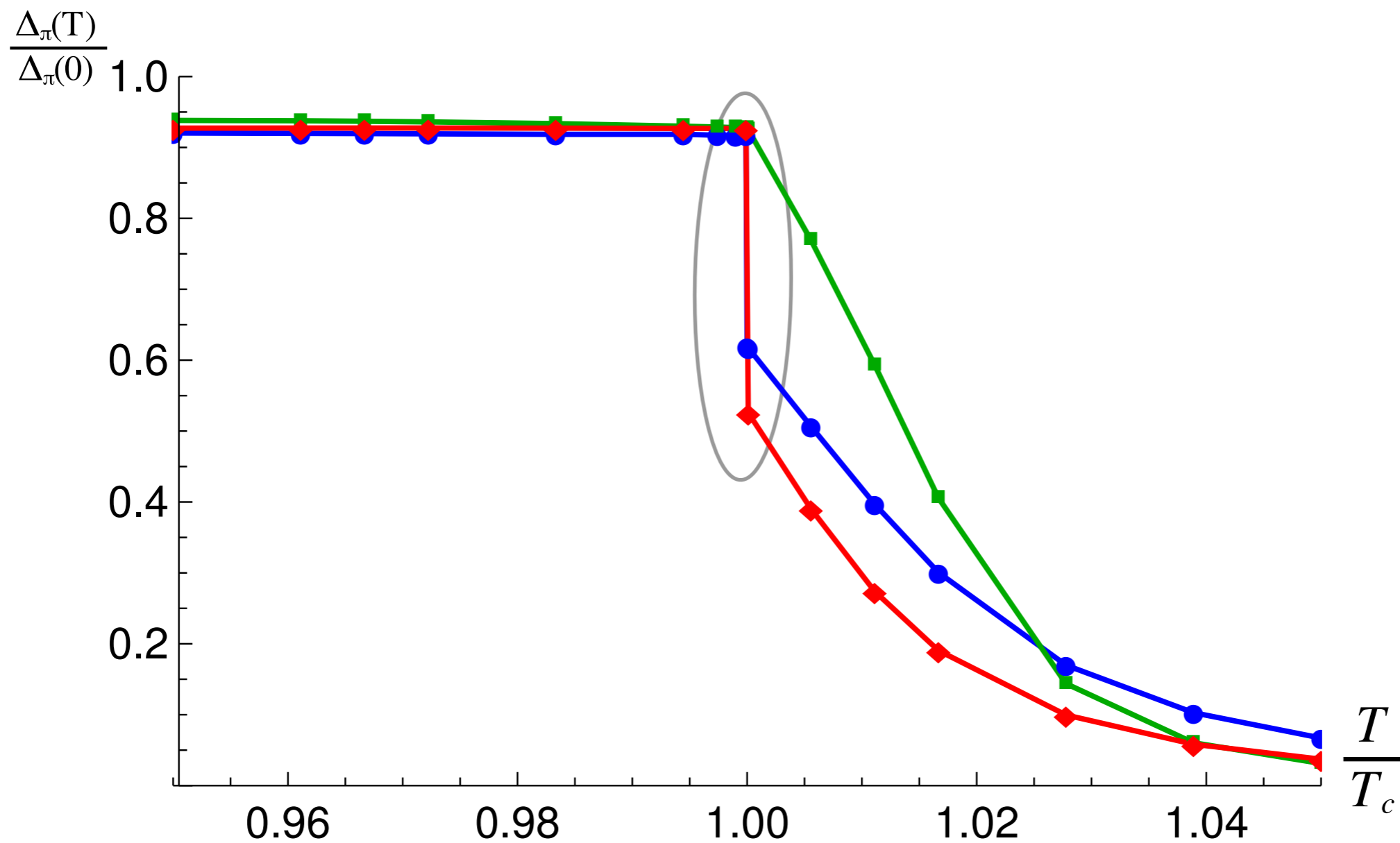
Chiral condensate



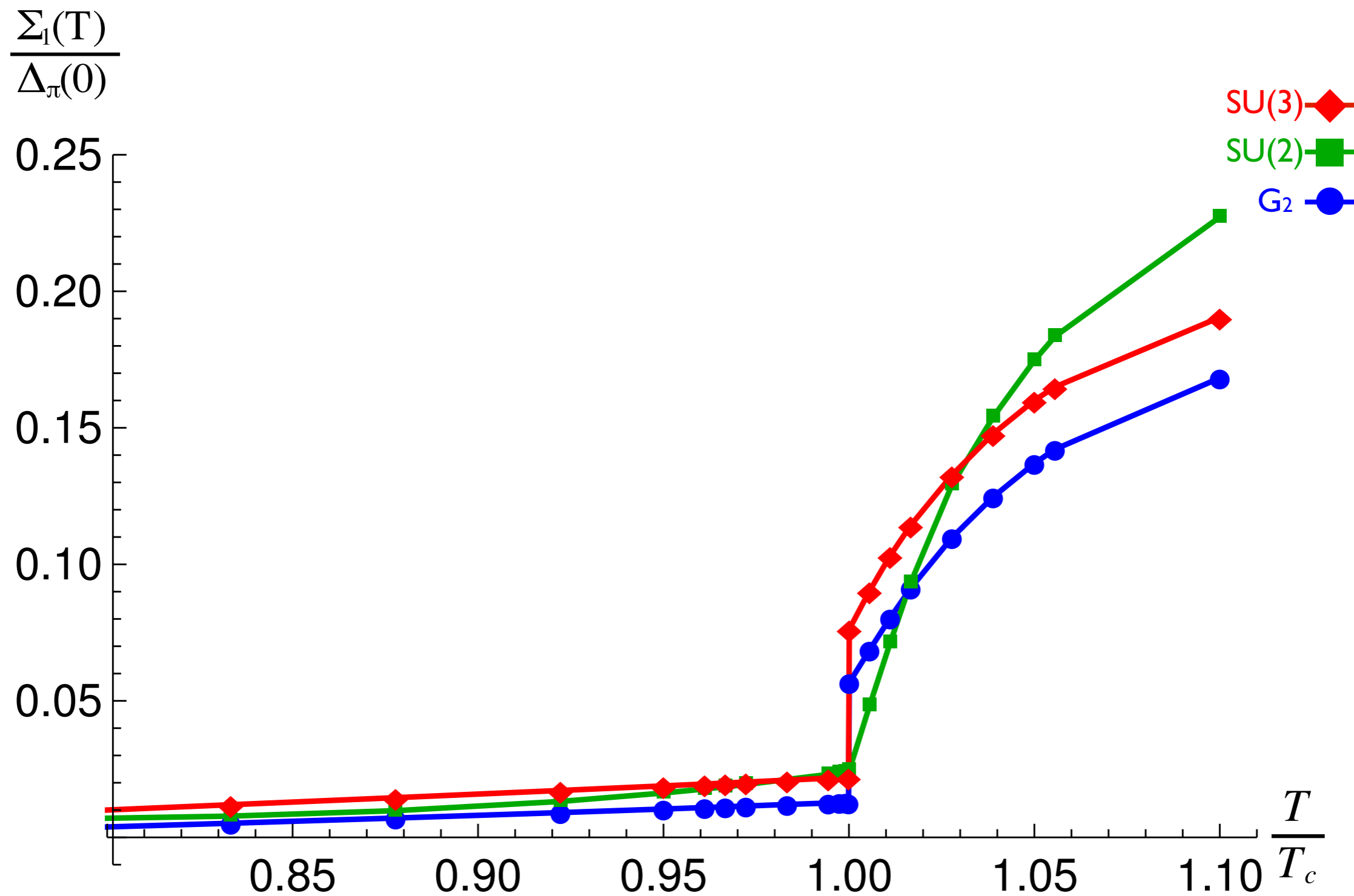
Chiral condensate

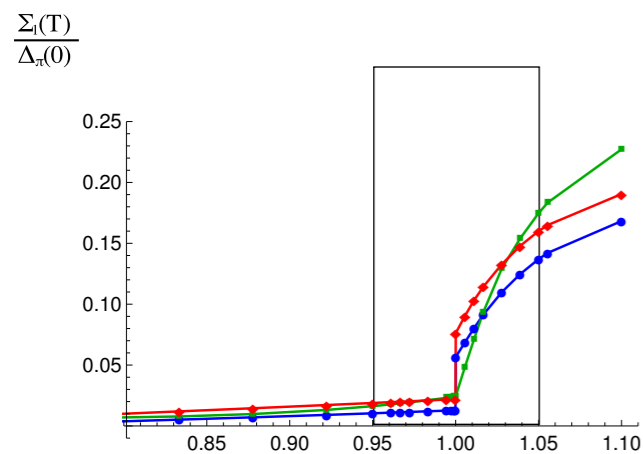


- 1st order transition SU(3) ◆
- 2nd order transition SU(2) ■
- 1st order transition G₂ ●



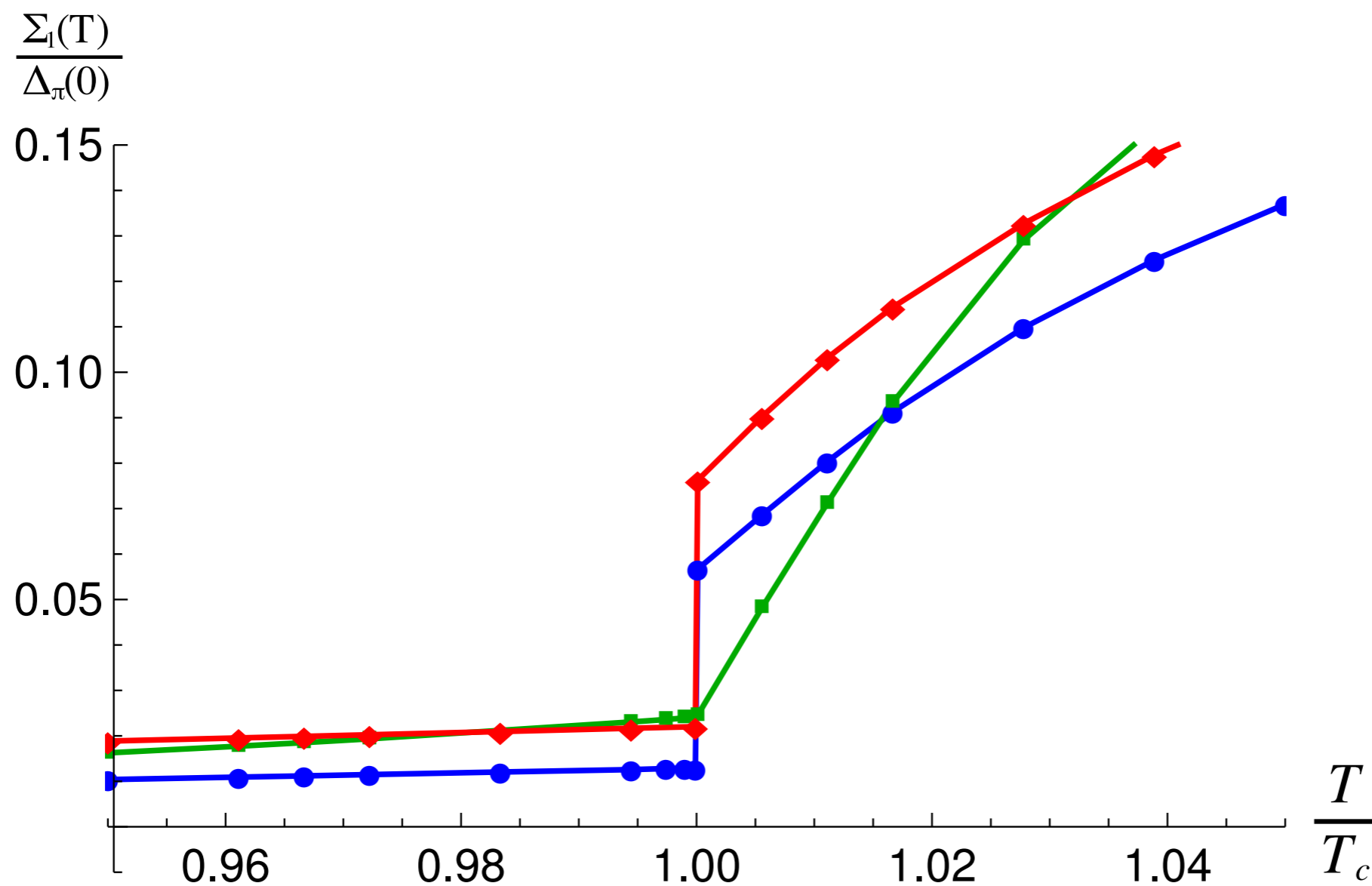
Dual condensate





Dual condensate

1st order transition SU(3) ◆
2nd order transition SU(2) ■
1st order transition G₂ ●



