Matter-antimatter asymmetry of the Universe

András Patkós

Eötvös Loránd Tudományegyetem Természettudományi Kar Atomfizikai tanszék

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Evidence 1: Primordial nucleosynthesis Evidence 2: Cosmological Microwave Background Evidence 3: Cosmic observation of antimatter Strong 1st order EWPT with an extra scalar field Matter-antimatter separation near the bubble wall Conclusions

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Light element abundance BBN reaction network (12 reactions) observed, reconstructed

$$\eta = \frac{n_B}{s}$$

 Fractional number density in an ideal nonrelativistic gas mixture:

$$X_{i} = \frac{n_{i}}{n_{B}}, \quad \rho_{i} = \left(M_{u} + \Delta M_{i} + \frac{3}{2}T\right)n_{i}, \quad p_{i} = Tn_{i}$$
$$\rho = \sum_{i}\rho_{i} + \rho_{rad} + \rho_{\nu} + \rho_{e}, \quad p = \sum_{i}p_{i} + p_{rad} + p_{\nu} + p_{e}$$

- Expansion of the Friedmann-Lemaitre Universe: $\frac{\dot{n}_B}{n_B} = -3H, \quad \dot{\rho} = -3H(\rho + p), \quad H^2 = \frac{8\pi G_N}{3}\rho \sim T^4$
- Nuclear reaction kinetics with laboratory rates:

$$\dot{X}_{i} = \sum_{j,k,l} N_{i} \left(\Gamma_{kl \to ij} \frac{X_{l}^{N_{l}} X_{k}^{N_{k}}}{N_{l}! N_{k}!} - \Gamma_{ij \to kl} \frac{X_{i}^{N_{i}} X_{j}^{N_{j}}}{N_{i}! N_{j}!} \right)$$

• Chemical equilibrium: $n_B \sum_i Z_i X_i = n_{e^-} - n_{e^+}$

- Public codes involve reaction channels for isotopes from n, p to ${}^{15}O, {}^{16}O$, run in the range 10 MeV > T > 0.01 MeV.
- D/H varies monotonically with ρ_B e.g. (η) , produced at $z \sim 10^8$: $p(n, \gamma)D$, cosmic evolution: $D(p, \gamma)^3 He$, $D(D, n)^3 He$, $D(D, p)^3 H$ spectroscopically observed at $z \sim 2-3$ in Lyman- α clouds
- Reaction rate sensitivity: $\frac{\Delta(D/H)}{D/H} = -.32 \left(\frac{\Delta(\sigma v)}{\sigma v}\right)_{D(p,\gamma)^{3}He} - .54 \left(\frac{\Delta(\sigma v)}{\sigma v}\right)_{D(D,n)^{3}He} - .46 \left(\frac{\Delta(\sigma v)}{\sigma v}\right)_{D(D,p)^{3}H}.$
- 1% accuracy for meaningful comparison with observations; 2020 November: "long awaited and major progress" 3% accurate measurement of (σv)_{D(p,γ)³He} (LUNA, 2020), major contribution from Atomki and Konkoly Observatory¹.

• Theory predictions with CMB inputs for deuteron abundance

 $\Omega_B h^2 = 0.02237$, $N_{\nu,eff} = 3.04 + \text{nuclear reaction rates}$

Latest outputs using LUNA2020 for $(D/H)10^5$: Pisanti *et al.* (arXiv:2011.11537): 2.54 ± 0.07 Yeh *et al.* (arXiv:2011.13874): 2.51 ± 0.11 Pitrou *et al.* (arXiv:2011.11320): 2.439 ± 0.037

- Observed in 7 $Ly\alpha$ clouds (Cooke *et al.*, 2018): $(D/H)_{obs}10^5 = 2.527 \pm 0.030$
- Increased experimental accuracy results in slight signs for tension among theoretical treatments
- More Ly α clouds should be observed (several thousands are known)