4 Unquenching Quark loop

● System to solve :

$$- - - \bullet \rightarrow -^{-1} = - - - \rightarrow -^{-1} - - - \overset{\curvearrowright}{\bullet \rightarrow \bullet}$$

$$\text{Wavy line} \bullet \text{Wavy line}^{-1} = \text{Wavy line}^{-1} - \frac{1}{2} \text{Wavy line} \text{Loop} \text{Wavy line}^{-1} - \frac{1}{2} \text{Wavy line} \text{Loop} \text{Wavy line}$$

$$\boxed{\text{Wavy line} \text{Loop} \text{Wavy line}} + \text{Wavy line} \text{Loop} \text{Wavy line}^{-1} - \frac{1}{6} \text{Wavy line} \text{Loop} \text{Loop} \text{Wavy line}^{-1} - \frac{1}{2} \text{Wavy line} \text{Loop} \text{Loop} \text{Wavy line} + \text{higher equations ...}$$

● Approximation :

$$\text{Wavy line} \bullet \text{Wavy line}^{-1} = \text{Wavy line} \overset{\bullet}{\text{Wavy line}} \text{Wavy line}^{-1} + N_f \text{Wavy line} \text{Loop} \text{Wavy line}$$

Quenched Input

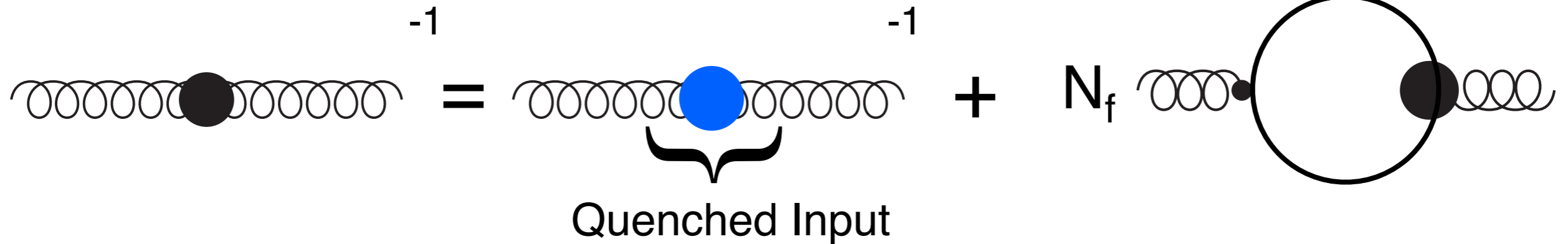
[C.S Fischer , J. Luecker (2012)]

➔ Neglect all indirect quark contributions in the gluon dressing

➔ Remove spurious divergence with a generalized Brown-Pennington projector

4 Unquenching Quark loop

- Adding the quark loop

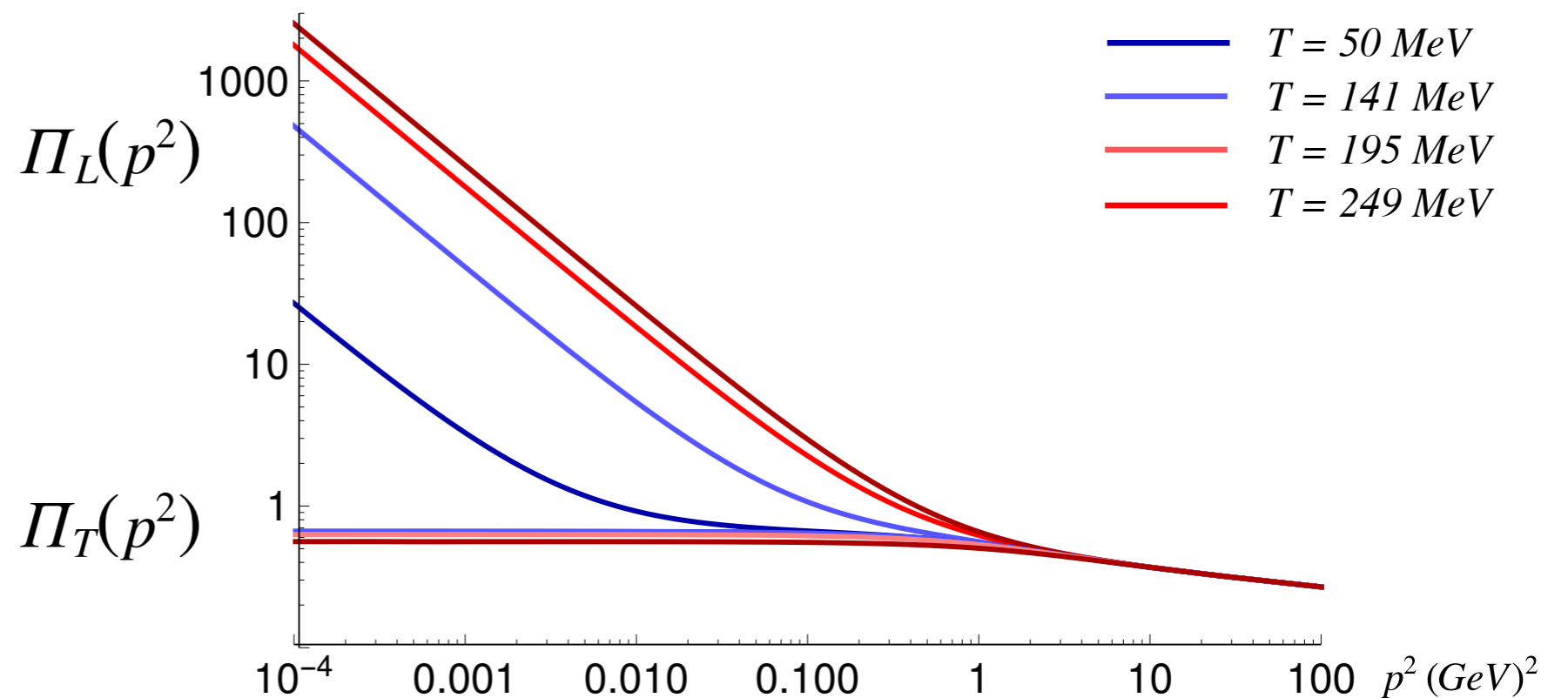


[C.S Fischer , J. Luecker (2012)]

$$\Pi_L(p)p^2 \xrightarrow{p \rightarrow 0} (m_{th})^2$$

Debye Screening
of the chromo-electric
charge

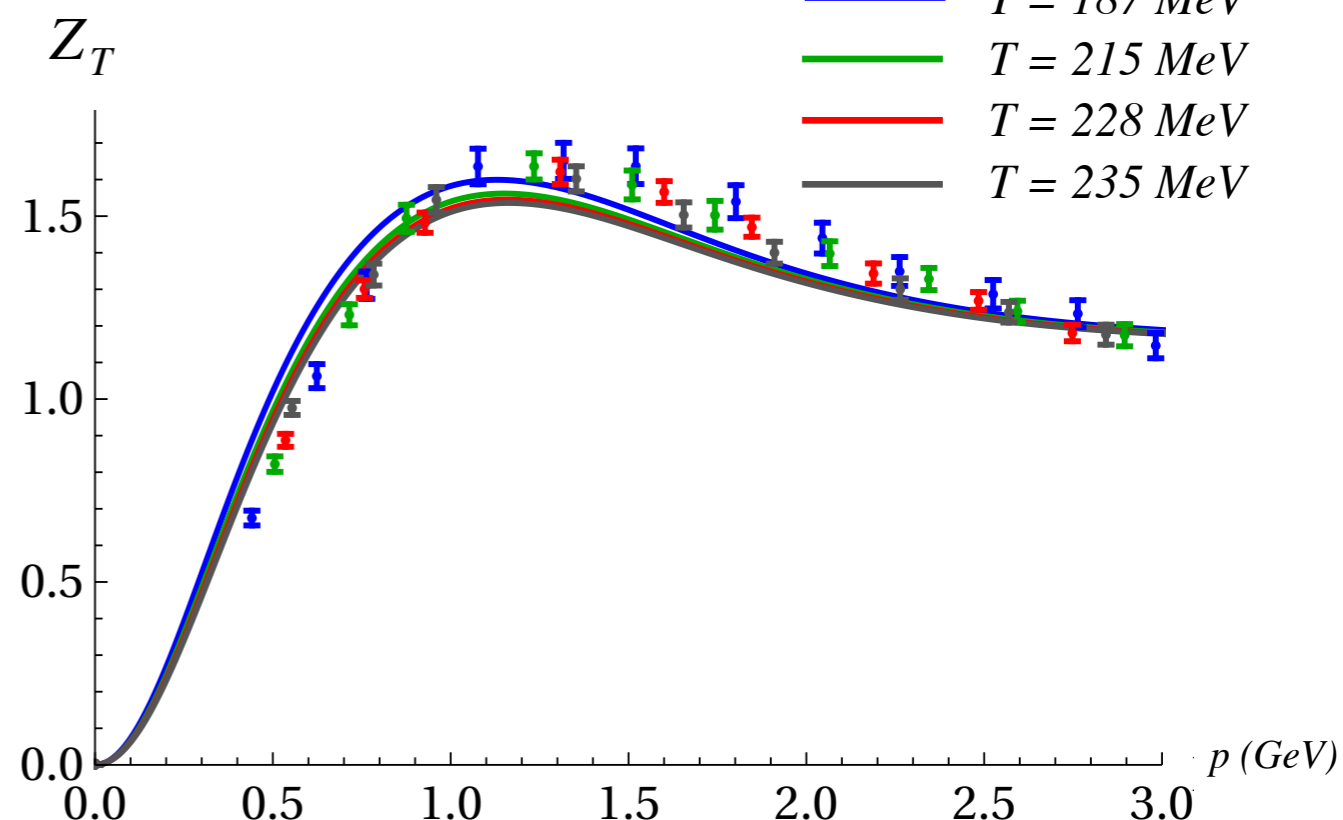
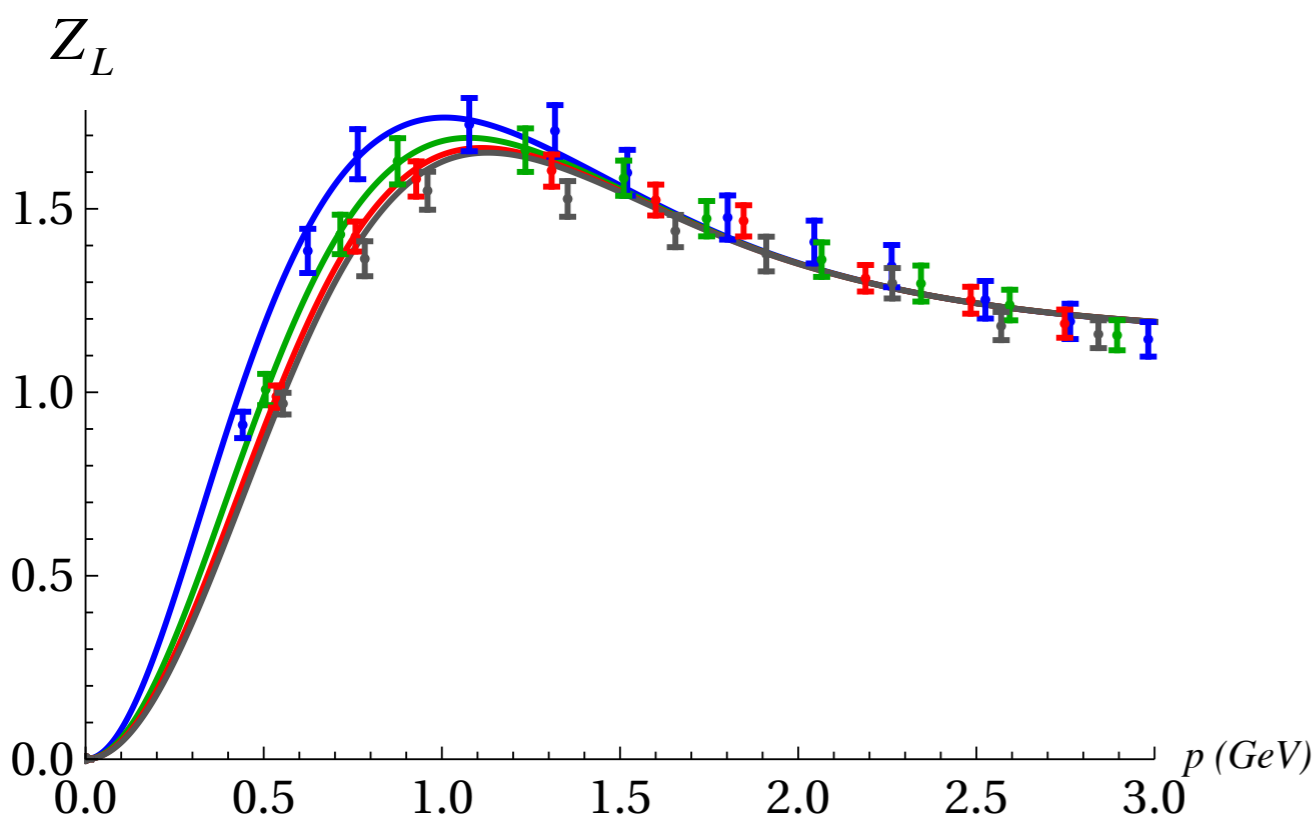
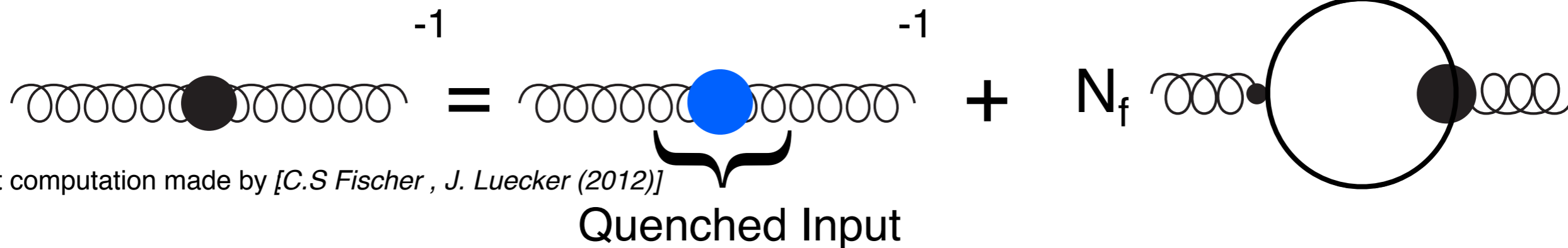
$$\Pi_T(p)p^2 \xrightarrow{p \rightarrow 0} 0$$