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• CMB carries imprints of baryonic matter distribution at $\sim 3.8 \cdot 10^5$ yrs ($z \sim 10^3$) following BB, snapshot taken at the moment of photon decoupling from thermal equilibrium

Physics scenario

- Dark Matter forms gravitatonal potential, with fluctuations originating from inflationary quantum fluctuations grown macroscopic
- Baryon-photon plasma before decoupling oscillates in the gravitational potential, reflected by a rich peak-trough structure in the angular decomposition of CMB
- Late evolution of CMB from $z \sim 10^3$ to z = 0 is influenced by interaction with matter re-ionised in star formation

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The Planck multipole spectra

Theoretical reconstruction with dependence on cosmological parameters

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Evidence 3: Cosmic observation of antimatter

Upper curve: distance \sim 20Mpc, lower curve \sim 1Gpc



Diffuse gamma background indicates matter-antimatter boundary farther than 1Gpc Cohen, de Rujula, Glashow (1998)

Evidence 3: Cosmic observation of antimatter

increased anti-He sensitivity of AMS-2 detector on ISS



8 events compatible with $\overline{{}^{3}He}$ (6) or $\overline{{}^{4}He}$ (2) of $E \sim 2-50$ GeV too many(!) compared to $\sim 10^{8}$ detected ${}^{4}He$, ? primary cosmic ray, DM annihilation, **anti-clouds, anti-stars** ?

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Conclusion on empirical evidence

Status of matter-antimatter asymmetry is solid At percent level somewhat fluctuating



The most ambitious science story of mankind uniting observations from z = 0 to $z = 10^8$

Prelude to Electroweak Baryogenesis: Dimensional reduction

Short reminder: The case of real scalar field $\phi(\tau, \mathbf{x}) = \frac{1}{\sqrt{\beta V}} \sum_{n} \sum_{\mathbf{p}} e^{i(\omega_n \tau + \mathbf{p}\mathbf{x})} \beta \phi_n(\mathbf{p}).$

Gaussian integration in the background of the static $\Phi_0(x)$ mode: $-\beta \mathcal{F} = -\frac{\beta}{2} \int_x \left[(\nabla \Phi_0)^2 + m^2 \Phi_0^2 + \frac{\lambda}{4} \Phi_0^4 \right] \\ -\frac{1}{2} \sum_{n,p} \ln \left[\beta^2 \left(\omega_n^2 + p^2 + m^2 + 3\lambda \Phi_0^2 \right) \right].$

 $\begin{array}{l} \text{High-temperature expansion } m^2 + 3\lambda \Phi_0^2 << T^2: \\ L_{3D} = \frac{1}{2} \int_X \left[(\nabla \Phi_{3D})^2 + (m_{3D}^2 + \delta m_{3D}^2) \Phi_{3D}^2 + \frac{\lambda_{3D}}{4} \Phi_{3D}^4 \right] \\ \Phi_{3D} = \sqrt{\beta} \Phi_0, \quad m_{3D}^2 = m_{ren}^2 + \frac{\lambda_{ren} T^2}{4}, \qquad \lambda_{3D} = T\lambda_{ren} \\ \text{Location of } T_c \text{ (Landau): } m_{ren}^2 + \frac{\lambda_{ren} T_c^2}{4} = 0 \end{array}$

1-loop solution of 3D theory: $\mathcal{F} = \frac{1}{2}m_{3D}^2 \Phi_0^2 + \frac{\lambda_{ren}}{4} \Phi_0^4 - \frac{T}{12\pi} \left(m_{3D}^2 + 3\lambda_{ren} \Phi_0^2\right)^{3/2}$ Transition might turn into 1st order due to $\sim \Phi_0^3$ contribution from massless d.o.f.

Perturbative Electroweak Baryogenesis

Strategy 1985-1998 :

Thermally induced cubic potential \rightarrow 1st order $transition^2$

SU(2) invariant Higgs+Gauge theory $V_h = \frac{\lambda h^2}{2} \left(\frac{h^2}{2} - v^2\right) + V_T$ $V_T = \sum_i n_i \left(m_i^2 \frac{T^2}{24} - \frac{T}{12\pi} (m_i^2)^{3/2}\right) (n_i: \text{ multiplicity of } i\text{-th field})$ Three massive gauge fields with 3 polarisations, mass $m_i^2 = \frac{g^2 h^2}{4}$:

Resummed 1-loop approximation fails: for $m_H > 80$ GeV transition becomes crossover! (see Zsolt Szép's lecture!)

²Kuzmin, Rubakov, Shaposhnikov, PLB**155** (1985) 36⊢ ∢ ℬ ≻ ∢ ≣ ≻ ∢ ≣ ≻ → ≣

Electroweak Baryogenesis: PT with additional scalar

New strategy 2011³:

Two-step transition with classical barrier

$$V_{class} = \frac{\lambda_h}{4} \left(h^2 - v_c^2 + \frac{v_c^2}{w_c^2} S^2 \right)^2 + \frac{\kappa}{4} S^2 h^2 + \frac{1}{2} (T^2 - T_c^2) (c_h h^2 + c_s S^2)$$

Potentials of extrema at $T = T_c$ (step 2 transition):



Electroweak Baryogenesis: PT with additional scalar

Parametrisation and renormalisation at
$$T = 0$$

 $v_0^2 = v_c^2 + \frac{c_h}{\lambda_h}T_c^2$, $w_0^2 = w_c^2 + c_s \frac{w_c^4}{v_c^4} \frac{1}{\lambda_h}T_c^2$, $v_0 = 246 \text{GeV}$
Quadratic stability of SM vacuum: $c_h > \frac{w_c^2}{v_c^2}c_s$
Spectra:

$$m_{S}^{2} = \frac{1}{2} \left(\lambda_{m} + \frac{2v_{c}^{2}}{w_{c}^{2}} \lambda_{h} \right) v_{c}^{2} + \left(\frac{v_{c}^{2}}{w_{c}^{2}} - \frac{c_{s}}{c_{h}} \right) \frac{c_{s}}{c_{h}} T_{c}^{2} > 0$$

$$m_{H}^{2} = 2\lambda_{h} v_{0}^{2}, \qquad m_{H} = 125 \text{GeV}, \qquad m_{H} << m_{S}$$

Quartic stability at large
$$(h, s)$$
: $\frac{\lambda_h}{|\lambda_m|} > \frac{w_c^2}{2v_c^2}$, $\lambda_m = \kappa + 2\lambda_h \frac{v_c^2}{w_c^2}$
 $V_{1-loop} = \frac{1}{64\pi^2} \sum_{I=H,S} M_I^4(h, S) \left[\log \frac{M_I^2(h, S)}{Q^2} - C_I \right] + V_{div} + \delta V$,
 $\delta V = \delta V_0 + \frac{1}{2} \left(\delta \mu_h^2 h^2 + \delta \mu_s^2 S^2 \right) + \frac{1}{4} \left(\delta \lambda_h h^4 + \delta \lambda_{hs} h^2 S^2 + \delta \lambda_s S^4 \right)$.

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Renormalisation conditions at T = 0 for $V = V_{class} + V_{1-loop}$

Principle of minimal sensitivity applied $\frac{\partial V_{1-loop}}{\partial h}_{(v_0,0)} = \frac{\partial V_{1-loop}}{\partial S}_{(0,w_0)} = 0 \Leftrightarrow \text{ no change of } v_0, w_0$ $\frac{\partial^2 V_{1-loop}}{\partial S^2}_{(v_0,0)} = \frac{\partial^2 V_{1-loop}}{\partial h^2}_{(v_0,0)} = 0 \Leftrightarrow \text{ unchanged spectra}$ $V_{1-loop}|_{(v_0,0)} = V_{1-loop}|_{(0,w_0)} = 0 \Leftrightarrow V_{class}(T=0) \text{ maintained}$