4

Unquenching Quark loop

● Adding the quark loop



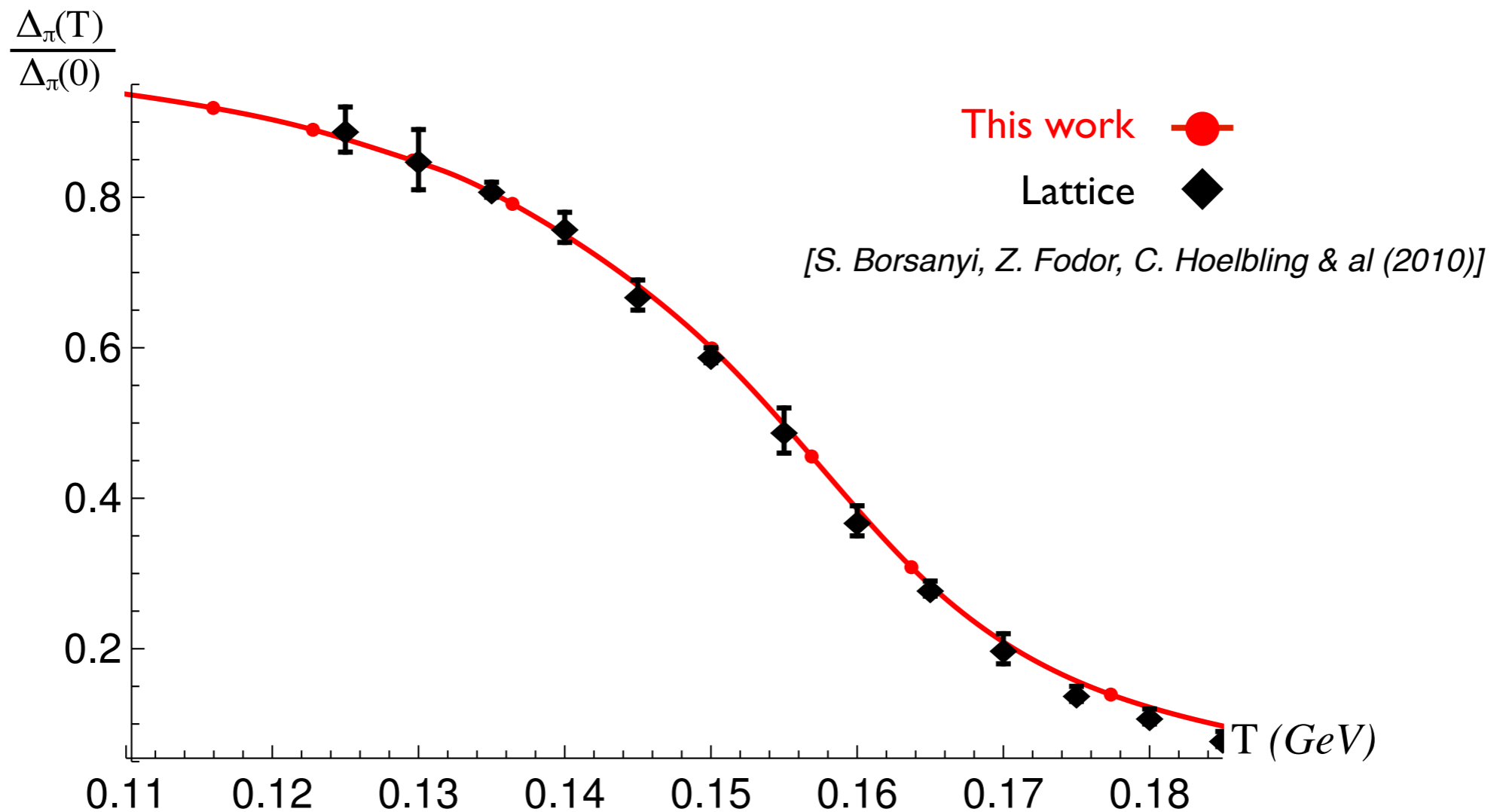
Compared to : [R.Aouane, F. Burger E.-M. Illgenfritz & al (2012)]

4 Unquenching Order parameters

Chiral condensate

➔ For 2 light flavors and a strange quark, comparison with available lattice results is possible

First computation made by : [C.S Fischer , J. Luecker (2012)]



4

Unquenching

Order parameters

Contant Romain

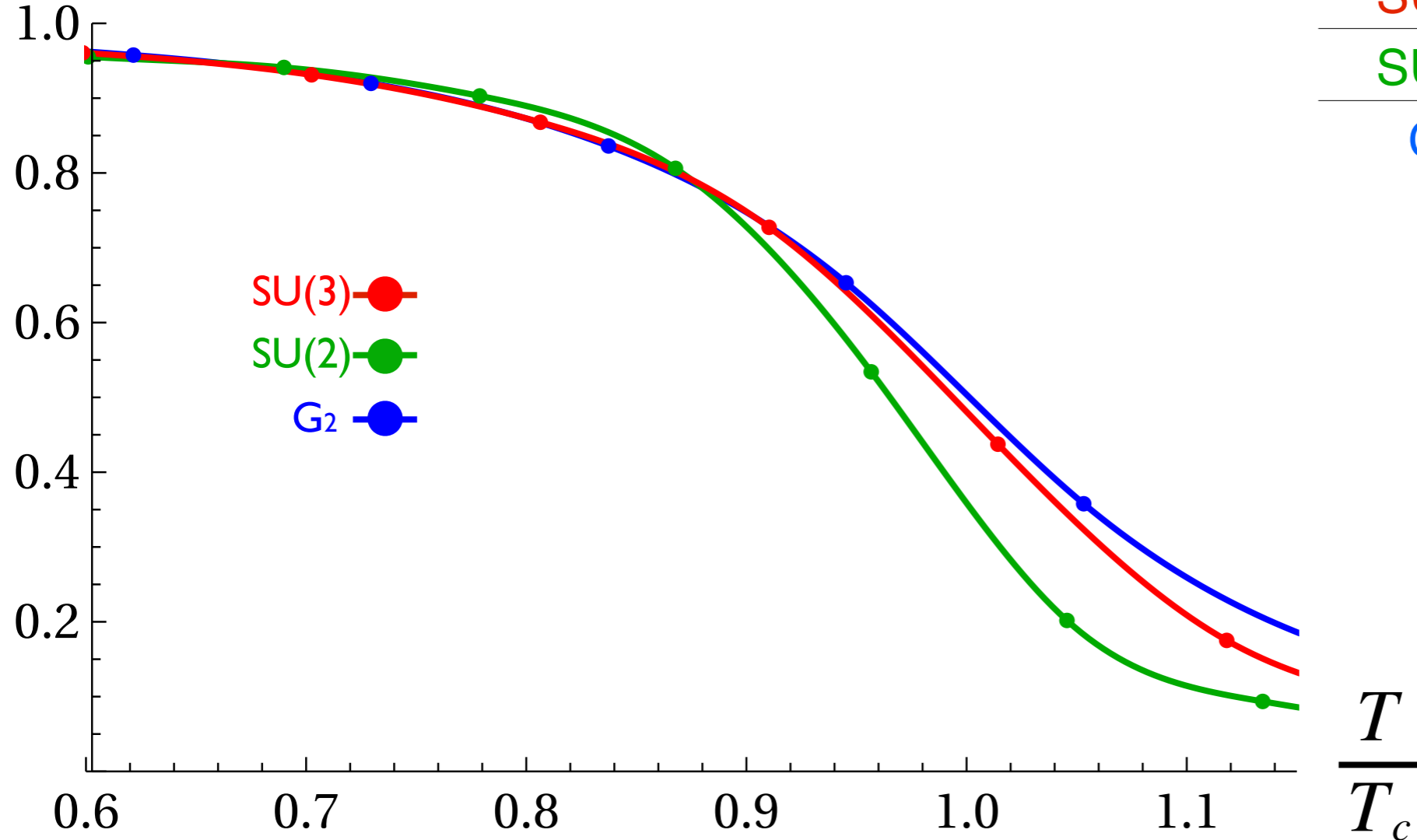
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Chiral condensate