Parameters λ_h , v_0 , λ_m , w_0 , T_c 2 fixed in the Higgs sector



Electroweak Baryogenesis: PT with additional scalar

The potential
$$V_{T=0,ren}[\lambda_h, v_0, \lambda_m, w_0, T_c] + V_T$$

 $V_T = \frac{T^4}{2\pi^2} \sum_{I=B,F} N_I \int_0^\infty dx x^2 \log \left[1 \pm e^{-(x^2 + m_I^2/T^2)}\right]$
 $- \frac{T}{12\pi} \sum_B N_B \left[m_B^2 + c_B T^2\right]^{3/2}$

Scenario of thermal evolution during the cooling of Universe⁴

- Cooling system starts in the symmetric phase and Z(2) violating transition at $T_S \approx \left(T_c^2 + \frac{\lambda_h}{c_s} \frac{v_c^4}{w_c^2}\right)^{1/2}$. (Step 1)
- Further cooling: 1st order transition to the SM Higgs vacuum at modified transition temperature T_c^{new} . (Step 2, EWBG)
- Bubble nucleation starts at T_{nucl} below T_c (super-cooling)

⁴J.R. Espinosa *et al.* NPB**854**, 592 (2012) < ロトイクトイミトイミト ミークへの

EWBG: Bubble-wall with additional scalar

Nucleation temperature T_{nucl}

Nucleation speed per unit volume : $\Gamma_N(T) = T^4 \left(\frac{S_3}{2\pi T}\right)^{3/2} e^{-S_3/T}$ Competing with expansion rate: one bubble in 1 Hubble volume: 4π 1 $\Gamma_N(T) \simeq H(T)$

$$\overline{3} \, \overline{H(T_n)^3} \, {}^{\mathsf{I}} \, {}^{\mathsf{N}} \, (\overline{I_n}) \approx H(\overline{I_n})$$

The surface energy S_3 in thin wall approximation⁵

$$S_3 = \int_{-\infty}^{\infty} dz \left[\frac{1}{2} \left((\partial_z h)^2 + (\partial_z S)^2 \right) + V(h, s, T) \right],$$

$$h(-\infty) = 0, \quad h(\infty) = v(T), \quad S(-\infty) = w(T), \quad S(\infty) = 0$$



András Patkós

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EWBG: Bubble-wall with additional scalar

Bubble profile (using tree-level potential)^{6,7}

Nearby path close to
$$V_{barrier}$$
:
 $h(z) = v_c \sin \varphi(z), \quad S(z) = w_c \cos \varphi(z),$
 $\varphi(z) = \frac{\pi}{4} \left(1 + \tanh \frac{z}{L_w} \right), \quad \varphi(-\infty) = 0, \quad \varphi(\infty) = \frac{\pi}{2}$
 $V_{class}[\varphi] = \frac{\kappa}{4} v_c^2 w_c^2 \sin^2 \varphi \cos^2 \varphi, \quad V_{barrier} \approx \frac{\kappa}{16} v_c^2 w_c^2$
 $S_3 = \frac{\alpha}{L_w} (v_c^2 + w_c^2) + \beta L_w V_{barrier}, \quad L_w = ?$
 $\alpha \approx \int_0^{\pi/2} d\varphi \varphi \left(1 - \frac{2\varphi}{\pi} \right), \quad \beta \approx 2 \int_0^{\pi/2} d\varphi \sin^2 \varphi \cos^2 \varphi \frac{1}{\varphi(1 - \frac{2\varphi}{\pi})}.$