→ For 2 light flavors :

$$\frac{\Delta_\pi(T)}{\Delta_\pi(0)}$$



Chiral «restoration» (MeV)

	T_c quenched	T_c 2 flavors
SU(3)	277	174
SU(2)	303	218
G2	255	155

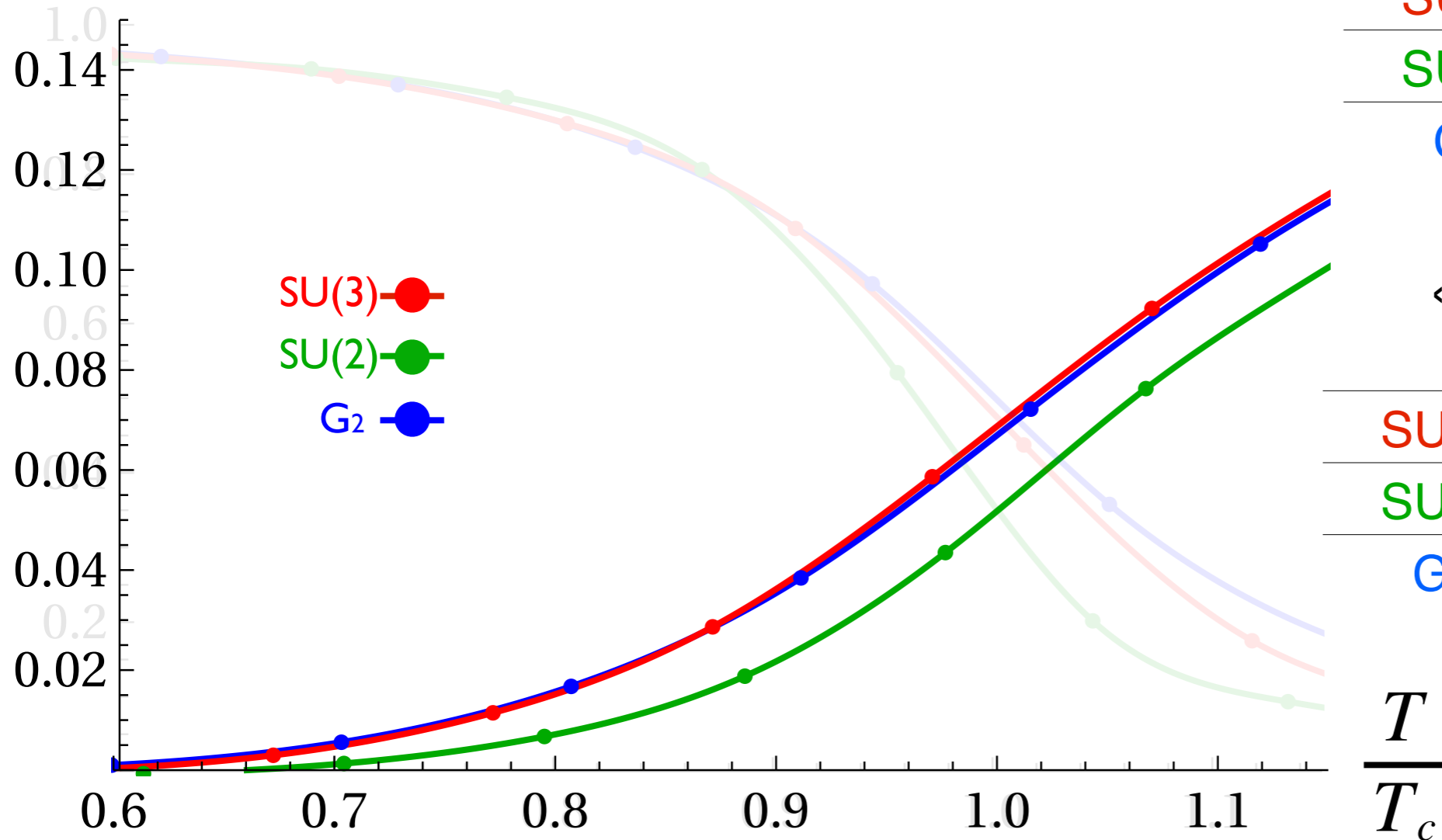
4

Unquenching Order parameters

Dual condensate

→ For 2 light flavors :

$$\frac{\Sigma_1(T)}{\Delta_\pi(0)}$$



Chiral «restoration» (MeV)

	quenched	2 flavors
SU(3)	277	174
SU(2)	303	218
G2	255	155

«Deconfinement» (MeV)

	quenched	2 flavors
SU(3)	277	182
SU(2)	303	222
G2	255	160

The confinement/deconfinement transitions and chiral transitions occur approximatively at the same temperatures

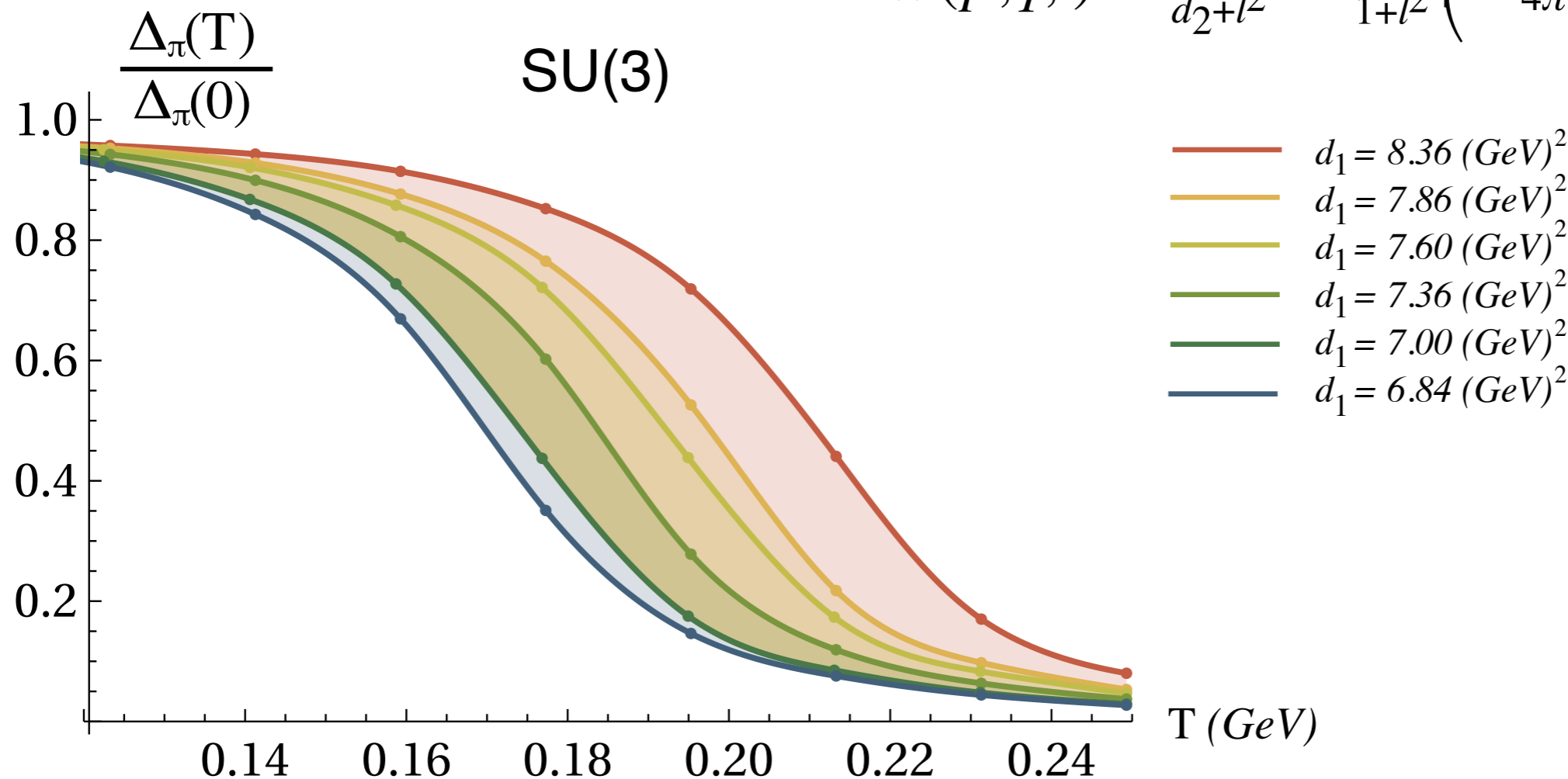
4 Unquenching Parameter variation

30/40

$$\Gamma_{q-g}(p, q, l) = \left(\frac{A(p)+A(q)}{2} \vec{\gamma}, \frac{C(p)+C(q)}{2} \gamma_4 \right) W(p, q, l)$$

$$W(p, q, l) = \frac{d_1}{d_2+l^2} + \frac{l^2}{1+l^2} \left(\frac{\beta_0 \alpha(\mu)}{4\pi} \ln(l^2+1) \right)^{2\delta}$$

→ For 2 light flavors :