⁶J.R. Espinosa *et al.* JCAP 01(2012) 012, ⁷J.M. Cline *et al.* PRD**95** 115006 (2017) S coupled with massive fermion χ $\Delta L = \bar{\chi}[i\gamma_{\mu}\partial^{\mu} - m_{\chi} - (mP_R + m^*P_L)S]\chi$ Let m = i|m|, then in the bubble wall: $\Delta L = \bar{\chi}[i\gamma^{\mu}\partial^{\mu} - M(z)e^{i\gamma_5\Theta(z)}]\chi$, $M^2(z) = m_{\chi}^2 + |m|^2S^2(z)$, $\Theta(z) = \arctan\left(\frac{|m|S(z)}{m_{\chi}}\right)$ $\Theta = \Theta(x)$ cannot be removed by $\psi \to e^{-i\gamma_5\Theta/2}\psi$, since it reappears in the kinetic term

CP-violation basics CP-transformation, fermions:

$$\begin{split} \psi &\to i\gamma^2\gamma^0\psi^*, \qquad \psi^\dagger \to \psi^T\gamma^0\gamma^2i\\ \text{Consequence: } \bar{\psi}e^{i\Theta\gamma_5}\psi \to \bar{\psi}e^{-i\Theta\gamma_5}\psi\\ \Theta(z)\text{: space-dependent CP-violating feature of the construction}\\ CP[\Theta(z)] &= -\Theta(z) \end{split}$$

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Semiclassical solution of Dirac equation with complex mass^{8,9}:
$$\begin{split} m &= |m|e^{i\Theta} \\ (i\gamma^{\mu}\partial_{\mu} - mP_R - m^*P_L)\psi = (i\gamma^{\mu}\partial_{\mu} - me^{i\gamma_5\Theta})\psi = 0 \\ \text{One-dimensional variation accross the bubble-wall:} \\ \psi_s &= e^{-i\omega t} \begin{pmatrix} L_s \\ R_s \end{pmatrix} \chi_s, \quad \sigma_3\chi_s = s\chi_s \\ (\omega - is\partial_z)L_s - mR_s = 0, \quad (\omega + is\partial_z)R_s - m^*L_s = 0 \\ \text{or} \\ (\omega + is\partial_z)\frac{1}{m(z)}(\omega - is\partial_z)L_s = 0, \quad (\omega - is\partial_z)\frac{1}{m^*(z)}(\omega + is\partial_z)R_s = 0 \end{split}$$

WKB trial wave function:

$$L_s = w_L(z)e^{i\int^z p(z')dz'}, \qquad R_s = w_R(z)e^{i\int^z p(z')dz'}$$

⁸M. Joyce *et al.*, Phys. Rev. Lett. 75, 1695 (1995)
 ⁹J. M. Cline *et al.* JHEP 0007, 018 (2000)

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Matter-antimatter separation near bubble-wall

Solution for L_s Real part: $\omega^2 - |m|^2 - p(z)^2 + (s\omega + p)\Theta' - \frac{|m|'w'}{|m|w} + \frac{w''}{w} = 0$ Imaginary part: $2pw' + p' - \frac{|m|'}{|m|}(s+p)w - \Theta'w' = 0$ Perturbative solution assuming slow variation of w, p, Θ $p^{(0)} = \operatorname{sign}(p) \sqrt{\omega^2 - |m|^2} \equiv p_0$ $p^{(1)} = (p_0^2 + (s\omega + p_0)\Theta')^{1/2} \to p_0 + \frac{s\omega + p_0}{2m}\Theta'$ CP-transformed Dirac equation $\Theta \to -\Theta$ $p^{(1)} = p_0 + \frac{s_{CP}}{2p_0} \frac{s_{\omega} + p_0}{2p_0} \Theta'$ Influence of the phase transformation of $\psi \to e^{i\alpha(z)}\psi$: $p_{l}^{(1)} = p_{0} + s_{CP} \frac{s\omega}{2m} \Theta' + \frac{\Theta'}{2} + \alpha' \equiv p_{0} + \frac{s_{CP} s_{2m}}{2m} \Theta' + \alpha_{CP,L}$ Result of the analysis of the equation of R_s : $p_{R}^{(1)} = p_{0} + s_{CP} \frac{s_{\omega}}{2p_{0}} \Theta' - \frac{\Theta'}{2} + \alpha' \equiv p_{0} + \frac{s_{CP} s_{2p_{0}}}{2p_{0}} \Theta' + \alpha_{CP,R}$ Dispersion relation: $\omega = \left((p - \alpha_{CP})^2 + |m|^2 \right)^{1/2} - \frac{\Theta'}{2}$.