→ Similar results for the QCD-like theories

A large parameter dependence of the quark-gluon vertex
Require a lot of tuning



5

Finite μ Chiral transition

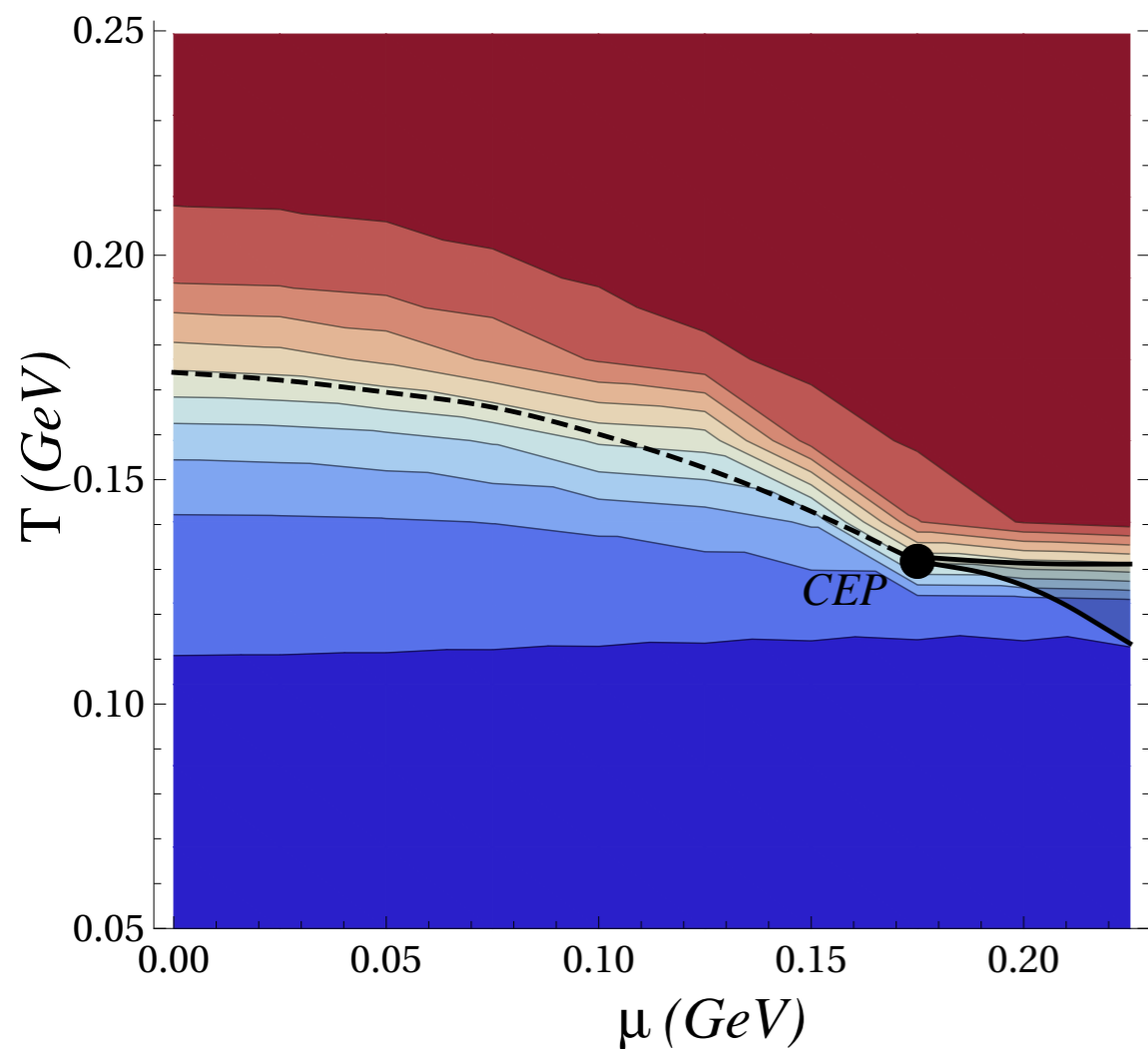
Contant Romain

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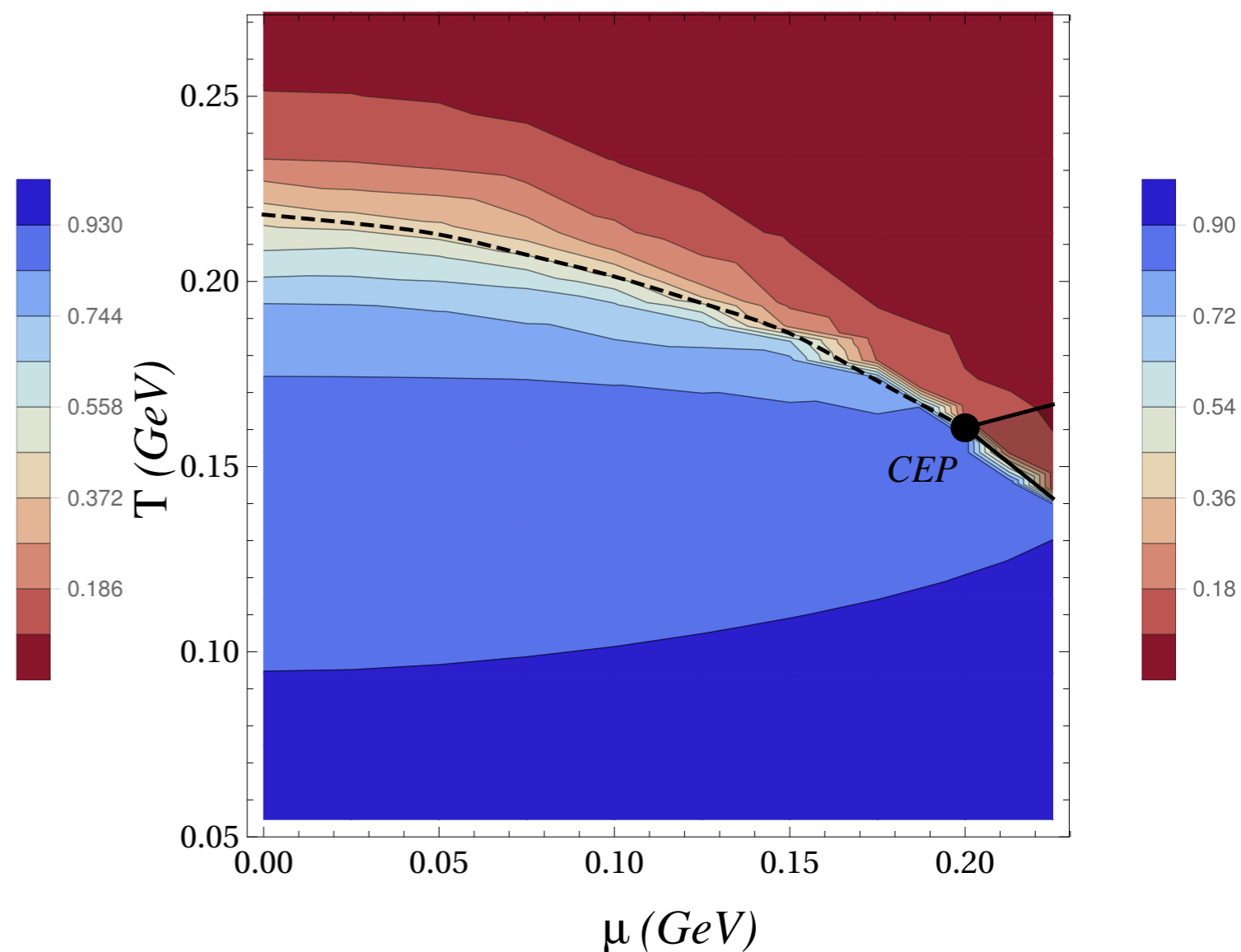
31/40

-  Shift ω_n to $\omega_n + i \mu$
-  For 2 light flavors

SU(3)

CEP \approx (175, 132) MeV

SU(2)

CEP \approx (200, 160) MeV



5

Finite μ Chiral transition

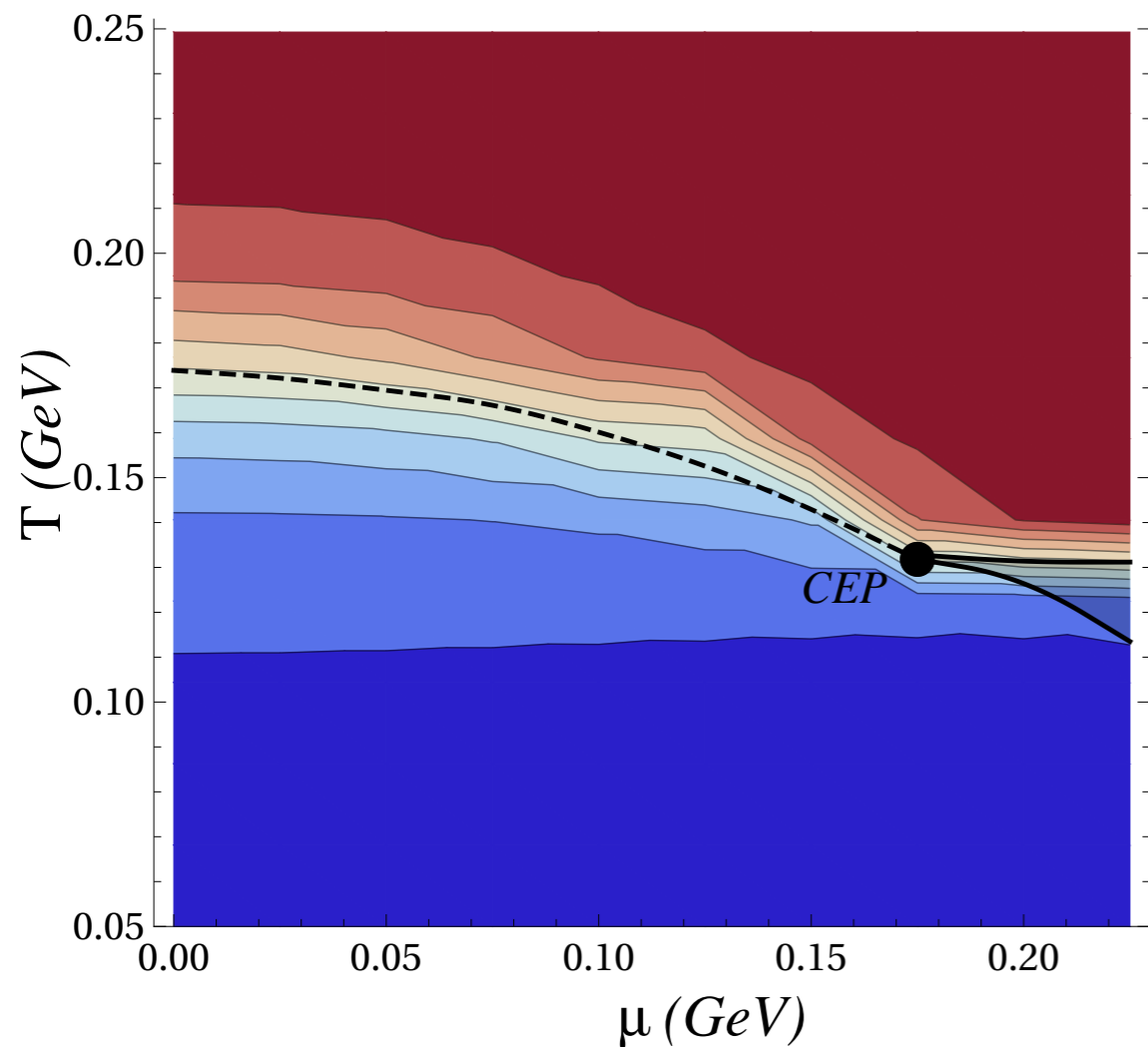
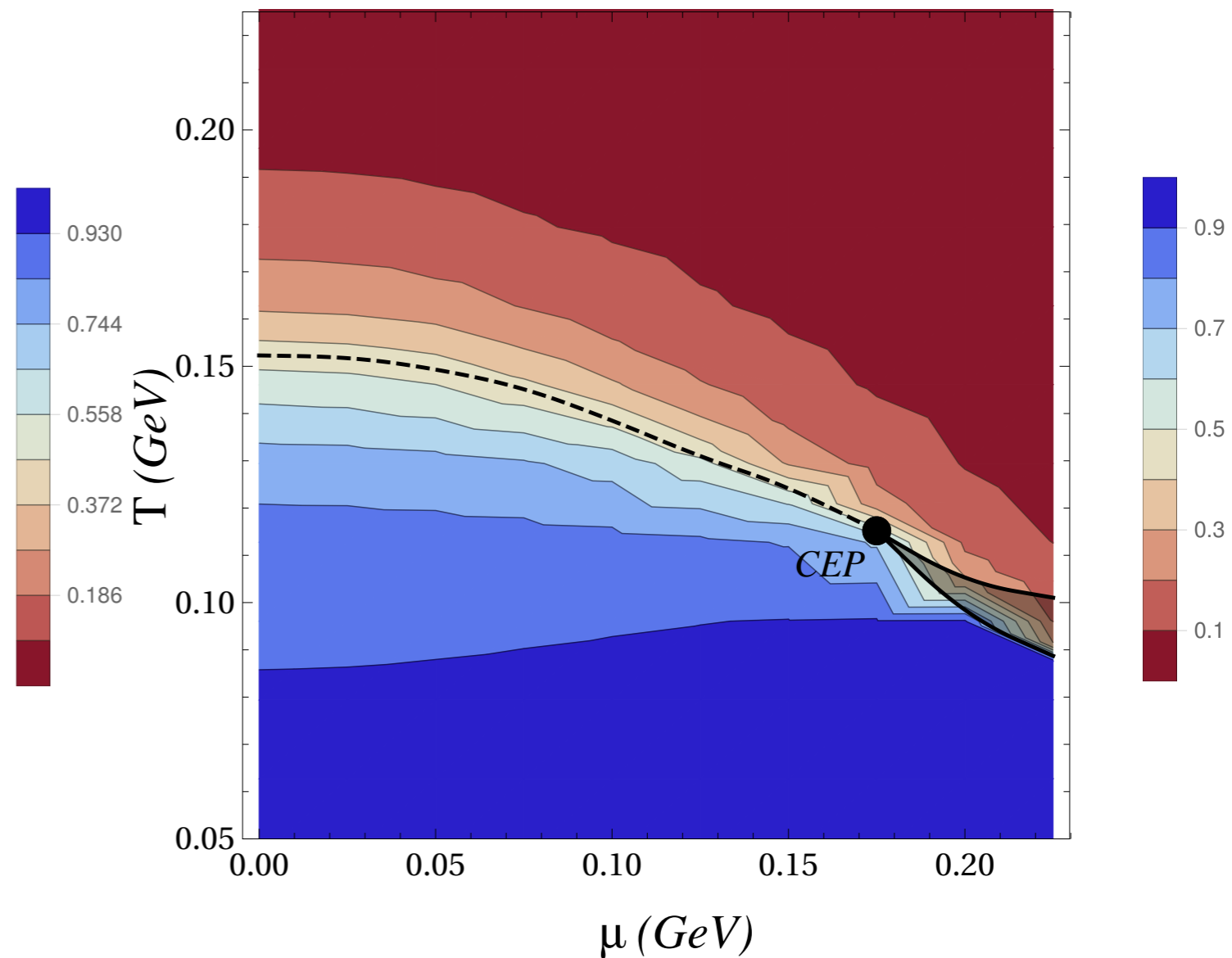
Contant Romain

ACHT 20-22 September

32/40

-  Shift ω_n to $\omega_n + i \mu$
-  For 2 light flavors

SU(3)

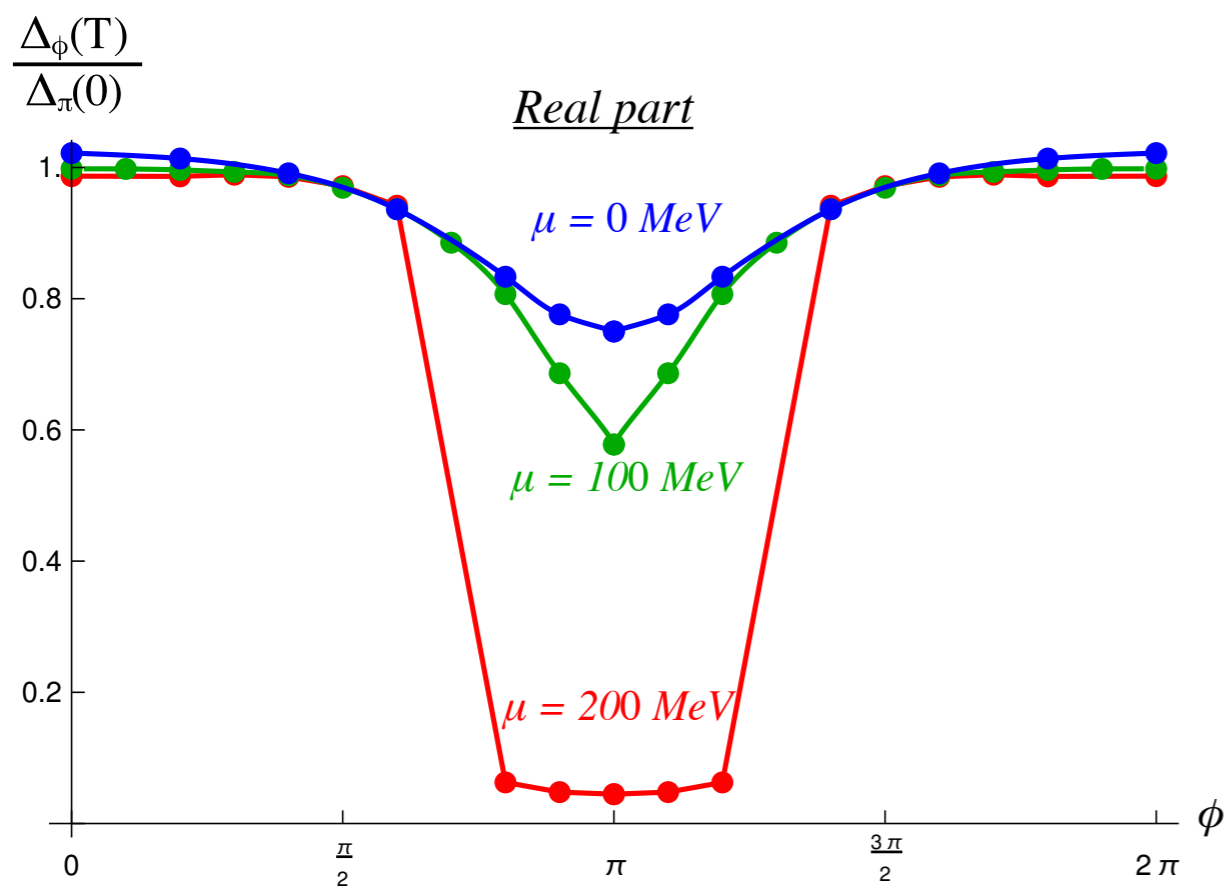
CEP \approx (175, 132) MeV G_2 CEP \approx (175, 115) MeV

5 Finite μ Preliminary : confinement

Computation on-going

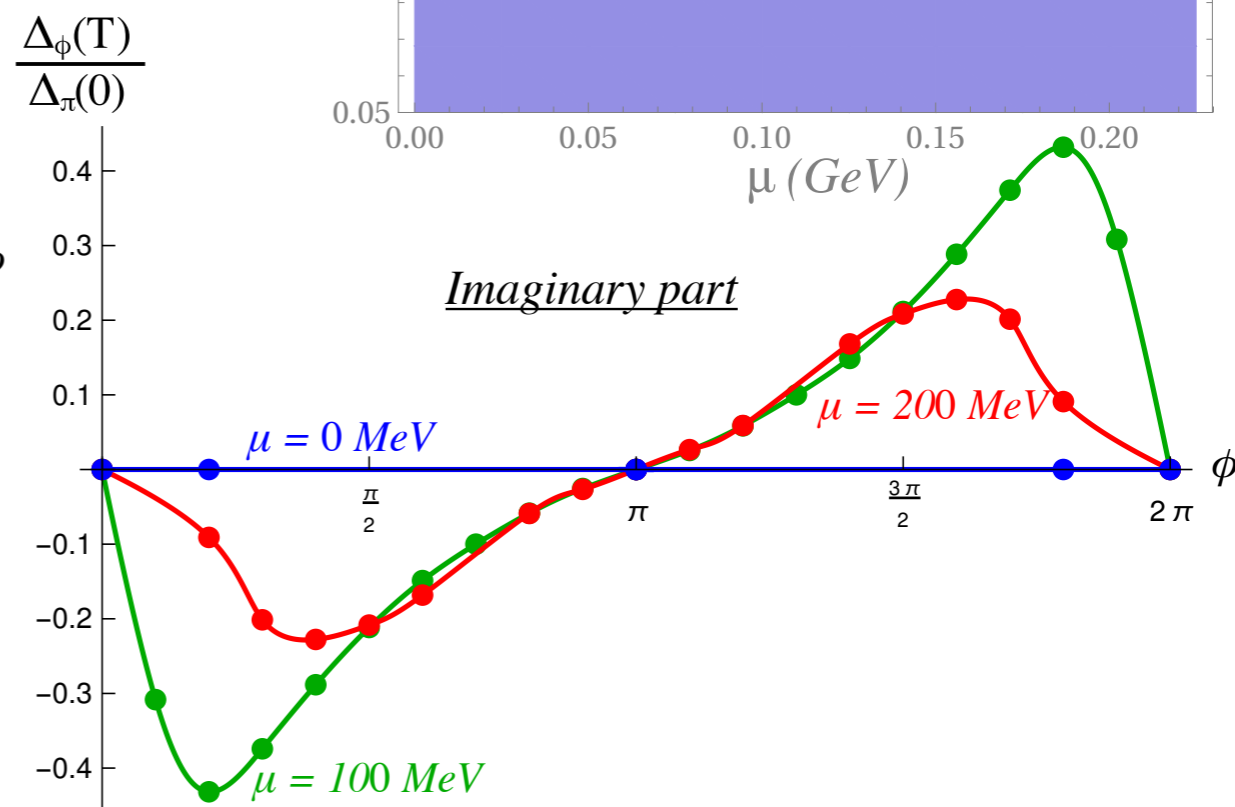
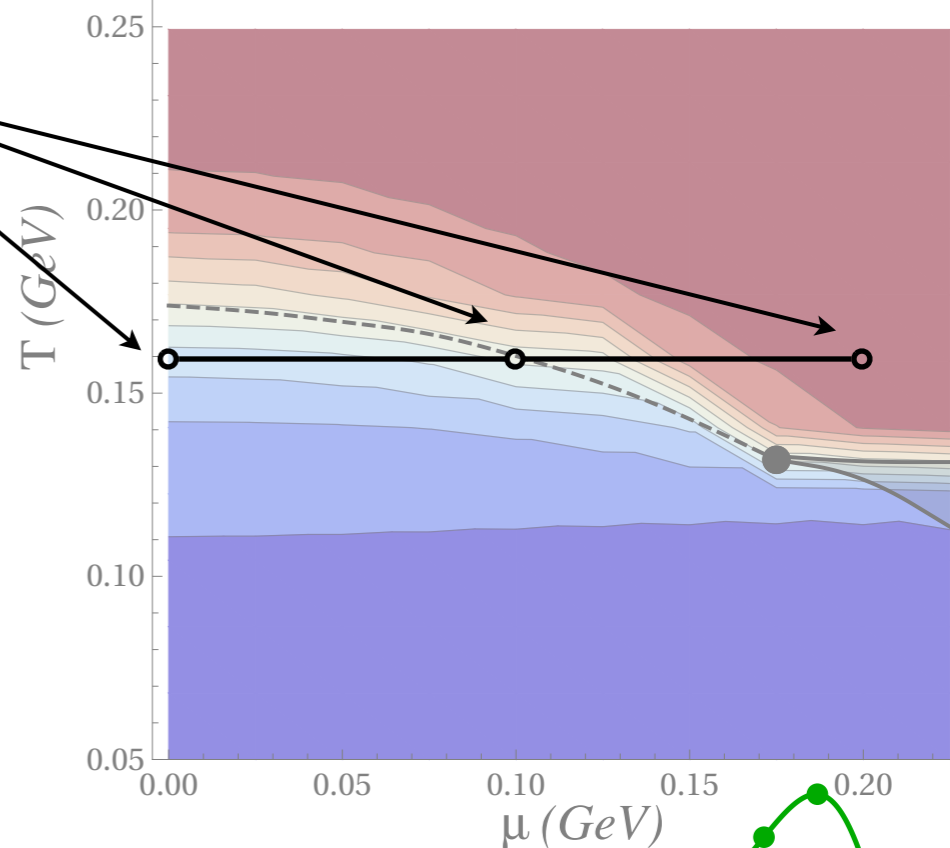
➔ Chemical potential effects on the dual condensate