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Canonical equations:

$$\begin{aligned} \mathbf{v}_{g} &= \frac{\partial \omega}{\partial p} = \frac{p_{0}}{\omega} \left(1 + s_{CP} s \frac{|m|^{2}}{2p_{0}^{2} \omega} \Theta' \right) \equiv \frac{p_{kin}}{\omega}, \qquad \dot{p} = -\frac{\partial \omega}{\partial z} \\ \dot{p}_{kin} &= \omega \dot{v}_{g} = \omega (\dot{z} \partial_{z} v_{g} + \dot{p} \partial_{p} v_{g}) \\ F &= -\frac{|m||m|'}{\omega} + s_{CP} s \frac{1}{2\omega^{2}} (|m|^{2} \Theta')' \end{aligned}$$

Second term distinguishes (anti-)fermion with spin projection s(-s) and (anti)-fermion with spin projection -s(s)

Boltzmann-equation for the distribution of particles/antiparticles in the neighbourhood of the bubble-wall $% \left[\left({{{\left[{{{\left[{{\left[{{\left[{{\left[{{{\left[{{{\left[{{{\left[{{{\left[{{{\left[{{{\left[{{{\left[{{{\left[{{{}}}} \right]}}} \right.}$

$$\dot{f}_i + \frac{p_{kin}}{|m|} \frac{\partial f_i}{\partial z} + \dot{p}_{kin} \frac{\partial f_i}{\partial p_{kin}} = \text{scattering terms}$$

In the frame of the bubble-wall, assuming local thermal equilibrium:

$$\dot{f}_i = 0, \qquad f_i = \left(e^{\beta(\gamma(\omega_i - v_{wall}p_{kin}) - \mu_i)}\right)^{-1} + \delta f_i$$

Matter-antimatter separation near bubble-wall

 $\begin{array}{l} \mu_i, \delta f_i \text{ from the first two moments of the Boltzmann equation} \\ \text{Elimination of } \delta f_i \text{ leads to diffusion equations for } \xi_i = \mu_i/T: \\ -D_i\xi_i'' - v_w\xi_i' + \sum_r \left(\Gamma_r(l+m \to i+j) - \Gamma_r(i+j \to l+m) \right) = S_i \\ \text{CP-dependent source term: } S_i = \frac{v_{wall}D_i}{\langle v_g^2 \rangle T} \langle v_g \frac{(|m|^2 s_{CP} s \Theta')'}{2\omega^2} \rangle \end{array}$

Solution with Green's method leads to helicity state separation



Matter-antimatter separation: model building II.

Transformation into τ -lepton asymmetry by massive Majorana fermion χ coupled with inert scalar dublet ϕ to τ -leptons^{10,11}:

$$\Delta L = y \bar{L}_{\tau} \phi P_R \chi + \text{h.c.}$$

• Helicity state separation in the bubble-wall

- $\chi \tau_L \leftrightarrow \phi$: Helicity asymmetry of χ transfered to $\tau \overline{\tau}$
- Lepton-asymmetry transfered to quarks through sphaleron mediated processes

¹⁰ J.M. Cline *et al.* PRD**95** 115006 (2017) ¹¹ j.M. Cline," Is electroweak baryogenesis dead?", arXiv:1704.08911 (≧) ≧ <

Conclusions

- Real scalar field represents a simplest extension of SM possessing sufficient number of new couplings for strong 1st order phase transition
- CP-violating coupling of the scalar to new fermions provides additional strength to matter-antimatter separation in the electroweak bubble wall
- Question for public poll: Is EWBG dead?
- There are other attractive constructions, but experimental guidance for model building is missing!.

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