● Follow the line $T = 159 \text{ MeV}$ for selected μ



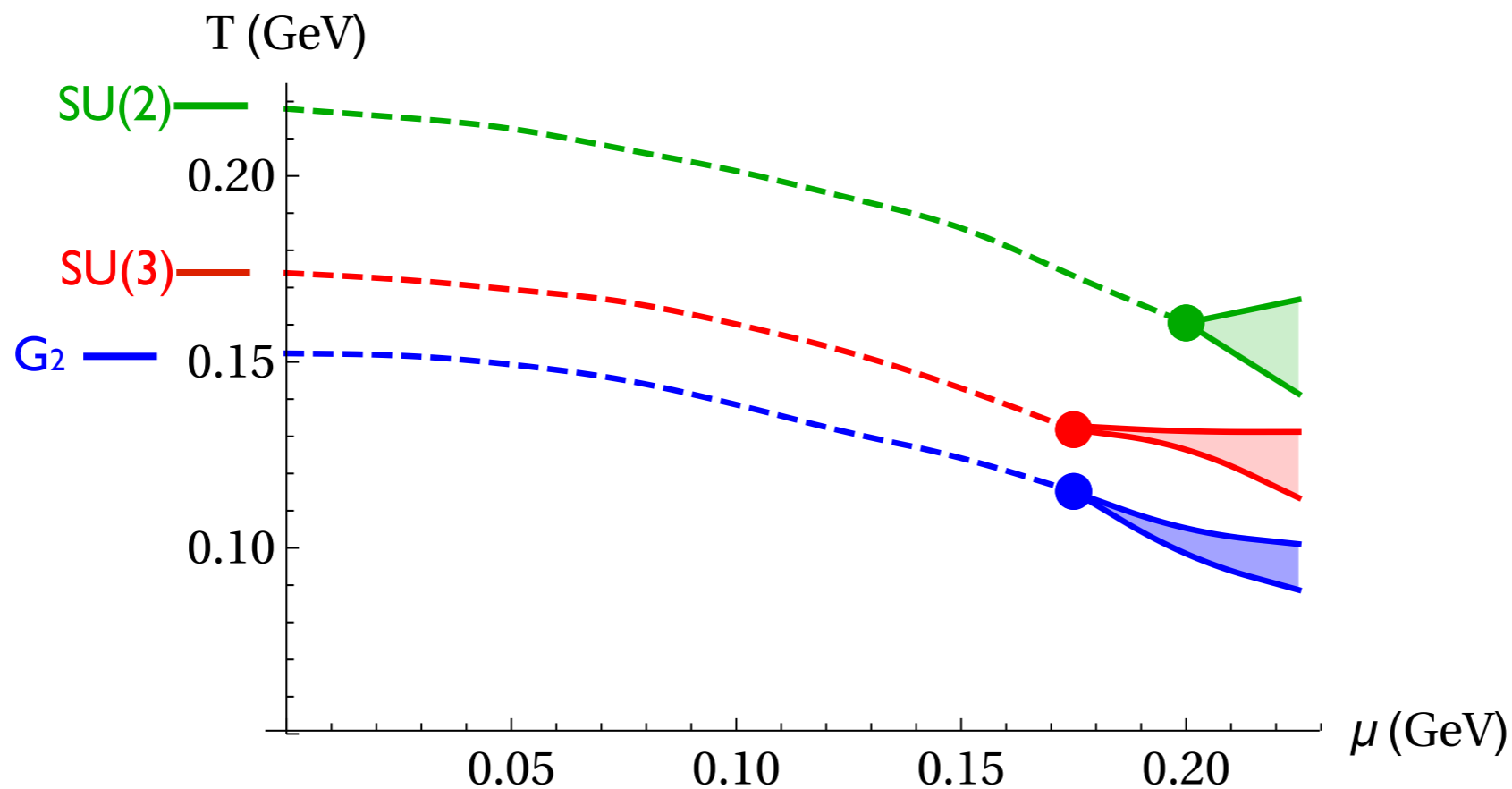
- $\mu = 0 \text{ MeV}$
- $\mu = 100 \text{ MeV}$
- $\mu = 200 \text{ MeV}$

$$\Delta_\phi(T) = Z_2(Z_m) N_c T \sum_{\omega_n(\phi)} \int \frac{d^3\vec{p}}{(2\pi)^3} \text{Tr}[S(\vec{p}, \omega_n(\phi))] \\ \omega_n = \pi T \left(2n + \frac{\phi}{\pi} \right)$$



Computation on-going

- ➔ Increase the grid resolution
- ➔ Scan the confinement properties of different QCD-like theories at finite μ
- ➔ Study of the low temperature and large μ behavior
- ➔ Diquark condensate



➔ The bending of the crossover line does not reproduce lattices results for low μ

6

Conclusion Summary

- The D dressing function can be neglected in this truncation at $\mu = 0$
- The quenched results show the expected behavior
- ➔ The truncation can be generalized for different gauge-groups
 - Ansatz for the gluon dressing
- ➔ G_2 is a good choice for an evaluation of the truncation effects in medium
- ➔ Parameter dependence of our quark-gluon vertex

6

Conclusion Summary

- The D dressing function can be neglected in this truncation at $\mu = 0$
- The quenched results show the expected behavior
 - ➔ The truncation can be generalized for different gauge-groups
 - ➔ G_2 is a good choice for an evaluation of the truncation effects in medium
 - ➔ Parameter dependence of our quark-gluon vertex
- An unquenching procedure is possible
 - ➔ The qualitative behavior of the order parameters is respected
- The qualitative behavior remains the same for different quark-gluon vertex parameters
- The (pseudo)-critical temperature for chiral and deconfinement are close to each other
 - ➔ The (pseudo)-critical temperature depends on the quark-gluon vertex parameters

6 Conclusion Summary

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- At finite μ
 - ➔ The qualitative behavior of the order parameters is respected
 - ➔ Calculated CEPs remain close for different gauge groups
 - ➔ The bending of the crossover line does not reproduce lattice result

6 Conclusion Summary

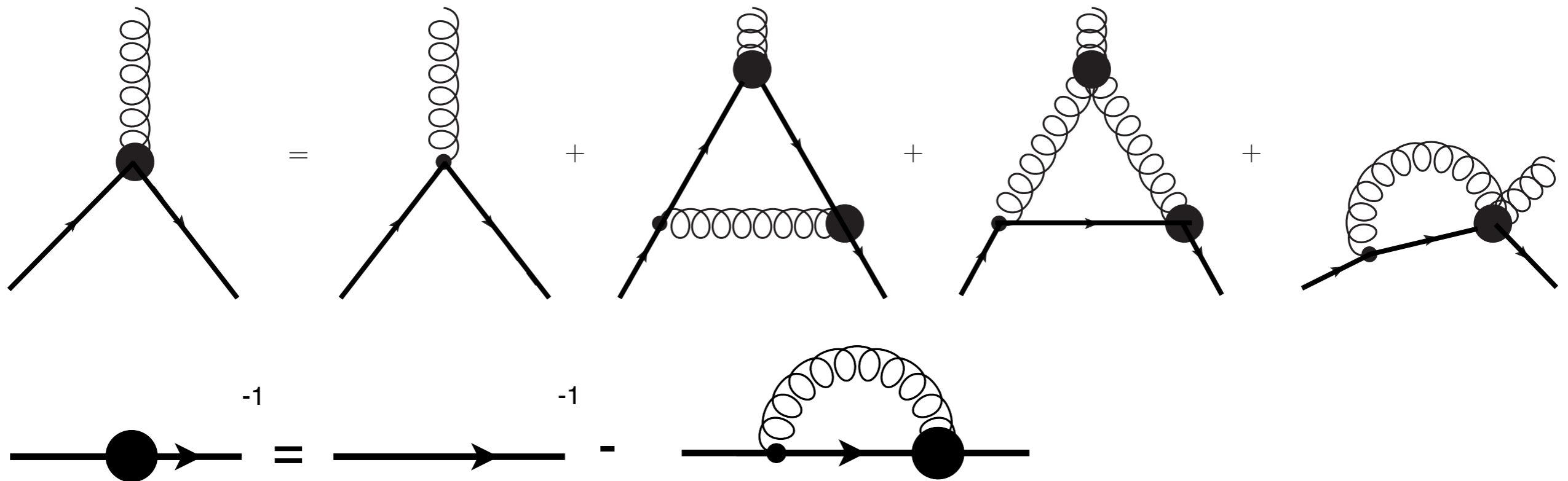
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Conclusion Outlook

- The quark-gluon vertex

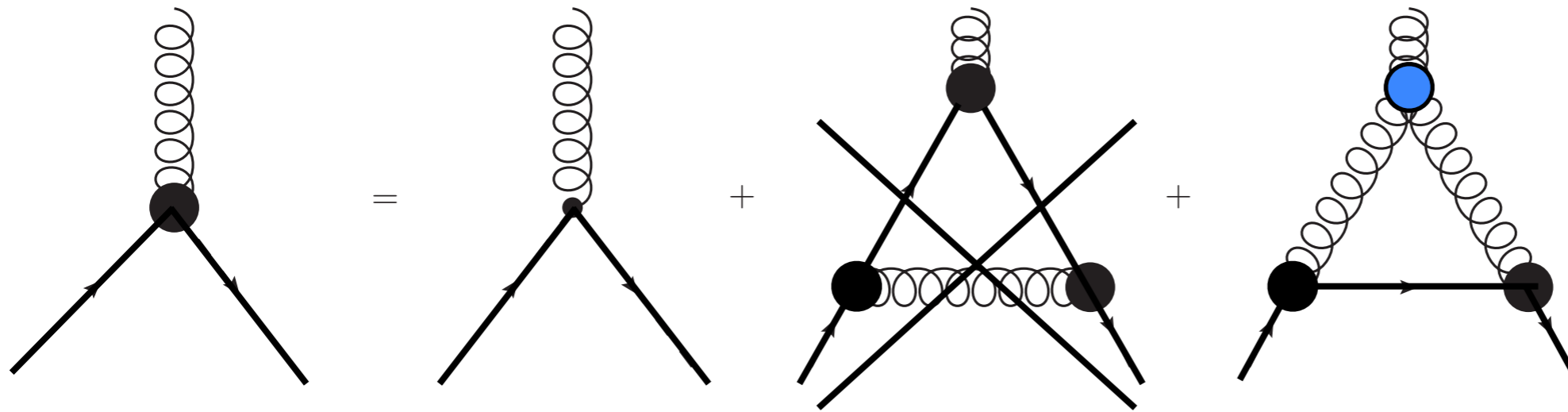
➔ New system to solve :



6 Conclusion Outlook

- The quark-gluon vertex

➔ New system to solve :



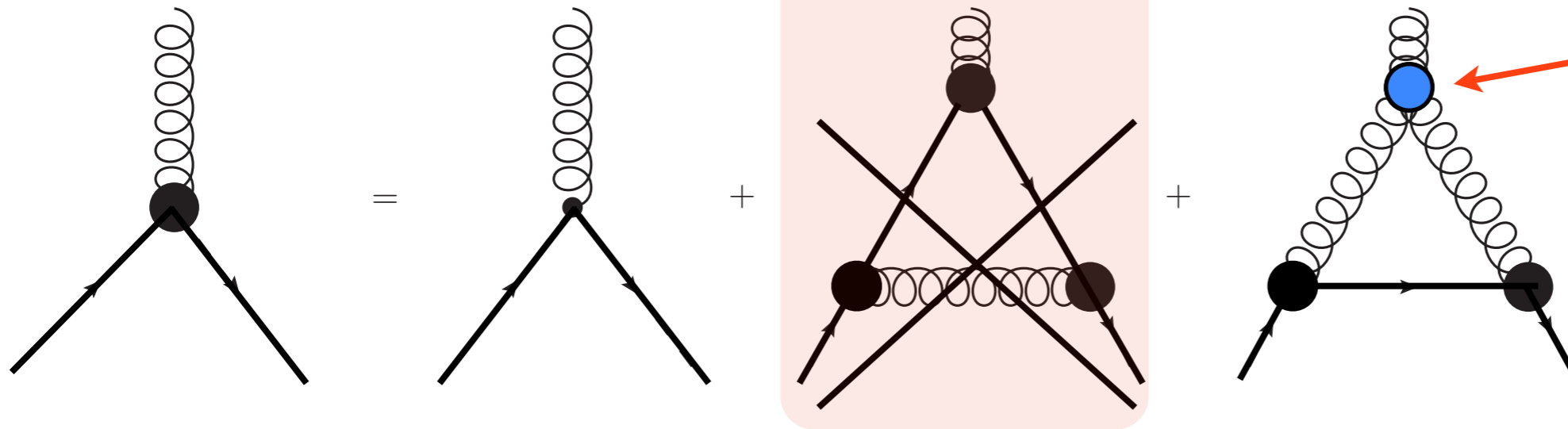
- Follow the approximation used in vacuum study

[R.Williams (2015)]

6 Conclusion Outlook

- The quark-gluon vertex

➔ New system to solve :



Relative color factor still negligible ?
Dynamical suppression after T_c ?

New correlation function
to models

- Follow the approximation used in vacuum study

[R.Williams (2015)]

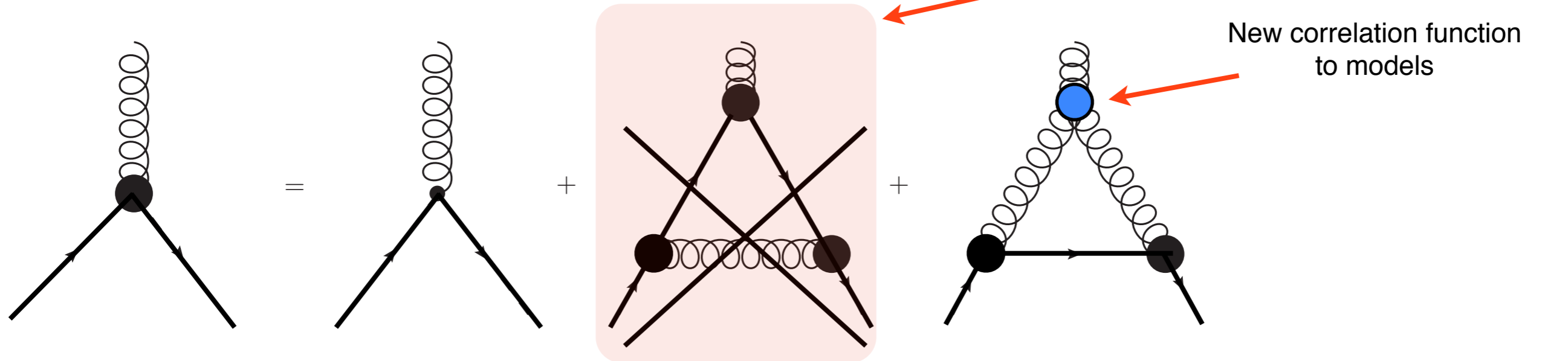


This approximation is still acceptable :
- for QCD-like theory ?
- in medium ?

6 Conclusion Outlook

- The quark-gluon vertex

➔ New system to solve :



- Follow the approximation used in vacuum study

[R. Williams (2015)]

- In Landau gauge, 24 dressings functions

$$\begin{aligned} & \vec{\gamma}h_1 + u^\mu \gamma^4 h_2 + i\vec{\gamma}\vec{l}h_3 + ii\vec{\gamma}\vec{k}_3h_4 + \vec{\gamma}[\vec{l}, \vec{k}_3]h_5 + i\vec{l}h_6 + \vec{l}\vec{l}h_7 + \vec{l}\vec{k}_3h_8 + i\vec{l}[\vec{l}, \vec{k}_3]h_9 + iu^\mu h_{10} + u^\mu \vec{l}h_{11} + u^\mu \vec{k}_3h_{12} \\ & + iu^\mu [\vec{l}, \vec{k}_3]h_{13} + i\vec{\gamma}\gamma^4 h_{14} + \vec{l}\gamma^4 h_{15} + \vec{\gamma}[\vec{l}, \psi]h_{16} + \vec{\gamma}[\vec{k}_3, \psi]h_{17} + i\vec{l}[\vec{l}, \psi]h_{18} + i\vec{l}[\vec{k}_3, \psi]h_{19} \\ & + iu^\mu [\vec{l}, \psi]h_{20} + iu^\mu [\vec{k}_3, \psi]h_{21} + i\vec{\gamma}\vec{l}\vec{k}_3\psi h_{22} + \vec{l}\vec{l}\vec{k}_3\psi h_{23} + u^\mu \vec{l}\vec{k}_3\psi h_{24} \end{aligned}$$

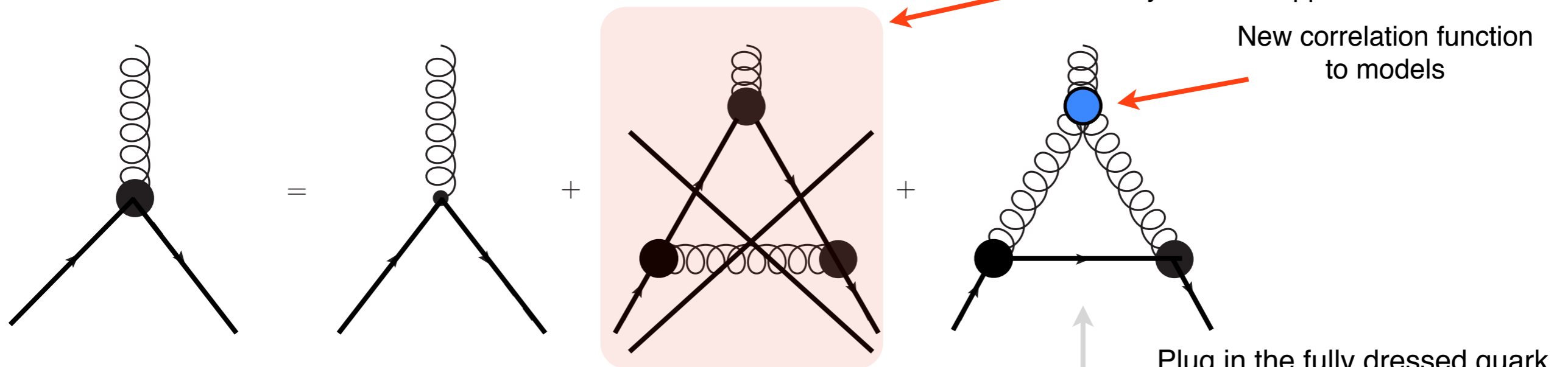
Generalization of

[M. Mitter, J.M. Pawłowski, N. Strodthoff (2014)]

6 Conclusion Outlook

- The quark-gluon vertex

➔ New system to solve :



- Follow the approximation used in vacuum study

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- In Landau gauge, 24 dressings functions

13 824 Terms

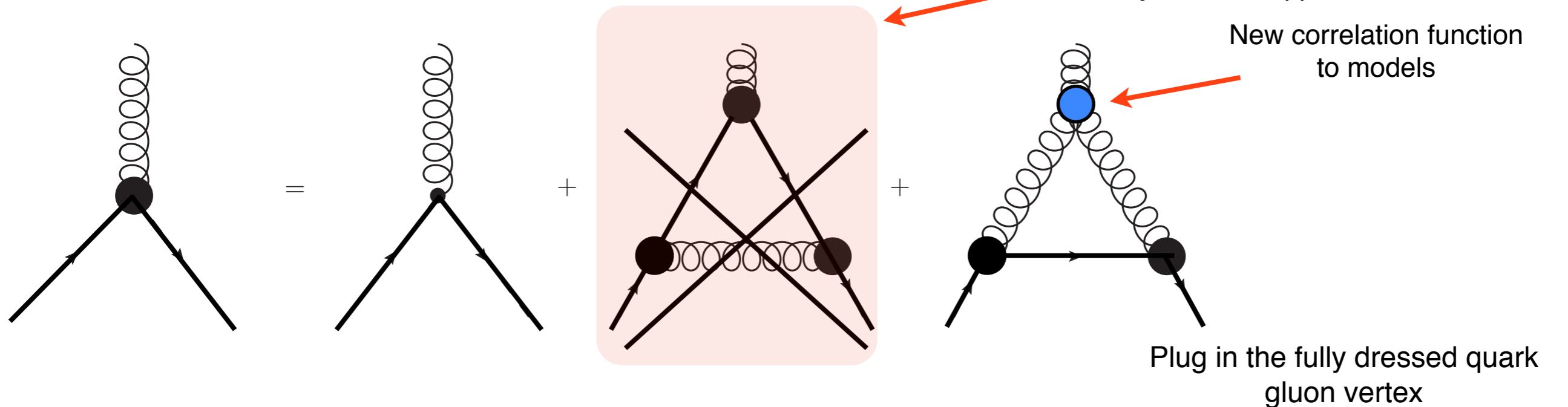
$$\begin{aligned} & \vec{\gamma}h_1 + u^\mu \gamma^4 h_2 + i\vec{\gamma}\vec{l}h_3 + ii\vec{\gamma}\vec{k}_3 h_4 + \vec{\gamma}[\vec{l}, \vec{k}_3]h_5 + i\vec{l}h_6 + \vec{l}\vec{l}h_7 + \vec{l}\vec{k}_3 h_8 + i\vec{l}[\vec{l}, \vec{k}_3]h_9 + iu^\mu h_{10} + u^\mu \vec{l}h_{11} + u^\mu \vec{k}_3 h_{12} \\ & + iu^\mu [\vec{l}, \vec{k}_3]h_{13} + i\vec{\gamma}\gamma^4 h_{14} + \vec{l}\gamma^4 h_{15} + \vec{\gamma}[\vec{l}, \psi]h_{16} + \vec{\gamma}[\vec{k}_3, \psi]h_{17} + i\vec{l}[\vec{l}, \psi]h_{18} + i\vec{l}[\vec{k}_3, \psi]h_{19} \\ & + iu^\mu [\vec{l}, \psi]h_{20} + iu^\mu [\vec{k}_3, \psi]h_{21} + i\vec{\gamma}\vec{l}\vec{k}_3\psi h_{22} + \vec{l}\vec{l}\vec{k}_3\psi h_{23} + u^\mu \vec{l}\vec{k}_3\psi h_{24} \end{aligned}$$

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6 Conclusion Outlook

- The quark-gluon vertex

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$$\vec{\gamma}h_1 + u^\mu \gamma^4 h_2 + i\vec{\gamma}\vec{l}h_3 + i\vec{\gamma}\vec{k}_3 h_4 + \vec{\gamma}[\vec{l}, \vec{k}_3]h_5 + i\vec{l}h_6 + \vec{l}\vec{l}h_7 + \vec{l}\vec{k}_3 h_8 + i\vec{l}[\vec{l}, \vec{k}_3]h_9 + iu^\mu h_{10} + u^\mu \vec{l}h_{11} + u^\mu \vec{k}_3 h_{12}$$

$$+iu^\mu [\vec{l}, \vec{k}_3]h_{13} + i\vec{\gamma}\gamma^4 h_{14} + \vec{l}\gamma^4 h_{15} + \vec{\gamma}[\vec{l}, \psi]h_{16} + \vec{\gamma}[\vec{k}_3, \psi]h_{17} + i\vec{l}[\vec{l}, \psi]h_{18} + i\vec{l}[\vec{k}_3, \psi]h_{19}$$

$$+iu^\mu [\vec{l}, \psi]h_{20} + iu^\mu [\vec{k}_3, \psi]h_{21} + i\vec{\gamma}\vec{l}\vec{k}_3\psi h_{22} + \vec{l}\vec{l}\vec{k}_3\psi h_{23} + u^\mu \vec{l}\vec{k}_3\psi h_{24}$$

Computation in progress

Generalization of
[M. Mitter, J.M. Pawłowski, N. Strodthoff (2014)]

↕
13 824 Terms

- The employed setup behaves universally
- Qualitative and quantitative comparison with lattice results at vanishing μ

- Sensitivity to the model parameters
- Low chemical potential results do not reproduce lattices results

- Improvement of the truncation in progress

Thank you